

t12\_rfunct\_1  
(TMP9vM3V8gDK7ad7iw7j2k8EfSouFRmxAq1)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xcmplx\_0 : \iota \Rightarrow o$  be given. Let  $k24\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k18\_valued\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_xcmplx\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_valued\_0 X0))) \Rightarrow \\ (\forall X1.((v1\_relat\_1 X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_valued\_0 \\ X1))) \Rightarrow (\forall X2.k1\_funct\_1 (k18\_valued\_1 X0 X1) X2 = k3\_xcmplx\_0 \\ (k1\_funct\_1 X0 X2) (k1\_funct\_1 X1 X2))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.((v1\_xcmplx\_0 X0) \wedge ((v1\_xcmplx\_0 \\ X1) \wedge (v1\_xcmplx\_0 X2))) \Rightarrow (k3\_xcmplx\_0 (k3\_xcmplx\_0 X0 X1) X2 = k3\_xcmplx\_0 \\ X0 (k3\_xcmplx\_0 X1 X2)) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_valued\_0 X0))) \Rightarrow (v1\_xcmplx\_0 (k1\_funct\_1 X0 X1)) \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_valued\_0 \\ X0))) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow (((v1\_relat\_1 (k24\_valued\_1 X0 X1)) \wedge \\ ((v1\_funct\_1 (k24\_valued\_1 X0 X1)) \wedge (v1\_valued\_0 (k24\_valued\_1 \\ X0 X1)))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xcmplx\_0 X0) \wedge (v1\_xcmplx\_0 X1)) \Rightarrow (v1\_xcmplx\_0 (k3\_xcmplx\_0 X0 X1)) \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 \\ X0)))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v1\_valued\_0 X1))))\Rightarrow \\ ((v1\_relat\_1 (k18\_valued\_1 X0 X1))\wedge((v1\_funct\_1 (k18\_valued\_1 \\ X0 X1))\wedge(v1\_valued\_0 (k18\_valued\_1 X0 X1)))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 \\ X0)))\wedge(v1\_xcmplx\_0 X1))\Rightarrow((v1\_relat\_1 (k24\_valued\_1 X0 X1))\wedge \\ (v1\_funct\_1 (k24\_valued\_1 X0 X1))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 X0)))\Rightarrow \\ (\forall X1.(v1\_xcmplx\_0 X1)\Rightarrow(\forall X2.((v1\_relat\_1 X2)\wedge \\ v1\_funct\_1 X2))\Rightarrow((X2 = k24\_valued\_1 X0 X1)\Leftrightarrow((k9\_xtuple\_0 X2 = k9\_xtuple\_0 \\ X0)\wedge(\forall X3.(X3 \in k9\_xtuple\_0 X2)\Rightarrow(k1\_funct\_1 X2 X3 = k3\_xcmplx\_0 \\ X1 (k1\_funct\_1 X0 X3)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(X2 = k3\_xboole\_0 X0 X1)\Leftrightarrow(\forall X3. \\ (X3 \in X2)\Leftrightarrow((X3 \in X0)\wedge(X3 \in X1))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 X0)))\Rightarrow \\ (\forall X1.((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v1\_valued\_0 \\ X1)))\Rightarrow(\forall X2.((v1\_relat\_1 X2)\wedge(v1\_funct\_1 X2))\Rightarrow((X2 = k18\_valued\_1 \\ X0 X1)\Leftrightarrow((k9\_xtuple\_0 X2 = k3\_xboole\_0 (k9\_xtuple\_0 X0) (k9\_xtuple\_0 \\ X1))\wedge(\forall X3.(X3 \in k9\_xtuple\_0 X2)\Rightarrow(k1\_funct\_1 X2 X3 = k3\_xcmplx\_0 \\ (k1\_funct\_1 X0 X3) (k1\_funct\_1 X1 X3)))))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xcmplx\_0 X0)\wedge(v1\_xcmplx\_0 X1))\Rightarrow( \\ k3\_xcmplx\_0 X0 X1 = k3\_xcmplx\_0 X1 X0) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 \\ X0)))\wedge((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v1\_valued\_0 X1))))\Rightarrow \\ (k18\_valued\_1 X0 X1 = k18\_valued\_1 X1 X0) \end{aligned} \quad (12)$$

**Theorem 1**

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0)\wedge((v1\_funct\_1 X0)\wedge(v1\_valued\_0 X0)))\Rightarrow \\ (\forall X1.((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v1\_valued\_0 \\ X1)))\Rightarrow(\forall X2.(v1\_xcmplx\_0 X2)\Rightarrow(k24\_valued\_1 (k18\_valued\_1 \\ X0 X1) X2 = k18\_valued\_1 (k24\_valued\_1 X0 X2) X1))) \end{aligned}$$