

t140_zmodul01 (TMZzM-
SCK8EVi1G39x5GdNVT4J5PjgqQnE7M)

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Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v13_algstr_0 : \iota \Rightarrow o$ be given. Let $v2_rlvect_1 : \iota \Rightarrow o$ be given. Let $v3_rlvect_1 : \iota \Rightarrow o$ be given. Let $v4_rlvect_1 : \iota \Rightarrow o$ be given. Let $v2_zmodul01 : \iota \Rightarrow o$ be given. Let $v3_zmodul01 : \iota \Rightarrow o$ be given. Let $v4_zmodul01 : \iota \Rightarrow o$ be given. Let $v5_zmodul01 : \iota \Rightarrow o$ be given. Let $l1_zmodul01 : \iota \Rightarrow o$ be given. Let $v8_zmodul01 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_zmodul01 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m3_zmodul01 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $r1_struct_0 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k9_zmodul01 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r1_zmodul01 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_rlvect_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\ & X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v2_zmodul01 X0) \wedge \\ & ((v3_zmodul01 X0) \wedge ((v4_zmodul01 X0) \wedge ((v5_zmodul01 X0) \wedge (l1_zmodul01 \\ & X0)))))))))) \Rightarrow (\forall X1.((v8_zmodul01 X1 X0) \wedge (m1_zmodul01 \\ & X1 X0)) \Rightarrow (\forall X2.(m3_zmodul01 X2 X0 X1) \Rightarrow ((r1_zmodul01 X0 X2 \\ & X1) \wedge (r1_zmodul01 X0 X1 X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge \\ & ((v2_rlvect_1 X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v2_zmodul01 \\ & X0) \wedge ((v3_zmodul01 X0) \wedge ((v4_zmodul01 X0) \wedge ((v5_zmodul01 X0) \wedge \\ & (l1_zmodul01 X0)))))))))) \wedge (m1_zmodul01 X1 X0)) \Rightarrow (\forall X2. \\ & (m3_zmodul01 X2 X0 X1) \Rightarrow (m1_zmodul01 X2 X0)) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. (((\neg v2_struct_0 \\
& X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 X0) \wedge ((v3_rlvect_1 X0) \wedge \\
& ((v4_rlvect_1 X0) \wedge ((v2_zmodul01 X0) \wedge ((v3_zmodul01 X0) \wedge ((v4_zmodul01 \\
& X0) \wedge ((v5_zmodul01 X0) \wedge (l1_zmodul01 X0)))))))))) \wedge ((m1_subset_1 \\
& X1 (u1_struct_0 X0)) \wedge ((m1_zmodul01 X2 X0) \wedge (m1_zmodul01 X3 X0))) \Rightarrow \\
& (m1_subset_1 (k9_zmodul01 X0 X1 X2 X3) (k2_zfmisc_1 (u1_struct_0 \\
& X0) (u1_struct_0 X0)))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v2_zmodul01 X0) \wedge \\
& ((v3_zmodul01 X0) \wedge ((v4_zmodul01 X0) \wedge ((v5_zmodul01 X0) \wedge (l1_zmodul01 \\
& X0)))))))))) \Rightarrow (\forall X1. (m1_subset_1 X1 (u1_struct_0 X0)) \Rightarrow \\
& (\forall X2. (m1_zmodul01 X2 X0) \Rightarrow (\forall X3. (m1_zmodul01 X3 X0) \Rightarrow \\
& ((r1_zmodul01 X0 X2 X3) \Rightarrow (\forall X4. (m1_subset_1 X4 (k2_zfmisc_1 \\
& (u1_struct_0 X0) (u1_struct_0 X0))) \Rightarrow ((X4 = k9_zmodul01 X0 X1 X2 \\
& X3) \Leftrightarrow ((X1 = k3_rlvect_1 X0 (k2_domain_1 (u1_struct_0 X0) (u1_struct_0 \\
& X0) X4) (k3_domain_1 (u1_struct_0 X0) (u1_struct_0 X0) X4)) \wedge ((\\
& r1_struct_0 X2 (k2_domain_1 (u1_struct_0 X0) (u1_struct_0 X0) \\
& X4)) \wedge (r1_struct_0 X3 (k3_domain_1 (u1_struct_0 X0) (u1_struct_0 \\
& X0) X4))))))))))
\end{aligned} \tag{4}$$

Theorem 1

$$\begin{aligned}
& \forall X0. ((\neg v2_struct_0 X0) \wedge ((v13_algstr_0 X0) \wedge ((v2_rlvect_1 \\
& X0) \wedge ((v3_rlvect_1 X0) \wedge ((v4_rlvect_1 X0) \wedge ((v2_zmodul01 X0) \wedge \\
& ((v3_zmodul01 X0) \wedge ((v4_zmodul01 X0) \wedge ((v5_zmodul01 X0) \wedge (l1_zmodul01 \\
& X0)))))))))) \Rightarrow (\forall X1. ((v8_zmodul01 X1 X0) \wedge (m1_zmodul01 \\
& X1 X0)) \Rightarrow (\forall X2. (m3_zmodul01 X2 X0 X1) \Rightarrow (\forall X3. (m1_subset_1 \\
& X3 (u1_struct_0 X0)) \Rightarrow ((r1_struct_0 X1 (k2_domain_1 (u1_struct_0 \\
& X0) (u1_struct_0 X0) (k9_zmodul01 X0 X3 X1 X2))) \wedge (r1_struct_0 X2 \\
& (k3_domain_1 (u1_struct_0 X0) (u1_struct_0 X0) (k9_zmodul01 X0 \\
& X3 X1 X2))))))
\end{aligned}$$