

## t15\_bvfunc11

(TMWhYB1L7urM8K1bJHeaJJHU8UoVNEveQMZ)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_margrel1 : \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_bvfunc\_2 : \iota \Rightarrow \iota$  be given. Let  $m1\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_bvfunc\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_bvfunc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_bvfunc\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_bvfunc\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_partit1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ (k1\_partit1 X0))) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 \\ X2 X0 k6\_margrel1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ X0 k6\_margrel1)))) \Rightarrow (\forall X3.(m1\_eqrel\_1 X3 X0) \Rightarrow (r2\_funct\_2 \\ X0 k6\_margrel1 (k1\_bvfunc\_1 X0 (k6\_bvfunc\_2 X0 X2 X1 X3)) (k7\_bvfunc\_2 \\ X0 (k1\_bvfunc\_1 X0 X2) X1 X3)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((v1\_funct\_1 X1) \wedge ( \\ (v1\_funct\_2 X1 X0 k6\_margrel1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 ( \\ k2\_zfmisc\_1 X0 k6\_margrel1)))) \Rightarrow (\forall X2.(m1\_subset\_1 X2 \\ (k1\_zfmisc\_1 (k1\_bvfunc\_2 X0))) \Rightarrow (\forall X3.(m1\_eqrel\_1 X3 X0) \Rightarrow \\ (\forall X4.(m1\_eqrel\_1 X4 X0) \Rightarrow ((v2\_bvfunc\_2 X2 X0) \Rightarrow (r2\_funct\_2 \\ X0 k6\_margrel1 (k6\_bvfunc\_2 X0 (k6\_bvfunc\_2 X0 X1 X2 X3) X2 X4) (k6\_bvfunc\_2 \\ X0 (k6\_bvfunc\_2 X0 X1 X2 X4) X2 X3)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.\forall X3.(((v1\_funct\_1 X2) \wedge \\ ((v1\_funct\_2 X2 X0 X1) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ X0 X1)))) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 X0 X1) \wedge (m1\_subset\_1 \\ X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \Rightarrow ((r2\_funct\_2 X0 X1 X2 \\ X3) \Leftrightarrow (X2 = X3)) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.k1_{bvfunc.2} X0 = k1_{partit1} X0 \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1_{xboole.0} X0) \wedge \\ & (((v1_{funct.1} X1) \wedge ((v1_{funct.2} X1 X0 k6_{margrel1}) \wedge (m1_{subset.1} \\ & X1 (k1_{zfmisc.1} (k2_{zfmisc.1} X0 k6_{margrel1})))))) \wedge ((m1_{subset.1} \\ & X2 (k1_{zfmisc.1} (k1_{bvfunc.2} X0))) \wedge (m1_{eqrel.1} X3 X0)))) \Rightarrow ((v1_{funct.1} \\ & (k6_{bvfunc.2} X0 X1 X2 X3)) \wedge ((v1_{funct.2} (k6_{bvfunc.2} X0 X1 X2 X3) \\ & X0 k6_{margrel1}) \wedge (m1_{subset.1} (k6_{bvfunc.2} X0 X1 X2 X3) (k1_{zfmisc.1} \\ & (k2_{zfmisc.1} X0 k6_{margrel1})))))) \end{aligned} \quad (5)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(\neg v1_{xboole.0} X0) \Rightarrow (\forall X1.((v1_{funct.1} X1) \wedge ( \\ & (v1_{funct.2} X1 X0 k6_{margrel1}) \wedge (m1_{subset.1} X1 (k1_{zfmisc.1} ( \\ & k2_{zfmisc.1} X0 k6_{margrel1})))))) \Rightarrow (\forall X2.(m1_{subset.1} X2 \\ & (k1_{zfmisc.1} (k1_{bvfunc.2} X0))) \Rightarrow (\forall X3.(m1_{eqrel.1} X3 X0) \Rightarrow \\ & (\forall X4.(m1_{eqrel.1} X4 X0) \Rightarrow ((v2_{bvfunc.2} X2 X0) \Rightarrow (r2_{funct.2} \\ & X0 k6_{margrel1} (k1_{bvfunc.1} X0 (k6_{bvfunc.2} X0 (k6_{bvfunc.2} X0 \\ & X1 X2 X3) X2 X4)) (k7_{bvfunc.2} X0 (k1_{bvfunc.1} X0 (k6_{bvfunc.2} X0 \\ & X1 X2 X4)) X2 X3)))))) \end{aligned}$$