

## t15\_scmpds\_6

(TMbZ1wWpvr8DQHxMcizreRAdJAcozsSWBnd)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_compos\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_scmpds\_2 : \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v5\_funct\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $v5\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_numbers : \iota$  be given. Let  $v6\_compos\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_scmpds\_5 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $v1\_afinsq\_1 : \iota \Rightarrow o$  be given. Let  $v2\_scmpds\_4 : \iota \Rightarrow o$  be given. Let  $v3\_scmpds\_4 : \iota \Rightarrow o$  be given. Let  $v1\_ami\_2 : \iota \Rightarrow o$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_scmpds\_4 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_scmpds\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k8\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_compos\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_compos\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_scmpds\_4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_compos\_1 : \iota \Rightarrow o$  be given. Let  $k3\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $l1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k16\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k7\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((v1\_relat\_1 X0) \wedge ((v4\_relat\_1 X0 k5\_numbers) \wedge ((v5\_relat\_1 \\
 & X0 (u1\_compos\_1 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X0) \wedge (v1\_partfun1 \\
 & X0 k5\_numbers)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 \\
 & X1 (u1\_struct\_0 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X1) \wedge ((v5\_funct\_1 \\
 & X1 (k2\_memstr\_0 np\_2 k1\_scmpds\_2)) \wedge ((v1\_partfun1 X1 (u1\_struct\_0 \\
 & k1\_scmpds\_2)) \wedge (v5\_memstr\_0 X1 np\_2 k1\_scmpds\_2 k6\_numbers)))))) \Rightarrow \\
 & (\forall X2.((v1\_scmpds\_5 X2) \wedge (m1\_subset\_1 X2 (u1\_compos\_1 k1\_scmpds\_2))) \Rightarrow \\
 & (k2\_extpro\_1 np\_2 k1\_scmpds\_2 X2 X1 = k6\_scmpds\_4 (k9\_compos\_1 \\
 & k1\_scmpds\_2 X2) X1 X0))
 \end{aligned}
 \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_ami\_2 X0) \wedge (m1\_subset\_1 X0 (u1\_struct\_0 k1\_scmpds\_2))) \Rightarrow \\
& \quad (\forall X1.((v1\_relat\_1 X1) \wedge ((v4\_relat\_1 X1 k5\_numbers) \wedge ((v5\_relat\_1 X1 (u1\_compos\_1 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X1) \wedge (v1\_partfun1 X1 k5\_numbers)))))) \Rightarrow (\forall X2.((v1\_relat\_1 X2) \wedge ((v4\_relat\_1 X2 (u1\_struct\_0 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X2) \wedge ((v5\_funct\_1 X2 (k2\_memstr\_0 np\_2 k1\_scmpds\_2)) \wedge ((v1\_partfun1 X2 (u1\_struct\_0 k1\_scmpds\_2)) \wedge (v5\_memstr\_0 X2 np\_2 k1\_scmpds\_2 k6\_numbers)))))) \Rightarrow (\forall X3.((\neg v1\_xboole\_0 X3) \wedge ((v1\_relat\_1 X3) \wedge ((v4\_relat\_1 X3 k5\_numbers) \wedge ((v5\_relat\_1 X3 (u1\_compos\_1 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X3) \wedge ((v1\_finset\_1 X3) \wedge ((v1\_afinsq\_1 X3) \wedge ((v2\_compos\_1 X3 k1\_scmpds\_2) \wedge (v2\_scmpds\_4 X3)))))))))) \Rightarrow (\forall X4.((\neg v1\_xboole\_0 X4) \wedge ((v1\_relat\_1 X4) \wedge ((v4\_relat\_1 X4 k5\_numbers) \wedge ((v5\_relat\_1 X4 (u1\_compos\_1 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 X4) \wedge ((v1\_finset\_1 X4) \wedge ((v1\_afinsq\_1 X4) \wedge ((v2\_scmpds\_4 X4) \wedge (v3\_scmpds\_4 X4)))))))))) \Rightarrow (k1\_funct\_1 (k6\_scmpds\_4 (k1\_scmpds\_4 X3 X4) X2 X1) X0 = k1\_funct\_1 (k6\_scmpds\_4 X4 (k8\_memstr\_0 np\_2 k1\_scmpds\_2 (k6\_scmpds\_4 X3 X2 X1)) X1) X0))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. ((l1\_compos\_1 X0) \wedge (m1\_subset\_1 X1 (u1\_compos\_1 X0))) \Rightarrow (k9\_compos\_1 X0 X1 = k3\_afinsq\_1 X1) \tag{3}$$

Assume the following.

$$\forall X0. \neg v1\_xboole\_0 (k3\_afinsq\_1 X0) \tag{4}$$

Assume the following.

