

t12\_parsp\_1  
(TMQ9H4e6j9tdpguvSi6GwCx9xeToymWCLSW)

October 27, 2020

Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v6\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v33\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v5\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k9\_parsp\_1 : \iota \Rightarrow \iota$  be given. Let  $r1\_parsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_group\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_mcart\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_mcart\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_mcart\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given.

given. Let  $k6\_parsp\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v6\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\
& X0) \wedge ((v33\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ( \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 \\
& X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow (\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X2.( \\
& m1\_subset\_1 X2 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X3.(m1\_subset\_1 \\
& X3 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow ((r1\_parsp\_1 (k9\_parsp\_1 X0) \\
& X1 X2 X3 X4) \Leftrightarrow ((k5\_domain\_1 (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 \\
& (k9\_parsp\_1 X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 ( \\
& k9\_parsp\_1 X0)) X1 X2 X3 X4 \in k6\_parsp\_1 X0) \wedge (\exists X5.(m1\_subset\_1 \\
& X5 (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0))) \wedge (\exists X6.(m1\_subset\_1 X6 (k3\_zfmisc\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0))) \wedge (\exists X7.(m1\_subset\_1 \\
& X7 (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0))) \wedge (\exists X8.(m1\_subset\_1 X8 (k3\_zfmisc\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0))) \wedge ((k5\_domain\_1 (u1\_struct\_0 \\
& (k9\_parsp\_1 X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 ( \\
& k9\_parsp\_1 X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) X1 X2 X3 X4 = k5\_domain\_1 \\
& (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& X5 X6 X7 X8) \wedge ((k5\_algstr\_0 X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k1\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 \\
& X0 (k2\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X7) (k2\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X8))) (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k1\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k2\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k2\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 \\
& X0) \wedge ((k5\_algstr\_0 X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k1\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 \\
& X0 (k3\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X7) (k3\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X8))) (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k1\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k3\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k3\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 \\
& X0) \wedge (k5\_algstr\_0 X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k2\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k2\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 \\
& X0 (k3\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X7) (k3\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X0) X8))) (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k2\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k2\_mcart\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k3\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k3\_mcart\_1 \\
& (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 \\
& X0))))))))))))))
\end{aligned}$$

(1)

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v6\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\
& X0) \wedge ((v33\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ( \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 \\
& X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow (\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X2.( \\
& m1\_subset\_1 X2 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X3.(m1\_subset\_1 \\
& X3 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X4.(m1\_subset\_1 X4 \\
& (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (k5\_domain\_1 (u1\_struct\_0 (k9\_parsp\_1 \\
& X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) \\
& (u1\_struct\_0 (k9\_parsp\_1 X0)) X1 X2 X3 X4 \in k6\_parsp\_1 X0))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v6\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\
& X0) \wedge ((v33\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ( \\
& (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 \\
& X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow (u1\_struct\_0 \\
& (k9\_parsp\_1 X0) = k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) \\
& (u1\_struct\_0 X0))
\end{aligned} \tag{3}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v6\_struct\_0 X0) \wedge ((v13\_algstr\_0 \\ & X0) \wedge ((v33\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v5\_group\_1 X0) \wedge ( \\ & (v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 \\ & X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow (\forall X1. \\ & (m1\_subset\_1 X1 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X2. ( \\ & m1\_subset\_1 X2 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X3. (m1\_subset\_1 \\ & X3 (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow (\forall X4. (m1\_subset\_1 X4 \\ & (u1\_struct\_0 (k9\_parsp\_1 X0))) \Rightarrow ((r1\_parsp\_1 (k9\_parsp\_1 X0) \\ & X1 X2 X3 X4) \Leftrightarrow (\exists X5. (m1\_subset\_1 X5 (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0))) \wedge (\exists X6. (m1\_subset\_1 \\ & X6 (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0))) \wedge (\exists X7. (m1\_subset\_1 X7 (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0))) \wedge (\exists X8. (m1\_subset\_1 \\ & X8 (k3\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0))) \wedge ((k5\_domain\_1 (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 \\ & (k9\_parsp\_1 X0)) (u1\_struct\_0 (k9\_parsp\_1 X0)) (u1\_struct\_0 ( \\ & k9\_parsp\_1 X0)) X1 X2 X3 X4 = k5\_domain\_1 (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) (k3\_zfmisc\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0)) X5 X6 X7 X8) \wedge ((k5\_algstr\_0 \\ & X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 X0) \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k1\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 X0 (k2\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k2\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8))) (k8\_group\_1 \\ & X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) \\ & (u1\_struct\_0 X0) X7) (k1\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k2\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k2\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 X0) \wedge ( \\ & (k5\_algstr\_0 X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k1\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 X0 (k3\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k3\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8))) (k8\_group\_1 \\ & X0 (k5\_algstr\_0 X0 (k1\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) \\ & (u1\_struct\_0 X0) X7) (k1\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k3\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k3\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 X0) \wedge ( \\ & k5\_algstr\_0 X0 (k8\_group\_1 X0 (k5\_algstr\_0 X0 (k2\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k2\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6)) (k5\_algstr\_0 X0 (k3\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X7) (k3\_mcart\_1 \\ & (u1\_struct\_0 X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X8))) (k8\_group\_1 \\ & X0 (k5\_algstr\_0 X0 (k2\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) \\ & (u1\_struct\_0 X0) X7) (k2\_mcart\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) X8)) (k5\_algstr\_0 X0 (k3\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X5) (k3\_mcart\_1 (u1\_struct\_0 \\ & X0) (u1\_struct\_0 X0) (u1\_struct\_0 X0) X6))) = k4\_struct\_0 X0))))))))) \end{aligned}$$