

t12_mesfun9c
(TMKWsdsk4k8m8nbfPgC4DAxro7w6u8vhjSf)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k5_numbers : \iota$ be given. Let $k4_partfun1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_numbers : \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v7_ordinal1 : \iota \Rightarrow o$ be given. Let $v1_mesfunc8 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_mesfunc5 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_numbers : \iota$ be given. Let $k1_seq_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_series_1 : \iota \Rightarrow \iota$ be given. Let $k10_seqfunc : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_mesfun9c : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_mesfunc9 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_mesfun7c : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_numbers : \iota$ be given. Let $k4_mesfunc9 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_mesfunc9 : \iota \Rightarrow \iota$ be given. Let $k1_mesfunc5 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_mesfunc9 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_mesfunc5 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k4_ordinal1 : \iota$ be given. Let $r1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_rfunct_3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v3_valued_0 : \iota \Rightarrow o$ be given. Let $v2_valued_0 : \iota \Rightarrow o$ be given. Let $v3_ordinal1 : \iota \Rightarrow o$ be given. Let $v3_membered : \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v2_membered : \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. ((v1_funct_1 X1) \wedge (\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers)) \wedge (m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers)))))) \Rightarrow \\ & (v2_mesfunc9 (k1_mesfun7c X0 X1) X0)) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. ((v1_funct_1 X1) \wedge (\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers)) \wedge (m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers)))))) \Rightarrow \\ & (r2_funct_2 k5_numbers (k4_partfun1 X0 k7_numbers) (k4_mesfunc9 \\ & X0 (k1_mesfun7c X0 X1)) (k1_mesfun7c X0 (k2_mesfun9c X0 X1)))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1_funct_1 X0) \wedge ((v1_funct_2 X0 k5_numbers k1_numbers) \wedge \\ & (m1_subset_1 X0 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers k1_numbers)))))) \Rightarrow \\ & (r2_funct_2 k5_numbers k7_numbers (k2_mesfunc9 (k1_mesfunc5 \\ & k5_numbers X0)) (k1_mesfunc5 k5_numbers (k3_series_1 X0))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge (\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k7_numbers)) \wedge (m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k7_numbers)))))) \Rightarrow \\ & (\forall X2.(v7_ordinal1 X2) \Rightarrow (\forall X3.(m1_subset_1 X3 X0) \Rightarrow \\ & (\forall X4.((v2_mesfunc9 X1 X0) \wedge ((v1_mesfunc8 X1 X0 k7_numbers) \wedge \\ & ((r1_tarski X4 (k1_relset_1 X0 (k4_mesfunc5 X0 k7_numbers X1 k6_numbers))) \wedge \\ & (X3 \in X4)))) \Rightarrow (k1_mesfunc9 (k2_mesfunc9 (k3_mesfunc5 X0 X1 X3)) \\ & X2 = k1_mesfunc9 (k3_mesfunc5 X0 (k4_mesfunc9 X0 X1) X3) X2)))))) \end{aligned} \quad (4)$$

Assume the following.

$$m1_subset_1 k1_xboole_0 k4_ordinal1 \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge (\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers)) \wedge (m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers)))))) \Rightarrow \\ & (\forall X2.(m1_subset_1 X2 X0) \Rightarrow (r1_funct_2 k5_numbers k1_numbers \\ & k5_numbers k7_numbers (k10_seqfunc X0 X1 X2) (k3_mesfunc5 X0 (k1_mesfun7c \\ & X0 X1) X2)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v1_funct_1 X2) \wedge \\ & ((v1_funct_2 X2 X0 X1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 \\ & X0 X1)))))) \wedge ((v1_funct_1 X3) \wedge ((v1_funct_2 X3 X0 X1) \wedge (m1_subset_1 \\ & X3 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1)))))) \Rightarrow ((r2_funct_2 X0 X1 X2 \\ & X3) \Leftrightarrow (X2 = X3)) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\ & ((\neg v1_xboole_0 X1) \wedge ((\neg v1_xboole_0 X3) \wedge (((v1_funct_1 X4) \wedge (\\ & v1_funct_2 X4 X0 X1) \wedge (m1_subset_1 X4 (k1_zfmisc_1 (k2_zfmisc_1 \\ & X0 X1)))))) \wedge ((v1_funct_1 X5) \wedge ((v1_funct_2 X5 X2 X3) \wedge (m1_subset_1 \\ & X5 (k1_zfmisc_1 (k2_zfmisc_1 X2 X3)))))) \Rightarrow ((r1_funct_2 X0 X1 \\ & X2 X3 X4 X5) \Leftrightarrow (X4 = X5)) \end{aligned} \quad (8)$$

Assume the following.

$$k6_numbers = k1_xboole_0 \quad (9)$$

Assume the following.

$$k5_numbers = k4_ordinal1 \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v1_funct_1 X2)\wedge \\ & ((v1_funct_2 X2 k5_numbers (k3_rfunct_3 X0 X1))\wedge(m1_subset_1 \\ & X2 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k3_rfunct_3 X0 X1))))))\wedge \\ & (v7_ordinal1 X3))\Rightarrow(k4_mesfunc5 X0 X1 X2 X3 = k1_funct_1 X2 X3) \end{aligned} \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.k3_rfunct_3 X0 X1 = k4_partfun1 X0 X1 \quad (12)$$

