

t13\_connsp\_1  
(TMGcWRYuy4jJhG6fnQZJCYKex5YeDKSve2Z)

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Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $v1\_connsp\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v3\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $k4\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $r1\_connsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_pre\_topc : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. r1\_xboole\_0 (k4\_xboole\_0 X0 X1) X1 \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0. (l1\_struct\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0))) \Rightarrow (((k2\_struct\_0 X0 = k4\_subset\_1 (u1\_struct\_0 \\ X0) X1 X2) \wedge (r1\_xboole\_0 X1 X2)) \Rightarrow (X2 = k7\_subset\_1 (u1\_struct\_0 \\ X0) (k2\_struct\_0 X0) X1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0. (l1\_struct\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (u1\_struct\_0 X0))) \Rightarrow ((\neg (X1 \neq k2\_struct\_0 X0) \wedge (k7\_subset\_1 (u1\_struct\_0 \\ X0) (k2\_struct\_0 X0) X1 = k1\_xboole\_0)) \wedge (\neg (k7\_subset\_1 (u1\_struct\_0 \\ X0) (k2\_struct\_0 X0) X1 \neq k1\_xboole\_0) \wedge (X1 = k2\_struct\_0 X0)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0. ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc X0)) \Rightarrow (\forall X1. \\ (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X2. \\ (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (((k2\_struct\_0 \\ X0 = k4\_subset\_1 (u1\_struct\_0 X0) X1 X2) \wedge (r1\_connsp\_1 X0 X1 X2)) \Rightarrow \\ ((v3\_pre\_topc X1 X0) \wedge ((v4\_pre\_topc X1 X0) \wedge ((v3\_pre\_topc X2 X0) \wedge \\ (v4\_pre\_topc X2 X0))))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0.(l1\_pre\_topc\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow (((v3\_pre\_topc\ X1\ X0) \Rightarrow (k2\_pre\_topc\ X0\ (k7\_subset\_1 \\ (u1\_struct\_0\ X0)\ (k2\_struct\_0\ X0)\ X1) = k7\_subset\_1\ (u1\_struct\_0 \\ X0)\ (k2\_struct\_0\ X0)\ X1)) \wedge (((v2\_pre\_topc\ X0) \wedge (k2\_pre\_topc\ X0 \\ (k7\_subset\_1\ (u1\_struct\_0\ X0)\ (k2\_struct\_0\ X0)\ X1) = k7\_subset\_1 \\ (u1\_struct\_0\ X0)\ (k2\_struct\_0\ X0)\ X1)) \Rightarrow (v3\_pre\_topc\ X1\ X0)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.(l1\_pre\_topc\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow (((v4\_pre\_topc\ X1\ X0) \Rightarrow (k2\_pre\_topc\ X0\ X1 = \\ X1)) \wedge (((v2\_pre\_topc\ X0) \wedge (k2\_pre\_topc\ X0\ X1 = X1)) \Rightarrow (v4\_pre\_topc \\ X1\ X0)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.(l1\_pre\_topc\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow (\forall X2.(m1\_subset\_1\ X2\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \Rightarrow ((r1\_connsp\_1\ X0\ X1\ X2) \Rightarrow (r1\_xboole\_0\ X1\ X2)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.((v2\_pre\_topc\ X0) \wedge (l1\_pre\_topc\ X0)) \Rightarrow ((v1\_connsp\_1 \\ X0) \Leftrightarrow (\forall X1.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1\ (u1\_struct\_0\ X0))) \Rightarrow \\ (\neg(X1 \neq k1\_struct\_0\ X0) \wedge ((X1 \neq k2\_struct\_0\ X0) \wedge (r1\_xboole\_0\ (k2\_pre\_topc \\ X0\ X1)\ (k2\_pre\_topc\ X0\ (k7\_subset\_1\ (u1\_struct\_0\ X0)\ (k2\_struct\_0 \\ X0)\ X1))))))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.\forall X1.(r1\_xboole\_0\ X0\ X1) \Rightarrow (r1\_xboole\_0\ X1\ X0) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1\ X1\ (k1\_zfmisc\_1 \\ X0)) \Rightarrow (k7\_subset\_1\ X0\ X1\ X2 = k4\_xboole\_0\ X1\ X2) \quad (10)$$

Assume the following.

$$\forall X0.(l1\_pre\_topc\ X0) \Rightarrow (l1\_struct\_0\ X0) \quad (11)$$

Assume the following.

$$\forall X0.(l1\_struct\_0\ X0) \Rightarrow (m1\_subset\_1\ (k2\_struct\_0\ X0)\ (k1\_zfmisc\_1 \\ (u1\_struct\_0\ X0))) \quad (12)$$

Assume the following.

$$\forall X0.(l1\_struct\_0\ X0) \Rightarrow (k2\_struct\_0\ X0 = u1\_struct\_0\ X0) \quad (13)$$

Assume the following.

$$\forall X0.(l1\_struct\_0 X0) \Rightarrow (k1\_struct\_0 X0 = k1\_xboole\_0) \quad (14)$$

Assume the following.

$$\begin{aligned} \forall X0.(l1\_pre\_topc X0) \Rightarrow & ((v1\_connsp\_1 X0) \Leftrightarrow (\forall X1.( \\ & m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\forall X2.( \\ & m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow (\neg(k2\_struct\_0 \\ & X0 = k4\_subset\_1 (u1\_struct\_0 X0) X1 X2) \wedge ((r1\_connsp\_1 X0 X1 X2) \wedge \\ & ((X1 \neq k1\_struct\_0 X0) \wedge (X2 \neq k1\_struct\_0 X0))))))) \end{aligned} \quad (15)$$

**Theorem 1**

$$\begin{aligned} \forall X0.((v2\_pre\_topc X0) \wedge (l1\_pre\_topc X0)) \Rightarrow & ((v1\_connsp\_1 \\ & X0) \Leftrightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\ & (\neg(v3\_pre\_topc X1 X0) \wedge ((v4\_pre\_topc X1 X0) \wedge ((X1 \neq k1\_struct\_0 \\ & X0) \wedge (X1 \neq k2\_struct\_0 X0)))))) \end{aligned}$$