# t157_member_1 (TMYhdELrdLrDD9Yve4TG1KHHC5uncwB76R1) 

October 27, 2020

Let $v 2 \_$membered : $\iota \Rightarrow o$ be given. Let $v 1 \_x$ real_0 : $\iota \Rightarrow o$ be given. Let k18_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k3_xboole_0 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4_{-}$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 16 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v 1 \_x x r e a l \_0: \iota \Rightarrow o$ be given. Let $k 1_{\_}$tarski $: \iota \Rightarrow \iota$ be given. Let $k$ 10_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 8 \_$member_ $1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 4 \_m e m b e r \_1\right.\right.$
( $k 3$ _xboole_0 X0 X1) = k3_xboole_0 ( $\left.k 4 \_m e m b e r \_1 ~ X 0\right) ~\left(k 4 \_m e m b e r \_1\right.$ X1)))

Assume the following.
$\forall X 0 .\left(v 2 \_\right.$membered $\left.X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_\right.\right.$membered $\left.X 1\right) \Rightarrow(\forall X 2$.
$\left(v 1 \_x r e a l \_0 X 2\right) \Rightarrow\left(k 16 \_m e m b e r \_1\left(k 3 \_x b o o l e \_0 X 0 X 1\right) X 2=k 3 \_x b o o l e \_0\right.$ (k16_member_1 X0 X2) (k16_member_1 X1 X2))))

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x x r e a l \_0 \quad X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(v 2 \_ m e m b e r e d ~ \left(k 3 \_x b o o l e \_0\right.\right. \\
X 1 X 0)) \tag{4}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 4 \_m e m b e r \_1 X 0\right)\right)$
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 10 \_m e m b e r \_1\right.\right.  \tag{6}\\
\left.\left.X 0 X 1=k 8 \_m e m b e r \_1 X 0\left(k 4 \_m e m b e r \_1 X 1\right)\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow\left(k 18 \_m e m b e r \_1\right.\right.  \tag{7}\\
\left.\left.X 0 \text { X1 }=k 10 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow\left(k 16 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 8 \_m e m b e r \_1\left(k 1 \_ \text {tarski } X 1\right) X 0\right)\right) \tag{8}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x r e a l \_0 X 0\right) \Rightarrow\left(v 1 \_x x r e a l \_0 X 0\right) \tag{9}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
(v1_xreal_0 X2) $\Rightarrow\left(k 18 \_m e m b e r \_1\right.$ ( $k 3 \_$_xboole_0 X0 X1) X2 $=k 3 \_x b o o l e \_0$
(k18_member_1 X0 X2) (k18_member_1 X1 X2))))

