

t138_member_1
(TMbi6hMnhmq9vzSu8PqmmhP2zPhLPJ1Vrgp)

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Let $v2_membered : \iota \Rightarrow o$ be given. Let $v1_xreal_0 : \iota \Rightarrow o$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k6_subset_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k16_member_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k4_xboole_0 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_tarski : \iota \Rightarrow \iota$ be given. Let $k8_member_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k7_numbers : \iota$ be given. Let $k1_xreal_3 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0. \forall X1. (m1_subset_1 X0 (k1_zfmisc_1 X1)) \Leftrightarrow (r1_tarski X0 X1) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. k6_subset_1 X0 X1 = k4_xboole_0 X0 X1 \quad (2)$$

Assume the following.

$$\forall X0. (v1_xreal_0 X0) \Rightarrow (v2_membered (k1_tarski X0)) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. ((v2_membered X0) \wedge (v1_xreal_0 X1)) \Rightarrow (v2_membered (k16_member_1 X0 X1)) \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. (v2_membered X0) \Rightarrow (v2_membered (k4_xboole_0 X0 X1)) \quad (5)$$

Assume the following.

$$\forall X0. \forall X1. m1_subset_1 (k6_subset_1 X0 X1) (k1_zfmisc_1 X0) \quad (6)$$

Assume the following.

$$\forall X0. (v2_membered X0) \Rightarrow (\forall X1. (r1_tarski X0 X1) \Leftrightarrow (\forall X2. (v1_xreal_0 X2) \Rightarrow ((X2 \in X0) \Rightarrow (X2 \in X1)))) \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(X2 = k4_xboole_0 X0 X1) \Leftrightarrow (\forall X3. \\ (X3 \in X2) \Leftrightarrow ((X3 \in X0) \wedge (\neg X3 \in X1))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.(v2_membered X0) \Rightarrow (\forall X1.(v2_membered X1) \Rightarrow (k8_member_1 \\ X0 X1 = ReplSep2 (toset (\lambda X2 : \iota.m1_subset_1 X2 k7_numbers)) \\ (\lambda X2 : \iota.toset (\lambda X3 : \iota.m1_subset_1 X3 k7_numbers)) (\\ \lambda X2 : \iota.\lambda X3 : \iota.(X2 \in X0) \wedge (X3 \in X1)) (\lambda X2 : \iota.\lambda X3 : \\ \iota.k1_xxreal_3 X2 X3))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.(v2_membered X0) \Rightarrow (\forall X1.(v1_xxreal_0 X1) \Rightarrow (k16_member_1 \\ X0 X1 = k8_member_1 (k1_tarski X1) X0)) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v2_membered X0) \wedge (v2_membered X1)) \Rightarrow (\\ k8_member_1 X0 X1 = k8_member_1 X1 X0) \end{aligned} \quad (11)$$

Theorem 1

$$\begin{aligned} \forall X0.(v2_membered X0) \Rightarrow (\forall X1.(v2_membered X1) \Rightarrow (\forall X2. \\ (v1_xxreal_0 X2) \Rightarrow (r1_tarski (k6_subset_1 (k16_member_1 X0 X2) \\ (k16_member_1 X1 X2)) (k16_member_1 (k6_subset_1 X0 X1) X2)))) \end{aligned}$$