$$\forall X0. ((v6\_compos\_0 X0 (u1\_compos\_1 k1\_scmpds\_2)) \wedge (m1\_subset\_1 X0 (u1\_compos\_1 k1\_scmpds\_2))) \Rightarrow (v2\_compos\_1 (k3\_afinsq\_1 X0) k1\_scmpds\_2) \tag{5}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((v1\_scmpds\_5 X0) \wedge (m1\_subset\_1 X0 (u1\_compos\_1 k1\_scmpds\_2))) \Rightarrow \\
& \quad ((\neg v1\_xboole\_0 (k3\_afinsq\_1 X0)) \wedge ((v1\_relat\_1 (k3\_afinsq\_1 X0) \wedge ((v4\_relat\_1 (k3\_afinsq\_1 X0) k5\_numbers) \wedge ((v5\_relat\_1 (k3\_afinsq\_1 X0) (u1\_compos\_1 k1\_scmpds\_2)) \wedge ((v1\_funct\_1 (k3\_afinsq\_1 X0) \wedge ((v1\_finset\_1 (k3\_afinsq\_1 X0) \wedge ((v1\_afinsq\_1 (k3\_afinsq\_1 X0) \wedge (v2\_scmpds\_4 (k3\_afinsq\_1 X0))))))))))
\end{aligned} \tag{6}$$

Assume the following.

$$\forall X0. \forall X1. (l1\_extpro\_1 X1 X0) \Rightarrow ((l1\_memstr\_0 X1 X0) \wedge (l1\_compos\_1 X1)) \tag{7}$$

Assume the following.

$$(v1\_extpro\_1\ k1\_scmpds\_2\ np\_2) \wedge (l1\_extpro\_1\ k1\_scmpds\_2\ np\_2) \quad (8)$$

Assume the following.

$$\forall X0. \forall X1. k16\_funcop\_1\ X0\ X1 = k7\_funcop\_1\ (k1\_tarski\ X0)\ X1 \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0. (m1\_subset\_1\ X0\ (u1\_compos\_1\ k1\_scmpds\_2)) \Rightarrow (\forall X1. \\ & ((\neg v1\_xboole\_0\ X1) \wedge ((v1\_relat\_1\ X1) \wedge ((v4\_relat\_1\ X1\ k5\_numbers) \wedge \\ & ((v5\_relat\_1\ X1\ (u1\_compos\_1\ k1\_scmpds\_2)) \wedge ((v1\_funct\_1\ X1) \wedge \\ & ((v1\_finset\_1\ X1) \wedge (v1\_afinsq\_1\ X1)))))) \Rightarrow (k2\_scmpds\_4\ X0\ X1 = \\ & k1\_scmpds\_4\ (k9\_compos\_1\ k1\_scmpds\_2\ X0)\ X1)) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0. k3\_afinsq\_1\ X0 = k16\_funcop\_1\ k6\_numbers\ X0 \quad (11)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. ((v1\_relat\_1\ X0) \wedge ((v4\_relat\_1\ X0\ k5\_numbers) \wedge ((v5\_relat\_1 \\ & X0\ (u1\_compos\_1\ k1\_scmpds\_2)) \wedge ((v1\_funct\_1\ X0) \wedge (v1\_partfun1 \\ & X0\ k5\_numbers)))))) \Rightarrow (\forall X1. ((v1\_relat\_1\ X1) \wedge ((v4\_relat\_1 \\ & X1\ (u1\_struct\_0\ k1\_scmpds\_2)) \wedge ((v1\_funct\_1\ X1) \wedge ((v5\_funct\_1 \\ & X1\ (k2\_memstr\_0\ np\_2\ k1\_scmpds\_2)) \wedge ((v1\_partfun1\ X1\ (u1\_struct\_0 \\ & k1\_scmpds\_2)) \wedge (v5\_memstr\_0\ X1\ np\_2\ k1\_scmpds\_2\ k6\_numbers)))))) \Rightarrow \\ & (\forall X2. ((v6\_compos\_0\ X2\ (u1\_compos\_1\ k1\_scmpds\_2)) \wedge ((v1\_scmpds\_5 \\ & X2) \wedge (m1\_subset\_1\ X2\ (u1\_compos\_1\ k1\_scmpds\_2)))))) \Rightarrow (\forall X3. \\ & ((\neg v1\_xboole\_0\ X3) \wedge ((v1\_relat\_1\ X3) \wedge ((v4\_relat\_1\ X3\ k5\_numbers) \wedge \\ & ((v5\_relat\_1\ X3\ (u1\_compos\_1\ k1\_scmpds\_2)) \wedge ((v1\_funct\_1\ X3) \wedge \\ & ((v1\_finset\_1\ X3) \wedge ((v1\_afinsq\_1\ X3) \wedge ((v2\_scmpds\_4\ X3) \wedge (v3\_scmpds\_4 \\ & X3)))))))))) \Rightarrow (\forall X4. ((v1\_ami\_2\ X4) \wedge (m1\_subset\_1\ X4\ (u1\_struct\_0 \\ & k1\_scmpds\_2))) \Rightarrow (k1\_funct\_1\ (k6\_scmpds\_4\ (k2\_scmpds\_4\ X2\ X3) \\ & X1\ X0)\ X4 = k1\_funct\_1\ (k6\_scmpds\_4\ X3\ (k8\_memstr\_0\ np\_2\ k1\_scmpds\_2 \\ & (k2\_extpro\_1\ np\_2\ k1\_scmpds\_2\ X2\ X1))\ X0)\ X4)))) \end{aligned}$$