

# t14\_hilbasis (TML- gFLm7taTTgS5RgqP2xTT6bu31HR1XSks)

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Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v1\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k15\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_hilbasis : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_group\_1 : \iota \Rightarrow o$  be given. Let  $k3\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_hilbasis : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_group\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_poly : \iota \Rightarrow o$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k14\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l4\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k5\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v6\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l4\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v9\_struct\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v4\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v3\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v6\_vectsp\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. ((\neg v7\_struct\_0 X1) \wedge ((v1\_group\_1 X1) \wedge (l6\_algstr\_0 X1))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 X0) \Rightarrow ((k3\_polynom1 X0 X1 (k3\_hilbasis X0 X2 X1) (k2\_hilbasis X0 X2) = k1\_group\_1 X1) \wedge (\forall X3. ((v1\_relat\_1 X3) \wedge ((v4\_relat\_1 X3 X0) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_partfun1 X3 X0) \wedge ((v4\_valued\_0 X3) \wedge (v2\_pre\_poly X3)))))) \Rightarrow ((X3 \neq k2\_hilbasis X0 X2) \Rightarrow (k3\_polynom1 X0 X1 (k3\_hilbasis X0 X2 X1) X3 = k4\_struct\_0 X1))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 X0) \Rightarrow (\forall X2. (m1\_subset\_1 X2 X0) \Rightarrow ((k2\_hilbasis X0 X1 = k2\_hilbasis X0 X2) \Rightarrow (X1 = X2))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((v1\_funct\_1 X2)\wedge \\ & ((v1\_funct\_2 X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1)))))\wedge((v1\_funct\_1 X3)\wedge((v1\_funct\_2 X3 X0 X1)\wedge(m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1))))))\Rightarrow((r2\_funct\_2 X0 X1 X2 \\ & X3)\Leftrightarrow(X2 = X3)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.k15\_pre\_poly X0 = k14\_pre\_poly X0 \quad (4)$$

Assume the following.

$$\forall X0.((\neg v2\_struct\_0 X0)\wedge((v4\_vectsp\_1 X0)\wedge(l4\_algstr\_0 X0)))\Rightarrow(k1\_group\_1 X0 = k5\_struct\_0 X0) \quad (5)$$

Assume the following.

$$\forall X0.\neg v1\_xboole\_0 (k14\_pre\_poly X0) \quad (6)$$

Assume the following.

$$\forall X0.((\neg v6\_struct\_0 X0)\wedge(l4\_struct\_0 X0))\Rightarrow(\neg v9\_struct\_0 (k5\_struct\_0 X0) X0) \quad (7)$$

Assume the following.

$$\forall X0.(l2\_struct\_0 X0)\Rightarrow(v9\_struct\_0 (k4\_struct\_0 X0) X0) \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))))\Rightarrow(\forall X2.(m2\_subset\_1 \\ & X2 X0 X1)\Rightarrow(m1\_subset\_1 X2 X0)) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(l6\_algstr\_0 X0)\Rightarrow((l2\_algstr\_0 X0)\wedge(l5\_algstr\_0 X0)) \quad (10)$$

Assume the following.

$$\forall X0.(l5\_algstr\_0 X0)\Rightarrow((l4\_algstr\_0 X0)\wedge(l4\_struct\_0 X0)) \quad (11)$$

Assume the following.

$$\forall X0.(l2\_struct\_0 X0)\Rightarrow(l1\_struct\_0 X0) \quad (12)$$

Assume the following.

$$\forall X0.(l2\_algstr\_0 X0)\Rightarrow((l2\_struct\_0 X0)\wedge(l1\_algstr\_0 X0)) \quad (13)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.((m1\_subset\_1 X1 X0)\wedge((\neg v2\_struct\_0 \\ X2)\wedge((v1\_group\_1 X2)\wedge(l5\_algstr\_0 X2))))\Rightarrow((v1\_funct\_1 (k3\_hilbasis \\ X0 X1 X2))\wedge((v1\_funct\_2 (k3\_hilbasis X0 X1 X2) (k15\_pre\_poly X0) \\ (u1\_struct\_0 X2))\wedge(m1\_subset\_1 (k3\_hilbasis X0 X1 X2) (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X2)))))) \end{aligned} \quad (14)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow(m2\_subset\_1 (k2\_hilbasis \\ X0 X1) (k14\_pre\_poly X0) (k15\_pre\_poly X0)) \quad (15)$$

