

# t15\_tmap\_1

## (TMaYvocePtdbjX4rbcztjbqFH7giXuFyYzj)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_tsep\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_connsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v3\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\ & (m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow ((m1\_connsp\_2 \\ & X2 X0 X1) \Leftrightarrow (\exists X3.(m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 \\ & X0))) \wedge ((v3\_pre\_topc X3 X0) \wedge ((r1\_tarski X3 X2) \wedge (X1 \in X3)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. ((r1\_tarski X0 X1) \wedge (r1\_tarski X1 X2)) \Rightarrow (r1\_tarski X0 X2) \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ & X0))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge (m1\_pre\_topc X1 X0)) \Rightarrow ( \\ & \forall X2.((\neg v2\_struct\_0 X2) \wedge (m1\_pre\_topc X2 X0)) \Rightarrow (\forall X3. \\ & (m1\_subset\_1 X3 (u1\_struct\_0 (k1\_tsep\_1 X0 X1 X2))) \Rightarrow (\forall X4. \\ & (m1\_subset\_1 X4 (k1\_zfmisc\_1 (u1\_struct\_0 X1))) \Rightarrow (\forall X5. \\ & (m1\_subset\_1 X5 (k1\_zfmisc\_1 (u1\_struct\_0 X2))) \Rightarrow (\neg (v3\_pre\_topc \\ & X4 X1) \wedge ((X3 \in X4) \wedge ((v3\_pre\_topc X5 X2) \wedge ((X3 \in X5) \wedge (\forall X6. ( \\ & m1\_subset\_1 X6 (k1\_zfmisc\_1 (u1\_struct\_0 (k1\_tsep\_1 X0 X1 X2)))))) \Rightarrow \\ & (\neg (v3\_pre\_topc X6 (k1\_tsep\_1 X0 X1 X2)) \wedge ((X3 \in X6) \wedge (r1\_tarski X6 \\ & (k2\_xboole\_0 X4 X5)))))))))) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. \forall X3. ((r1\_tarski X0 X1) \wedge (r1\_tarski X2 X3)) \Rightarrow (r1\_tarski (k2\_xboole\_0 X0 X2) (k2\_xboole\_0 X1 X3)) \quad (4)$$

Assume the following.

$$\forall X0.(l1\_pre\_topc\ X0)\Rightarrow(\forall X1.(m1\_pre\_topc\ X1\ X0)\Rightarrow(l1\_pre\_topc\ X1)) \quad (5)$$

Assume the following.

$$\begin{aligned} &\forall X0.\forall X1.(((\neg v2\_struct\_0\ X0)\wedge((v2\_pre\_topc\ X0)\wedge \\ &(l1\_pre\_topc\ X0)))\wedge(m1\_subset\_1\ X1\ (u1\_struct\_0\ X0)))\Rightarrow(\forall X2. \\ &(m1\_connsp\_2\ X2\ X0\ X1)\Rightarrow(m1\_subset\_1\ X2\ (k1\_zfmisc\_1\ (u1\_struct\_0 \\ &X0)))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.((v2\_pre\_topc\ X0)\wedge(l1\_pre\_topc\ X0))\Rightarrow(\forall X1.(m1\_pre\_topc\ X1\ X0)\Rightarrow(v2\_pre\_topc\ X1)) \quad (7)$$

**Theorem 1**

$$\begin{aligned} &\forall X0.((\neg v2\_struct\_0\ X0)\wedge((v2\_pre\_topc\ X0)\wedge(l1\_pre\_topc \\ &X0)))\Rightarrow(\forall X1.((\neg v2\_struct\_0\ X1)\wedge(m1\_pre\_topc\ X1\ X0))\Rightarrow( \\ &\forall X2.((\neg v2\_struct\_0\ X2)\wedge(m1\_pre\_topc\ X2\ X0))\Rightarrow(\forall X3. \\ &(m1\_subset\_1\ X3\ (u1\_struct\_0\ (k1\_tsep\_1\ X0\ X1\ X2))))\Rightarrow(\forall X4. \\ &(m1\_subset\_1\ X4\ (u1\_struct\_0\ X1))\Rightarrow(\forall X5.(m1\_subset\_1\ X5 \\ &(u1\_struct\_0\ X2))\Rightarrow(((X4 = X3)\wedge(X5 = X3))\Rightarrow(\forall X6.(m1\_connsp\_2 \\ &X6\ X1\ X4)\Rightarrow(\forall X7.(m1\_connsp\_2\ X7\ X2\ X5)\Rightarrow(\exists X8.(m1\_subset\_1 \\ &X8\ (k1\_zfmisc\_1\ (u1\_struct\_0\ (k1\_tsep\_1\ X0\ X1\ X2))))\wedge((v3\_pre\_topc \\ &X8\ (k1\_tsep\_1\ X0\ X1\ X2))\wedge((X3 \in X8)\wedge(r1\_tarski\ X8\ (k2\_xboole\_0\ X6 \\ &X7)))))))))) \end{aligned}$$