

## t13\_trees\_9

(TMQvJCmRe2WFEyHUNojSFkjRiRy9V35HVBp)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v3\_trees\_2 : \iota \Rightarrow o$  be given. Let  $m1\_trees\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_trees\_9 : \iota \Rightarrow \iota$  be given. Let  $k5\_trees\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k8\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_trees\_1 : \iota \Rightarrow o$  be given. Let  $k7\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k4\_trees\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 X0))) \Rightarrow \\ (\forall X1.(m2\_finseq\_1 X1 k5\_numbers) \Rightarrow (\forall X2.(m2\_finseq\_1 \\ X2 k5\_numbers) \Rightarrow ((k8\_finseq\_1 k5\_numbers X1 X2 \in k9\_xtuple\_0 X0) \Rightarrow \\ (k5\_trees\_2 X0 (k8\_finseq\_1 k5\_numbers X1 X2) = k5\_trees\_2 (k5\_trees\_2 \\ X0 X1) X2)))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. (m2\_finseq\_1 X1 X0) \Leftrightarrow (m1\_finseq\_1 X1 X0) \tag{4}$$

Assume the following.

$$\forall X0. ((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. (m1\_trees\_1 X1 X0) \Leftrightarrow (m1\_subset\_1 X1 X0)) \tag{5}$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((m1\_finseq\_1 X1 X0) \wedge (m1\_finseq\_1 X2 X0)) \Rightarrow (k8\_finseq\_1 X0 X1 X2 = k7\_finseq\_1 X1 X2) \tag{6}$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 X0))) \Rightarrow \\ ((\neg v1\_xboole\_0 (k9\_xtuple\_0 X0)) \wedge (v1\_trees\_1 (k9\_xtuple\_0 X0))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. \\ (m1\_trees\_1 X1 X0) \Rightarrow (m2\_finseq\_1 X1 k5\_numbers)) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. (((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 \\ X0))) \wedge (m1\_finseq\_1 X1 k5\_numbers)) \Rightarrow ((v1\_relat\_1 (k5\_trees\_2 \\ X0 X1)) \wedge ((v1\_funct\_1 (k5\_trees\_2 X0 X1)) \wedge (v3\_trees\_2 (k5\_trees\_2 \\ X0 X1)))) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 X0))) \Rightarrow \\ (k3\_trees\_9 X0 = ReplSep (toset (\lambda X1 : \iota. m1\_trees\_1 X1 (k9\_xtuple\_0 \\ X0))) (\lambda X1 : \iota. True) (\lambda X1 : \iota. k5\_trees\_2 X0 X1))) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v1\_xboole\_0 X0) \wedge (v1\_trees\_1 X0)) \Rightarrow (\forall X1. \\ (m2\_finseq\_1 X1 k5\_numbers) \Rightarrow ((X1 \in X0) \Rightarrow (\forall X2. ((\neg v1\_xboole\_0 \\ X2) \wedge (v1\_trees\_1 X2)) \Rightarrow ((X2 = k4\_trees\_1 X0 X1) \Leftrightarrow (\forall X3. (m2\_finseq\_1 \\ X3 k5\_numbers) \Rightarrow ((X3 \in X2) \Leftrightarrow (k8\_finseq\_1 k5\_numbers X1 X3 \in X0))))))) \end{aligned} \quad (12)$$

Assume the following.

$$\forall X0. \forall X1. (r1\_tarski X0 X1) \Leftrightarrow (\forall X2. (X2 \in X0) \Rightarrow (X2 \in X1)) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 X0))) \Rightarrow \\ (\forall X1. (m2\_finseq\_1 X1 k5\_numbers) \Rightarrow (\forall X2. ((v1\_relat\_1 \\ X2) \wedge ((v1\_funct\_1 X2) \wedge (v3\_trees\_2 X2))) \Rightarrow ((X2 = k5\_trees\_2 X0 X1) \Leftrightarrow \\ ((k9\_xtuple\_0 X2 = k4\_trees\_1 (k9\_xtuple\_0 X0) X1) \wedge (\forall X3. \\ (m2\_finseq\_1 X3 k5\_numbers) \Rightarrow ((X3 \in k4\_trees\_1 (k9\_xtuple\_0 X0) \\ X1) \Rightarrow (k1\_funct\_1 X2 X3 = k1\_funct\_1 X0 (k8\_finseq\_1 k5\_numbers X1 \\ X3)))))))))) \end{aligned} \quad (14)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v3\_trees\_2 X0))) \Rightarrow \\ & (\forall X1.(m1\_trees\_1 X1 (k9\_xtuple\_0 X0)) \Rightarrow (r1\_tarSKI (k3\_trees\_9 \\ & (k5\_trees\_2 X0 X1)) (k3\_trees\_9 X0))) \end{aligned}$$