

# t160\_zf\_lang1 (TMPNbnEsmstqM- TacBYMC3QFyDpFXG5bjit7)

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Let  $v1\_zf\_lang : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zf\_lang : \iota$  be given. Let  $k8\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_zf\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $m1\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_zf\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $r1\_xreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $np\_5 : \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(m2\_finseq\_1 X0 k5\_numbers) \Rightarrow (\forall X1.(m2\_finseq\_1 \\ & X1 k5\_numbers) \Rightarrow (\forall X2.(m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \Rightarrow \\ & (\forall X3.(m2\_subset\_1 X3 k5\_numbers k1\_zf\_lang) \Rightarrow ((k8\_zf\_lang \\ & X2 X0 = k8\_zf\_lang X3 X1) \Rightarrow ((X2 = X3) \wedge (X0 = X1)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge \\ & (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2.(m2\_subset\_1 \\ & X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.\forall X1.(m2\_finseq\_1 X1 X0) \Leftrightarrow (m1\_finseq\_1 X1 X0) \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((v1\_zf\_lang X0) \wedge (m1\_finseq\_1 \\ & X0 k5\_numbers)) \wedge ((m1\_subset\_1 X1 k1\_zf\_lang) \wedge (m1\_subset\_1 X2 \\ & k1\_zf\_lang))) \Rightarrow (k6\_zf\_lang1 X0 X1 X2 = k5\_zf\_lang1 X0 X1 X2) \end{aligned} \quad (4)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (\forall X1. \\ & ((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow (\forall X2.( \\ & m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X3.(m2\_subset\_1 \\ & X3 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X4.(m2\_subset\_1 X4 k5\_numbers \\ & k1\_zf\_lang) \Rightarrow (\forall X5.(m2\_subset\_1 X5 k5\_numbers k1\_zf\_lang) \Rightarrow \\ & ((X0 = k5\_zf\_lang1 X1 X2 X3) \Rightarrow (((\neg(X4 = X5) \wedge (X5 \neq X2)) \wedge (\neg(X4 = X3) \wedge \\ & (X5 = X2))) \vee (k8\_zf\_lang X4 X0 = k5\_zf\_lang1 (k8\_zf\_lang X5 X1) X2 \\ & X3)))))))))) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 X0 k1\_zf\_lang) \wedge ((v1\_zf\_lang X1) \wedge (m1\_finseq\_1 X1 k5\_numbers))) \Rightarrow (v1\_zf\_lang (k8\_zf\_lang X0 X1)) \quad (7)$$

Assume the following.

$$\neg v1\_xboole\_0 k1\_zf\_lang \quad (8)$$

Assume the following.

$$\forall X0. \forall X1. ((m1\_subset\_1 X0 k1\_zf\_lang) \wedge (m1\_finseq\_1 X1 k5\_numbers)) \Rightarrow (m2\_finseq\_1 (k8\_zf\_lang X0 X1) k5\_numbers) \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((v1\_zf\_lang X0) \wedge (m1\_finseq\_1 \\ & X0 k5\_numbers)) \wedge ((m1\_subset\_1 X1 k1\_zf\_lang) \wedge (m1\_subset\_1 X2 \\ & k1\_zf\_lang))) \Rightarrow ((v1\_zf\_lang (k6\_zf\_lang1 X0 X1 X2)) \wedge (m2\_finseq\_1 \\ & (k6\_zf\_lang1 X0 X1 X2) k5\_numbers)) \end{aligned} \quad (10)$$

Assume the following.

$$m1\_subset\_1 k1\_zf\_lang (k1\_zfmisc\_1 k5\_numbers) \quad (11)$$

Assume the following.

$$\begin{aligned} k1\_zf\_lang = \text{ReplSep } (& \text{toset } (\lambda X0 : \iota. m1\_subset\_1 X0 k5\_numbers)) \\ & (\lambda X0 : \iota. r1\_xreal\_0 np\_5 X0) (\lambda X0 : \iota. X0) \end{aligned} \quad (12)$$

Assume the following.

$$\forall X0. (v1\_xboole\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)) \Rightarrow (v1\_xboole\_0 X1)) \quad (13)$$

### Theorem 1

$$\begin{aligned} & \forall X0. ((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (\forall X1. \\ & ((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow (\forall X2.( \\ & m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X3.(m2\_subset\_1 \\ & X3 k5\_numbers k1\_zf\_lang) \Rightarrow ((k8\_zf\_lang X2 X0 = k6\_zf\_lang1 (k8\_zf\_lang \\ & X3 X1) X3 X2) \Leftrightarrow (X0 = k6\_zf\_lang1 X1 X3 X2)))))) \end{aligned}$$