

# t13\_circuit1

(TMT5uP9zLHtcWzEReAi44LXg8R395XXxh46)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_msafree2 : \iota \Rightarrow o$  be given. Let  $v5\_msafree2 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_msafree2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_msafree2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_msafree2 : \iota \Rightarrow \iota$  be given. Let  $k1\_msafree2 : \iota \Rightarrow \iota$  be given. Let  $k5\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k4\_circuit1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finseq\_1 : \iota \Rightarrow o$  be given. Let  $v6\_trees\_3 : \iota \Rightarrow o$  be given. Let  $k4\_trees\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_msafree2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $v3\_trees\_2 : \iota \Rightarrow o$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k11\_trees\_3 : \iota \Rightarrow \iota$  be given. Let  $k2\_funct\_6 : \iota \Rightarrow \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_finseq\_1 : \iota \Rightarrow \iota$  be given. Let  $k5\_trees\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_msafree2 \\ & X0) \wedge ((v5\_msafree2 X0) \wedge (l1\_msualg\_1 X0)))))) \Rightarrow (\forall X1.((v4\_msualg\_1 \\ & X1 X0) \wedge ((v4\_msafree2 X1 X0) \wedge (l3\_msualg\_1 X1 X0))) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\ & (k1\_funct\_1 (u3\_msualg\_1 X0 (k5\_msafree2 X0 X1)) X2)) \Rightarrow (\neg (X2 \in k7\_subset\_1 \\ & (u1\_struct\_0 X0) (k3\_msafree2 X0) (k1\_msafree2 X0)) \wedge ((k5\_card\_1 \\ & X3 = k4\_circuit1 X0 X1 X2) \wedge (\forall X4.((v1\_relat\_1 X4) \wedge ((v1\_funct\_1 \\ & X4) \wedge ((v1\_finseq\_1 X4) \wedge (v6\_trees\_3 X4)))))) \Rightarrow (X3 \neq k4\_trees\_4 (k4\_tarski \\ & (k4\_msafree2 X0 X2) (u1\_struct\_0 X0) X4)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0.\forall X1.(((\neg v2\_struct\_0 X0)\wedge(\neg v11\_struct\_0 X0)\wedge((v2\_msafree2 X0)\wedge(l1\_msualg\_1 X0))))\wedge(m1\_subset\_1 X1 (u1\_struct\_0 X0))\Rightarrow(m1\_subset\_1 (k4\_msafree2 X0 X1) (u4\_struct\_0 X0)) \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.k4\_tarski X0 X1 = k2\_tarski (k2\_tarski X0 X1) (k1\_tarski X0) \quad (3)$$

Assume the following.

$$\begin{aligned} &\forall X0.\forall X1.((v1\_relat\_1 X1)\wedge((v1\_funct\_1 X1)\wedge(v1\_finseq\_1 X1)))\Rightarrow((v6\_trees\_3 X1)\Rightarrow(\forall X2.((v1\_relat\_1 X2)\wedge((v1\_funct\_1 X2)\wedge(v3\_trees\_2 X2))))\Rightarrow((X2 = k4\_trees\_4 X0 X1)\Leftrightarrow((\exists X3.((v1\_relat\_1 X3)\wedge((v1\_funct\_1 X3)\wedge(v1\_finseq\_1 X3)\wedge(v6\_trees\_3 X3))))\wedge((X1 = X3)\wedge(k9\_xtuple\_0 X2 = k11\_trees\_3 (k2\_funct\_6 X3))))\wedge \\ &((k1\_funct\_1 X2 k1\_xboole\_0 = X0)\wedge(\forall X3.(m1\_subset\_1 X3 k5\_numbers)\Rightarrow((\neg r1\_xreal\_0 (k3\_finseq\_1 X1) X3)\Rightarrow(k5\_trees\_2 X2 (k12\_finseq\_1 k5\_numbers X3) = k1\_funct\_1 X1 (k2\_nat\_1 X3 np\_1)))))))) \quad (4) \end{aligned}$$

Assume the following.

$$\forall X0.\forall X1.k2\_tarski X0 X1 = k2\_tarski X1 X0 \quad (5)$$

Assume the following.

$$\begin{aligned} &\forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge(\neg v11\_struct\_0 X0)\wedge((v2\_msafree2 X0)\wedge((v5\_msafree2 X0)\wedge(l1\_msualg\_1 X0))))\wedge \\ &(((v4\_msualg\_1 X1 X0)\wedge((v4\_msafree2 X1 X0)\wedge(l3\_msualg\_1 X1 X0)))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 X0))))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (k1\_funct\_1 (u3\_msualg\_1 X0 (k5\_msafree2 X0 X1)) X2))\Rightarrow(v3\_trees\_2 X3)) \quad (6) \end{aligned}$$

Assume the following.

$$\begin{aligned} &\forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X0)\wedge(\neg v11\_struct\_0 X0)\wedge((v2\_msafree2 X0)\wedge((v5\_msafree2 X0)\wedge(l1\_msualg\_1 X0))))\wedge \\ &(((v4\_msualg\_1 X1 X0)\wedge((v4\_msafree2 X1 X0)\wedge(l3\_msualg\_1 X1 X0)))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 X0))))\Rightarrow(\forall X3.(m1\_subset\_1 X3 (k1\_funct\_1 (u3\_msualg\_1 X0 (k5\_msafree2 X0 X1)) X2))\Rightarrow((v1\_relat\_1 X3)\wedge((v1\_funct\_1 X3)\wedge(\neg v1\_xboole\_0 X3)\wedge(v1\_finset\_1 X3)))) \quad (7) \end{aligned}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge (v2\_msafree2 \\ & X0) \wedge ((v5\_msafree2 X0) \wedge (l1\_msualg\_1 X0)))) \Rightarrow (\forall X1.((v4\_msualg\_1 \\ & X1 X0) \wedge ((v4\_msafree2 X1 X0) \wedge (l3\_msualg\_1 X1 X0))) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\ & (k1\_funct\_1 (u3\_msualg\_1 X0 (k5\_msafree2 X0 X1)) X2)) \Rightarrow (\neg (X2 \in k7\_subset\_1 \\ & (u1\_struct\_0 X0) (k3\_msafree2 X0) (k1\_msafree2 X0)) \wedge ((k5\_card\_1 \\ & X3 = k4\_circuit1 X0 X1 X2) \wedge (\forall X4.(m1\_subset\_1 X4 (u4\_struct\_0 \\ & X0)) \Rightarrow (k1\_funct\_1 X3 k1\_xboole\_0 \neq k4\_tarski X4 (u1\_struct\_0 X0)))))))))) \end{aligned}$$