Assume the following.

$$\forall X0.\forall X1.((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge(v3_valued_0 X0)))\Rightarrow(k1_seq_1 X0 X1 = k1_funct_1 X0 X1) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.((v1_relat_1 X0)\wedge((v1_funct_1 X0)\wedge(v2_valued_0 X0)))\Rightarrow(k1_mesfunc9 X0 X1 = k1_funct_1 X0 X1) \quad (14)$$

Assume the following.

$$(\neg v1_xboole_0 k4_ordinal1)\wedge(v3_ordinal1 k4_ordinal1) \quad (15)$$

Assume the following.

$$\neg v1_xboole_0 k7_numbers \quad (16)$$

Assume the following.

$$v3_membered k1_numbers \quad (17)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((v1_funct_1 X1)\wedge \\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers))\wedge((v1_mesfunc8 \\ & X1 X0 k1_numbers)\wedge(m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers \\ & (k4_partfun1 X0 k1_numbers))))))\Rightarrow((v1_funct_1 (k1_mesfun7c \\ & X0 X1))\wedge((v1_funct_2 (k1_mesfun7c X0 X1) k5_numbers (k4_partfun1 \\ & X0 k7_numbers))\wedge(v1_mesfunc8 (k1_mesfun7c X0 X1) X0 k7_numbers))) \end{aligned} \quad (18)$$

Assume the following.

$$\neg v1_xboole_0 \ k1_numbers \quad (19)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1_xboole_0 \ X0) \wedge ((v1_funct_1 \ X1) \wedge \\ & (v1_funct_2 \ X1 \ X0 \ k1_numbers) \wedge (m1_subset_1 \ X1 \ (k1_zfmisc_1 \ (k2_zfmisc_1 \\ & \ X0 \ k1_numbers)))))) \Rightarrow ((v1_funct_1 \ (k1_mesfunc5 \ X0 \ X1)) \wedge (v1_partfun1 \\ & \ (k1_mesfunc5 \ X0 \ X1) \ X0)) \end{aligned} \quad (20)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v1_xboole_0 \ X0) \wedge ((v1_funct_1 \ X1) \wedge (\\ & (v1_funct_2 \ X1 \ k5_numbers \ (k4_partfun1 \ X0 \ k7_numbers)) \wedge (m1_subset_1 \\ & \ X1 \ (k1_zfmisc_1 \ (k2_zfmisc_1 \ k5_numbers \ (k4_partfun1 \ X0 \ k7_numbers)))))) \Rightarrow \\ & \ ((v1_funct_1 \ (k4_mesfunc9 \ X0 \ X1)) \wedge ((v1_funct_2 \ (k4_mesfunc9 \\ & \ X0 \ X1) \ k5_numbers \ (k4_partfun1 \ X0 \ k7_numbers)) \wedge (m1_subset_1 \ (\\ & \ k4_mesfunc9 \ X0 \ X1) \ (k1_zfmisc_1 \ (k2_zfmisc_1 \ k5_numbers \ (k4_partfun1 \\ & \ X0 \ k7_numbers)))))) \end{aligned} \quad (21)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v1_funct_1 \ X0) \wedge ((v1_funct_2 \ X0 \ k5_numbers \ k1_numbers) \wedge \\ & (m1_subset_1 \ X0 \ (k1_zfmisc_1 \ (k2_zfmisc_1 \ k5_numbers \ k1_numbers)))))) \Rightarrow \\ & \ ((v1_funct_1 \ (k3_series_1 \ X0)) \wedge ((v1_funct_2 \ (k3_series_1 \ X0) \\ & \ k5_numbers \ k1_numbers) \wedge (m1_subset_1 \ (k3_series_1 \ X0) \ (k1_zfmisc_1 \\ & \ (k2_zfmisc_1 \ k5_numbers \ k1_numbers)))))) \end{aligned} \quad (22)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. ((\neg v1_xboole_0 \ X0) \wedge (((v1_funct_1 \\ & \ X1) \wedge ((v1_funct_2 \ X1 \ k5_numbers \ (k4_partfun1 \ X0 \ k7_numbers)) \wedge \\ & (m1_subset_1 \ X1 \ (k1_zfmisc_1 \ (k2_zfmisc_1 \ k5_numbers \ (k4_partfun1 \\ & \ X0 \ k7_numbers)))))) \wedge (m1_subset_1 \ X2 \ X0))) \Rightarrow ((v1_funct_1 \ (k3_mesfunc5 \\ & \ X0 \ X1 \ X2)) \wedge ((v1_funct_2 \ (k3_mesfunc5 \ X0 \ X1 \ X2) \ k5_numbers \ k7_numbers) \wedge \\ & (m1_subset_1 \ (k3_mesfunc5 \ X0 \ X1 \ X2) \ (k1_zfmisc_1 \ (k2_zfmisc_1 \\ & \ k5_numbers \ k7_numbers)))))) \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v1_relat_1 \ X0) \wedge ((v1_funct_1 \ X0) \wedge (v2_valued_0 \ X0))) \Rightarrow \\ & \ ((v1_funct_1 \ (k2_mesfunc9 \ X0)) \wedge ((v1_funct_2 \ (k2_mesfunc9 \ X0) \\ & \ k5_numbers \ k7_numbers) \wedge (m1_subset_1 \ (k2_mesfunc9 \ X0) \ (k1_zfmisc_1 \\ & \ (k2_zfmisc_1 \ k5_numbers \ k7_numbers)))))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((v1_funct_1 X1)\wedge \\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers))\wedge(m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers))))))\Rightarrow \\ & ((v1_funct_1 (k2_mesfun9c X0 X1))\wedge((v1_funct_2 (k2_mesfun9c \\ & X0 X1) k5_numbers (k4_partfun1 X0 k1_numbers))\wedge(m1_subset_1 (\\ & k2_mesfun9c X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 \\ & X0 k1_numbers)))))) \end{aligned} \quad (25)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((v1_funct_1 X1)\wedge(\\ & m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 X0 k1_numbers))))\Rightarrow \\ & ((v1_funct_1 (k1_mesfunc5 X0 X1))\wedge(m1_subset_1 (k1_mesfunc5 \\ & X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 X0 k7_numbers)))) \end{aligned} \quad (26)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1_xboole_0 X0)\wedge((v1_funct_1 X1)\wedge(\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers))\wedge(m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers))))))\Rightarrow \\ & ((v1_funct_1 (k1_mesfun7c X0 X1))\wedge((v1_funct_2 (k1_mesfun7c \\ & X0 X1) k5_numbers (k4_partfun1 X0 k7_numbers))\wedge(m1_subset_1 (\\ & k1_mesfun7c X0 X1) (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 \\ & X0 k7_numbers)))))) \end{aligned} \quad (27)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.((\neg v1_xboole_0 X0)\wedge(((v1_funct_1 \\ & X1)\wedge((v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers))\wedge \\ & (m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 \\ & X0 k1_numbers))))))\wedge(m1_subset_1 X2 X0))\Rightarrow((v1_funct_1 (k10_seqfunc \\ & X0 X1 X2))\wedge((v1_funct_2 (k10_seqfunc X0 X1 X2) k5_numbers k1_numbers)\wedge \\ & (m1_subset_1 (k10_seqfunc X0 X1 X2) (k1_zfmisc_1 (k2_zfmisc_1 \\ & k5_numbers k1_numbers)))))) \end{aligned} \quad (28)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1_xboole_0 X0)\Rightarrow(\forall X1.((v1_funct_1 X1)\wedge(\\ & m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 X0 k1_numbers))))\Rightarrow(\\ & k1_mesfunc5 X0 X1 = X1)) \end{aligned} \quad (29)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1_xboole_0 X0)\Rightarrow(\forall X1.((v1_funct_1 X1)\wedge(\\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers))\wedge(m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers))))))\Rightarrow \\ & (k1_mesfun7c X0 X1 = X1)) \end{aligned} \quad (30)$$

