

t14\_arytm\_3  
(TMSV9dzh9zNLutn5KMBVTmF2t7CvWwmTMjM)

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Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k3\_arytm\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k2\_arytm\_3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r2\_arytm\_3 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $np\_1 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Assume the following.

$$\forall X0.((v3\_ordinal1 X0) \wedge (v7\_ordinal1 X0)) \Rightarrow ((r2\_arytm\_3 X0 k1\_xboole\_0) \wedge (r2\_arytm\_3 np\_1 X0)) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \neg (v1\_xboole\_0 X0) \wedge ((X0 \neq X1) \wedge (v1\_xboole\_0 X1)) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (3)$$

Assume the following.

$$m1\_subset\_1 k1\_xboole\_0 k4\_ordinal1 \quad (4)$$

Assume the following.

$$\forall X0. \forall X1. ((v3\_ordinal1 X0) \wedge (v3\_ordinal1 X1)) \Rightarrow (r2\_arytm\_3 X0 X0) \quad (5)$$

Assume the following.

$$\exists X0. v1\_xboole\_0 X0 \quad (6)$$

Assume the following.

$$v1\_xboole\_0 k1\_xboole\_0 \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v3\_ordinal1\ X0)\wedge(v7\_ordinal1\ X0))\Rightarrow(\forall X1. \\ & ((v3\_ordinal1\ X1)\wedge(v7\_ordinal1\ X1))\Rightarrow(\forall X2.(m1\_subset\_1 \\ & X2\ k4\_ordinal1)\Rightarrow((X2 = k3\_arytm\_3\ X0\ X1)\Leftrightarrow((r2\_arytm\_3\ X2\ X0)\wedge( \\ & (r2\_arytm\_3\ X2\ X1)\wedge(\forall X3.((v3\_ordinal1\ X3)\wedge(v7\_ordinal1 \\ & X3))\Rightarrow(((r2\_arytm\_3\ X3\ X0)\wedge(r2\_arytm\_3\ X3\ X1))\Rightarrow(r2\_arytm\_3\ X3 \\ & X2)))))))) \end{aligned} \tag{8}$$

Assume the following.

$$\begin{aligned} & \forall X0.((v3\_ordinal1\ X0)\wedge(v7\_ordinal1\ X0))\Rightarrow(\forall X1. \\ & ((v3\_ordinal1\ X1)\wedge(v7\_ordinal1\ X1))\Rightarrow(\forall X2.(m1\_subset\_1 \\ & X2\ k4\_ordinal1)\Rightarrow((X2 = k2\_arytm\_3\ X0\ X1)\Leftrightarrow((r2\_arytm\_3\ X0\ X2)\wedge( \\ & (r2\_arytm\_3\ X1\ X2)\wedge(\forall X3.((v3\_ordinal1\ X3)\wedge(v7\_ordinal1 \\ & X3))\Rightarrow(((r2\_arytm\_3\ X0\ X3)\wedge(r2\_arytm\_3\ X1\ X3))\Rightarrow(r2\_arytm\_3\ X2 \\ & X3)))))))) \end{aligned} \tag{9}$$

Assume the following.

$$\forall X0.(v7\_ordinal1\ X0)\Leftrightarrow(X0 \in k4\_ordinal1) \tag{10}$$

Assume the following.

$$\forall X0.(v1\_xboole\_0\ X0)\Rightarrow(v7\_ordinal1\ X0) \tag{11}$$

Assume the following.

$$\forall X0.(v1\_xboole\_0\ X0)\Rightarrow(v3\_ordinal1\ X0) \tag{12}$$

**Theorem 1**

$$\forall X0.((v3\_ordinal1\ X0)\wedge(v7\_ordinal1\ X0))\Rightarrow((k3\_arytm\_3\ X0\ k1\_xboole\_0 = X0)\wedge(k2\_arytm\_3\ X0\ k1\_xboole\_0 = k1\_xboole\_0))$$