

t15_ens_1 (TMYyzpT-
mGVE7DxPG8619yLB6W3aDfDPfeLK)

October 27, 2020

Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_xboole_0 : \iota$ be given. Let $k1_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k7_ens_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_ens_1 : \iota \Rightarrow \iota$ be given. Let $k1_ens_1 : \iota \Rightarrow \iota$ be given. Let $k4_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v4_funct_1 : \iota \Rightarrow o$ be given. Let $k2_tarski : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k1_tarski : \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (m1_subset_1 X1 X0) \Rightarrow \\ & (\forall X2. (m1_subset_1 X2 X0) \Rightarrow (\forall X3. ((v1_funct_1 X3) \wedge \\ & ((v1_funct_2 X3 X1 X2) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 \\ & X1 X2)))))) \Rightarrow (((X2 = k1_xboole_0) \Rightarrow (X1 = k1_xboole_0)) \Rightarrow (k1_domain_1 \\ & (k2_zfmisc_1 X0 X0) (k1_zfmisc_1 (k2_zfmisc_1 X1 X2)) (k1_domain_1 \\ & X0 X0 X1 X2) X3 \in k2_ens_1 X0)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1_subset_1 X0 X1) \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (X1 \in k1_ens_1 X0) \Leftrightarrow (\\ & \exists X2. (m1_subset_1 X2 X0) \wedge (\exists X3. (m1_subset_1 X3 X0) \wedge \\ & (((X3 = k1_xboole_0) \Rightarrow (X2 = k1_xboole_0)) \wedge ((v1_funct_1 X1) \wedge (\\ & v1_funct_2 X1 X2 X3) \wedge (m1_subset_1 X1 (k1_zfmisc_1 (k2_zfmisc_1 \\ & X2 X3)))))))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1_xboole_0 X0) \wedge \\ & ((\neg v1_xboole_0 X1) \wedge ((m1_subset_1 X2 X0) \wedge (m1_subset_1 X3 X1)))) \Rightarrow \\ & (k1_domain_1 X0 X1 X2 X3 = k4_tarski X2 X3) \end{aligned} \tag{4}$$

Assume the following.

$$\forall X0. \neg v1_xboole_0 (k1_zfmisc_1 X0) \quad (5)$$

Assume the following.

$$\forall X0. (\neg v1_xboole_0 X0) \Rightarrow ((v4_funct_1 (k1_ens_1 X0)) \wedge (\neg v1_xboole_0 (k1_ens_1 X0))) \quad (6)$$

Assume the following.

$$\forall X0. \forall X1. ((\neg v1_xboole_0 X0) \wedge (\neg v1_xboole_0 X1)) \Rightarrow (\neg v1_xboole_0 (k2_zfmisc_1 X0 X1)) \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1_xboole_0 X0) \wedge \\ & ((\neg v1_xboole_0 X1) \wedge ((m1_subset_1 X2 X0) \wedge (m1_subset_1 X3 X1)))) \Rightarrow \\ & (m1_subset_1 (k1_domain_1 X0 X1 X2 X3) (k2_zfmisc_1 X0 X1)) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (m1_subset_1 X1 X0) \Rightarrow \\ & (\forall X2. (m1_subset_1 X2 X0) \Rightarrow (k7_ens_1 X0 X1 X2 = ReplSep (toset \\ & (\lambda X3 : \iota. m1_subset_1 X3 (k1_ens_1 X0))) (\lambda X3 : \iota. k1_domain_1 \\ & (k2_zfmisc_1 X0 X0) (k1_ens_1 X0) (k1_domain_1 X0 X0 X1 X2) X3 \in k2_ens_1 \\ & X0) (\lambda X3 : \iota. k1_domain_1 (k2_zfmisc_1 X0 X0) (k1_ens_1 X0) \\ & (k1_domain_1 X0 X0 X1 X2) X3)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0. \forall X1. k4_tarski X0 X1 = k2_tarski (k2_tarski X0 X1) (k1_tarski X0) \quad (10)$$

Theorem 1

$$\begin{aligned} & \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (m1_subset_1 X1 X0) \Rightarrow \\ & (\forall X2. (m1_subset_1 X2 X0) \Rightarrow (\forall X3. ((v1_funct_1 X3) \wedge \\ & ((v1_funct_2 X3 X1 X2) \wedge (m1_subset_1 X3 (k1_zfmisc_1 (k2_zfmisc_1 \\ & X1 X2)))))) \Rightarrow (((X2 = k1_xboole_0) \Rightarrow (X1 = k1_xboole_0)) \Rightarrow (k1_domain_1 \\ & (k2_zfmisc_1 X0 X0) (k1_zfmisc_1 (k2_zfmisc_1 X1 X2)) (k1_domain_1 \\ & X0 X0 X1 X2) X3 \in k7_ens_1 X0 X1 X2)))))) \end{aligned}$$