Assume the following.

$$\forall X0.(m1_subset_1 X0 k4_ordinal1) \Rightarrow (v7_ordinal1 X0) \quad (31)$$

Assume the following.

$$\forall X0.(v3_membered X0) \Rightarrow (v2_membered X0) \quad (32)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \Rightarrow (v1_relat_1 X2) \quad (33)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \Rightarrow ((v1_partfun1 X2 X0) \Rightarrow (v1_funct_2 X2 X0 X1)) \quad (34)$$

Assume the following.

$$\forall X0.\forall X1.(v3_membered X1) \Rightarrow (\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \Rightarrow (v3_valued_0 X2)) \quad (35)$$

Assume the following.

$$\forall X0.\forall X1.(v2_membered X1) \Rightarrow (\forall X2.(m1_subset_1 X2 (k1_zfmisc_1 (k2_zfmisc_1 X0 X1))) \Rightarrow (v2_valued_0 X2)) \quad (36)$$

Theorem 1

$$\begin{aligned} & \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.((v1_funct_1 X1) \wedge \\ & (v1_funct_2 X1 k5_numbers (k4_partfun1 X0 k1_numbers)) \wedge (m1_subset_1 \\ & X1 (k1_zfmisc_1 (k2_zfmisc_1 k5_numbers (k4_partfun1 X0 k1_numbers)))))) \Rightarrow \\ & (\forall X2.(v7_ordinal1 X2) \Rightarrow (\forall X3.(m1_subset_1 X3 X0) \Rightarrow \\ & (\forall X4.((v1_mesfunc8 X1 X0 k1_numbers) \wedge ((r1_tarski X4 (k1_relset_1 \\ & X0 (k4_mesfunc5 X0 k1_numbers X1 k6_numbers))) \wedge (X3 \in X4))) \Rightarrow (k1_seq_1 \\ & (k3_series_1 (k10_seqfunc X0 X1 X3)) X2 = k1_seq_1 (k10_seqfunc \\ & X0 (k2_mesfun9c X0 X1) X3) X2)))))) \end{aligned}$$