Assume the following.

$$\forall X0.m1\_subset\_1 (k15\_pre\_poly X0) (k1\_zfmisc\_1 (k14\_pre\_poly \\ X0)) \quad (16)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k15\_pre\_poly \\ X0)))\Rightarrow(v4\_funct\_1 X1) \quad (17)$$

Assume the following.

$$\forall X0.(v4\_funct\_1 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow( \\ (v1\_relat\_1 X1)\wedge(v1\_funct\_1 X1))) \quad (18)$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0)\Rightarrow(((\neg v2\_struct\_0 X0)\wedge(v4\_vectsp\_1 \\ X0))\Rightarrow((\neg v2\_struct\_0 X0)\wedge(v1\_group\_1 X0))) \quad (19)$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0)\Rightarrow(((\neg v2\_struct\_0 X0)\wedge(v4\_vectsp\_1 \\ X0))\Rightarrow((\neg v2\_struct\_0 X0)\wedge((v3\_vectsp\_1 X0)\wedge(v6\_vectsp\_1 X0)))) \quad (20)$$

Assume the following.

$$\forall X0.(l1\_struct\_0 X0)\Rightarrow((v2\_struct\_0 X0)\Rightarrow(v7\_struct\_0 X0)) \quad (21)$$

Assume the following.

$$\begin{aligned} \forall X0.(l6\_algstr\_0 X0)\Rightarrow(((\neg v2\_struct\_0 X0)\wedge((v6\_struct\_0 \\ X0)\wedge((v13\_algstr\_0 X0)\wedge((v1\_vectsp\_1 X0)\wedge((v3\_vectsp\_1 X0)\wedge \\ ((v3\_rlvect\_1 X0)\wedge(v4\_rlvect\_1 X0))))))\Rightarrow((\neg v2\_struct\_0 X0)\wedge \\ ((v7\_struct\_0 X0)\wedge((v13\_algstr\_0 X0)\wedge((v1\_vectsp\_1 X0)\wedge((v3\_vectsp\_1 \\ X0)\wedge((v3\_rlvect\_1 X0)\wedge(v4\_rlvect\_1 X0)))))) \end{aligned} \quad (22)$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X1)\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k15\_pre\_poly X0))))\Rightarrow(\forall X2.(m1\_subset\_1 X2 X1)\Rightarrow((v1\_partfun1 X2 X0)\wedge((v4\_valued\_0 X2)\wedge(v2\_pre\_poly X2)))) \quad (23)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 (k15\_pre\_poly X0)))\Rightarrow(\forall X2.(m1\_subset\_1 X2 X1)\Rightarrow(v4\_relat\_1 X2 X0)) \quad (24)$$

**Theorem 1**

$$\forall X0.((\neg v7\_struct\_0 X0)\wedge((v13\_algstr\_0 X0)\wedge((v3\_rlvect\_1 X0)\wedge((v4\_rlvect\_1 X0)\wedge((v1\_vectsp\_1 X0)\wedge((v4\_vectsp\_1 X0)\wedge(l6\_algstr\_0 X0)))))))\Rightarrow(\forall X1.(\neg v1\_xboole\_0 X1)\Rightarrow(\forall X2.(m1\_subset\_1 X2 X1)\Rightarrow(\forall X3.(m1\_subset\_1 X3 X1)\Rightarrow((r2\_funct\_2 (k15\_pre\_poly X1) (u1\_struct\_0 X0) (k3\_hilbasis X1 X2 X0) (k3\_hilbasis X1 X3 X0))\Rightarrow(X2 = X3))))))$$