## t165_member_1 <br> (TMaCTpg18UwsyVoAZeUYeXY2VXG4PoqhL5k)

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Let $v 1_{\_}$membered : $\iota \Rightarrow 0$ be given. Let $v 1 \_x c m p l x_{-} 0: \iota \Rightarrow o$ be given. Let $k 19 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 3 \_x$ boole $\_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5$ _member_1 : $\iota \Rightarrow \iota$ be given. Let $k 17 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1 \_$tarski : $\iota \Rightarrow \iota$ be given. Let $v 1 \_x$ boole_0 $: \iota \Rightarrow o$ be given. Let $k 11 \_m e m b e r \_1$ : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 9$ _member_ $1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 5 \_m e m b e r \_1\right.\right.$
$\left(k 3 \_x b o o l e \_0 X 0 X 1\right)=k 3 \_x b o o l e \_0\left(k 5 \_m e m b e r \_1 ~ X 0\right) ~\left(k 5 \_m e m b e r \_1\right.$ X1)))

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 \text {. }\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow(\forall X 2 .\right. \\
\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 17 \_m e m b e r \_1\left(k 3 \_x b o o l e \_0 X 0 X 1\right) X 2=k 3 \_x b o o l e \_0\right. \\
\left.\left.\left.\left(k 17 \_m e m b e r \_1 X 0 X 2\right)\left(k 17 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right) \tag{2}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{3}
\end{equation*}
$$

Assume the following.
$\forall X 0 .\left(\left(\neg v 1 \_\right.\right.$xboole_0 $\left.\left.X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 0\right)\right) \Rightarrow\left(\left(\neg v 1 \_x b o o l e \_0\right.\right.$
$\left.\left.\left(k 5 \_m e m b e r \_1 X 0\right)\right) \wedge\left(v 1 \_m e m b e r e d ~\left(k 5 \_m e m b e r \_1 X 0\right)\right)\right)$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_x b o o l e \_0 X 0\right) \Rightarrow\left(\left(v 1 \_x b o o l e \_0\left(k 5 \_m e m b e r \_1 X 0\right)\right) \wedge\right. \\
\left.\left(v 1 \_m e m b e r e d\left(k 5 \_m e m b e r \_1 X 0\right)\right)\right) \tag{5}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(v 1 \_ m e m b e r e d ~ \left(k 3 \_x b o o l e \_0\right.\right. \\
X 1 X 0)) \tag{6}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_ \text {membered } X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1 X 0\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right) \tag{7}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 19 \_m e m b e r \_1\right.\right.  \tag{8}\\
\left.\left.X 0 X 1=k 11 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 17 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 3 \_x b o o l e \_0 X 0 X 1=k 3 \_x b o o l e \_0 X 1 X 0 \tag{10}
\end{equation*}
$$

## Theorem 1

$\forall X 0$.(v1_membered $X 0) \Rightarrow\left(\forall X 1\right.$. $\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2$.
$\left(v 1 \_x c m p l x \_0 \quad X 2\right) \Rightarrow\left(k 19 \_m e m b e r \_1\left(k 3 \_x b o o l e \_0 X 0 X 1\right) X 2=k 3 \_x b o o l e \_0\right.$
(k19_member_1 X0 X2) (k19_member_1 X1 X2))))

