## t151_member_1 <br> (TMJ3GcAGQiXzGnE3v3ZpVS22u4U8S8DRfE7)

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Let $v 1 \_$membered : $\iota \Rightarrow o$ be given. Let $v 1 \_$xcmplx_0 : $\iota \Rightarrow o$ be given. Let $k 17 \_m e m b e r \_1: ~ \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5 \_$_xboole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k9_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 2_{-}$xboole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6 \_$subset_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_x b o o l e \_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1_{-}$tarski : $\iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_m e m b e r e d ~ X 2\right) \Rightarrow\left(k 9 \_m e m b e r \_1 X 0\left(k 2 \_x b o o l e \_0 X 1 X 2\right)=k 2 \_x b o o l e \_0\right.$
(k9_member_1 X0 X1) (k9_member_1 X0 X2))))
Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 17 \_m e m b e r \_1\left(k 6 \_\right.\right.$subset_1 X0 X1) X2 $=k 6 \_s u b s e t \_1$
( $\left.\left.\left.k 17 \_m e m b e r \_1 X 0 X 2\right)\left(k 17 \_m e m b e r \_1 X 1 X 2\right)\right)\right)$ )
Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 6 \_ \text {subset_1 } X 0 X 1=k 4 \_x b o o l e \_0 X 0 X 1 \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.
$\forall X 0 . \forall X 1 .\left(\left(v 1 \_\right.\right.$membered $\left.X 0\right) \wedge\left(v 1 \_\right.$membered $\left.\left.X 1\right)\right) \Rightarrow($
$\left.v 1 \_m e m b e r e d\left(k 5 \_x b o o l e \_0 X 0 X 1\right)\right)$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(v 1 \_ m e m b e r e d ~ \left(k 4 \_x b o o l e \_0\right.\right.  \tag{6}\\
X 0 X 1))
\end{gather*}
$$

Assume the following.

$$
\begin{array}{r}
\forall X 0 . \forall X 1 . k 5 \_x b o o l e \_0 X 0 X 1=k 2 \_x b o o l e \_0\left(k 4 \_x b o o l e \_0\right. \\
X 0 X 1)\left(k 4 \_x b o o l e \_0 X 1 X 0\right) \tag{7}
\end{array}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 17 \_m e m b e r \_1\right.\right.  \tag{8}\\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right)
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d \quad X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 \quad X 2\right) \Rightarrow\left(k 17 \_m e m b e r \_1\left(k 5 \_x b o o l e \_0 X 0 X 1\right) X 2=k 5 \_x b o o l e \_0\right.$ (k17_member_1 X0 X2) (k17_member_1 X1 X2))))

