

t13\_osalg\_4 (TM-  
 SJQ7WCMNjEhhY1ffV4u2SZgzhSvBCCQ11)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v4\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $v5\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $v2\_osalg\_4 : \iota \Rightarrow o$  be given. Let  $l3\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v12\_osalg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_msualg\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_osalg\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r3\_orders\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_osalg\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v4\_orders\_2 : \iota \Rightarrow o$  be given. Let  $v5\_orders\_2 : \iota \Rightarrow o$  be given. Let  $l1\_orders\_2 : \iota \Rightarrow o$  be given. Let  $k3\_osalg\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $l2\_osalg\_1 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $k6\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_osalg\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_osalg\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v3\_orders\_2 X0) \wedge ((v4\_orders\_2 \\ & X0) \wedge ((v5\_orders\_2 X0) \wedge (l1\_orders\_2 X0)))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 \\ & X0)) \Rightarrow ((r3\_orders\_2 X0 X1 X2) \Rightarrow (k3\_osalg\_4 X0 X1 = k3\_osalg\_4 X0 X2)))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0.(l3\_osalg\_1 X0) \Rightarrow ((l1\_osalg\_1 X0) \wedge (l2\_osalg\_1 X0)) \quad (2)$$

Assume the following.

$$\forall X0.(l2\_osalg\_1 X0) \Rightarrow ((l1\_msualg\_1 X0) \wedge (l1\_orders\_2 X0)) \quad (3)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v4\_osalg\_1 \\
& X0) \wedge ((v5\_osalg\_1 X0) \wedge ((v2\_osalg\_4 X0) \wedge (l3\_osalg\_1 X0)))))) \Rightarrow \\
& (\forall X1.((v4\_msualg\_1 X1 X0) \wedge ((v12\_osalg\_1 X1 X0) \wedge (l3\_msualg\_1 \\
& X1 X0)))) \Rightarrow (\forall X2.((v2\_msualg\_4 X2 X0 X1) \wedge (m1\_osalg\_4 X2 X0 \\
& X1)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4. \\
& (m1\_subset\_1 X4 (k1\_funct\_1 (u3\_msualg\_1 X0 X1) X3)) \Rightarrow (k8\_osalg\_4 \\
& X0 X1 X2 X3 X4 = k6\_eqrel\_1 (k4\_osalg\_4 X0 (u3\_msualg\_1 X0 X1) (k3\_osalg\_4 \\
& X0 X3)) (k4\_osalg\_4 X0 (u3\_msualg\_1 X0 X1) (k3\_osalg\_4 X0 X3)) (k5\_osalg\_4 \\
& X0 X1 X2 (k3\_osalg\_4 X0 X3)) X4))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\forall X0.(l3\_osalg\_1 X0) \Rightarrow ((v4\_osalg\_1 X0) \Rightarrow ((v3\_orders\_2 X0) \wedge ((v4\_orders\_2 X0) \wedge (v5\_orders\_2 X0)))) \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v4\_osalg\_1 \\
& X0) \wedge ((v5\_osalg\_1 X0) \wedge ((v2\_osalg\_4 X0) \wedge (l3\_osalg\_1 X0)))))) \Rightarrow \\
& (\forall X1.((v4\_msualg\_1 X1 X0) \wedge ((v12\_osalg\_1 X1 X0) \wedge (l3\_msualg\_1 \\
& X1 X0)))) \Rightarrow (\forall X2.((v2\_msualg\_4 X2 X0 X1) \wedge (m1\_osalg\_4 X2 X0 \\
& X1)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow (\forall X4. \\
& (m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow (\forall X5.(m1\_subset\_1 X5 \\
& (k1\_funct\_1 (u3\_msualg\_1 X0 X1) X3)) \Rightarrow ((r3\_orders\_2 X0 X3 X4) \Rightarrow ( \\
& \forall X6.(m1\_subset\_1 X6 (k1\_funct\_1 (u3\_msualg\_1 X0 X1) X4)) \Rightarrow \\
& ((X6 = X5) \Rightarrow (k8\_osalg\_4 X0 X1 X2 X3 X5 = k8\_osalg\_4 X0 X1 X2 X4 X6))))))))))
\end{aligned}$$