## t159_member_1 <br> (TMLPf3oS6Ej1AnnUsoqVQaLwpYUjAxJvxZy)

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Let $v 2_{\_}$membered : $\iota \Rightarrow 0$ be given. Let $v 1 \_x$ real_ $0: ~ \iota \Rightarrow o$ be given. Let $k 18 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5 \_$xboole $\_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4_{-}$member_1 : $\iota \Rightarrow \iota$ be given. Let $k 16 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v 1 \_x$ xreal_0 : $\iota \Rightarrow$ o be given. Let k1_tarski : $\iota \Rightarrow \iota$ be given. Let k10_member_1: $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 8 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 2 \_x b o o l e \_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_x$ boole $\_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 4 \_m e m b e r \_1\right.\right.$
( $k 5$ _xboole_0 $X 0 X 1$ ) $=k 5 \_x b o o l e \_0\left(k 4 \_m e m b e r \_1 ~ X 0\right) ~\left(k 4 \_m e m b e r \_1 ~\right.$
X1))
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d X 1\right) \Rightarrow(\forall X 2 .\right. \\
\left(v 1 \_x r e a l \_0 X 2\right) \Rightarrow\left(k 16 \_m e m b e r \_1\left(k 5 \_x b o o l e \_0 X 0 X 1\right) X 2=k 5 \_x b o o l e \_0\right. \\
\left.\left.\left.\left(k 16 \_m e m b e r \_1 X 0 X 2\right)\left(k 16 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right) \tag{2}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x x r e a l \_0 X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d \quad\left(k 1 \_t a r s k i X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_ \text {membered } X 0\right) \wedge\left(v 2 \_ \text {_membered } X 1\right)\right) \Rightarrow( \\
\left.v 2 \_m e m b e r e d\left(k 5 \_x b o o l e \_0 X 0 X 1\right)\right) \tag{4}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 2 \_m e m b e r e d\left(k 4 \_m e m b e r \_1 X 0\right)\right) \tag{5}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {membered } X 1\right) \Rightarrow\left(k 10 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 8 \_m e m b e r \_1 X 0\left(k 4 \_m e m b e r \_1 X 1\right)\right)\right) \tag{6}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 . k 5 \_x b o o l e \_0 X 0 X 1=k 2 \_x b o o l e \_0\left(k 4 \_x b o o l e \_0\right.  \tag{7}\\
X 0 X 1)\left(k 4 \_x b o o l e \_0 X 1 X 0\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow\left(k 18 \_m e m b e r \_1\right.\right.  \tag{8}\\
\left.\left.X 0 X 1=k 10 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow\left(k 16 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 8 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x r e a l \_0 X 0\right) \Rightarrow\left(v 1 \_x x r e a l \_0 X 0\right) \tag{10}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_\right.$membered $\left.X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 2 \_\right.$membered $\left.X 1\right) \Rightarrow(\forall X 2$.
$\left(v 1 \_x r e a l \_0 \quad X 2\right) \Rightarrow\left(k 18 \_m e m b e r \_1\left(k 5 \_x b o o l e \_0 X 0 X 1\right) X 2=k 5 \_x b o o l e \_0\right.$ (k18_member_1 X0 X2) (k18_member_1 X1 X2))))

