# t12 member_1 <br> (TMR96BDfsbUAp4RUHefRSgVTgXA6RXoZZU5) 

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Let $v 1_{\_}$membered : $\iota \Rightarrow 0$ be given. Let $v 1_{\_} x c m p l x_{-} 0: \iota \Rightarrow 0$ be given. Let $k 1_{\_}$binop_2 : $\iota \Rightarrow \iota$ be given. Let $k 5 \_$member_1 : $\iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{align*}
& \forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(( \right. \\
& \left.\left.X 1 \in X 0) \Leftrightarrow\left(k 1 \_b i n o p \_2 X 1 \in k 5 \_m e m b e r \_1 X 0\right)\right)\right) \tag{1}
\end{align*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(k 5 \_m e m b e r \_1\left(k 5 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{2}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right) \tag{3}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow(( \right.$
$\left.\left.\left.k 1 \_b i n o p \_2 X 1 \in X 0\right) \Leftrightarrow\left(X 1 \in k 5 \_m e m b e r \_1 X 0\right)\right)\right)$

