

t16\_card\_lar  
 (TMFXhbZd7ayxF8enyP8ebxYmoVTuoTR4yDz)

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Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v4\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k8\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_card\_lar : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_ordinal1 : \iota \Rightarrow \iota$  be given. Let  $v1\_card\_lar : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_ordinal1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k3\_ordinal2 : \iota \Rightarrow \iota$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0.((v3\_ordinal1 X0) \wedge ((v4\_ordinal1 X0) \wedge (\neg v1\_finset\_1 \\ X0))) \Rightarrow (\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)) \Rightarrow ((v1\_card\_lar \\ X1 X0) \Leftrightarrow (\forall X2.(v3\_ordinal1 X2) \Rightarrow (\neg (X2 \in X0) \wedge (\forall X3.( \\ v3\_ordinal1 X3) \Rightarrow (\neg (X3 \in X1) \wedge (r1\_ordinal1 X2 X3))))))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. \forall X1.(m1\_subset\_1 X0 (k1\_zfmisc\_1 X1)) \Leftrightarrow (r1\_tarski X0 X1) \quad (2)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (( \\ X0 \in X1) \Leftrightarrow (r1\_ordinal1 (k1\_ordinal1 X0) X1))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1.r1\_tarski (k3\_xboole\_0 X0 X1) X0 \quad (4)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (( \\ r1\_ordinal1 X0 X1) \vee (X1 \in X0))) \quad (5)$$

Assume the following.

$$\forall X0. \forall X1.((v3\_ordinal1 X0) \wedge (v3\_ordinal1 X1)) \Rightarrow ( \\ (r1\_ordinal1 X0 X1) \Leftrightarrow (r1\_tarski X0 X1)) \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 X0))\Rightarrow(k9\_subset\_1 X0 X1 X2 = k3\_xboole\_0 X1 X2) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(k8\_subset\_1 X0 X1 X2 = k3\_xboole\_0 X1 X2) \quad (8)$$

Assume the following.

$$\forall X0.(v3\_ordinal1 X0)\Rightarrow((\neg v1\_xboole\_0 (k1\_ordinal1 X0))\wedge (v3\_ordinal1 (k1\_ordinal1 X0))) \quad (9)$$

Assume the following.

$$\forall X0.\forall X1.(((v3\_ordinal1 X0)\wedge(v4\_ordinal1 X0)\wedge (\neg v1\_finset\_1 X0))\wedge(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))\Rightarrow(m1\_subset\_1 (k2\_card\_lar X0 X1) (k1\_zfmisc\_1 X0)) \quad (10)$$

Assume the following.

$$\forall X0.((v3\_ordinal1 X0)\wedge(v4\_ordinal1 X0)\wedge(\neg v1\_finset\_1 X0))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(k2\_card\_lar X0 X1 = ReplSep (toset (\lambda X2 : \iota.m1\_subset\_1 X2 X0)) (\lambda X2 : \iota.(\neg v1\_finset\_1 X2)\wedge((v4\_ordinal1 X2)\wedge(k3\_ordinal2 (k8\_subset\_1 X0 X1 X2) = X2)))) (\lambda X2 : \iota.X2)) \quad (11)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(X2 = k3\_xboole\_0 X0 X1)\Leftrightarrow(\forall X3.(X3 \in X2)\Leftrightarrow((X3 \in X0)\wedge(X3 \in X1))) \quad (12)$$

Assume the following.

$$\forall X0.((v3\_ordinal1 X0)\wedge(v4\_ordinal1 X0)\wedge(\neg v1\_finset\_1 X0))\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow((v1\_card\_lar X1 X0)\Leftrightarrow(k3\_ordinal2 X1 = X0))) \quad (13)$$

Assume the following.

$$\forall X0.\forall X1.(r1\_tarski X0 X1)\Leftrightarrow(\forall X2.(X2 \in X0)\Rightarrow (X2 \in X1)) \quad (14)$$

Assume the following.

$$\forall X0.k1\_ordinal1 X0 = k2\_xboole\_0 X0 (k1\_tarski X0) \quad (15)$$

Assume the following.

$$\forall X0.\forall X1.k3\_xboole\_0 X0 X1 = k3\_xboole\_0 X1 X0 \quad (16)$$

Assume the following.

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow(\forall X1.(m1\_subset\_1\ X1\ X0)\Rightarrow(v3\_ordinal1\ X1)) \quad (17)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1)\Rightarrow(\neg X1 \in X0) \quad (18)$$

**Theorem 1**

$$\begin{aligned} &\forall X0.((v3\_ordinal1\ X0)\wedge((v4\_ordinal1\ X0)\wedge(\neg v1\_finset\_1 \\ &\quad X0)))\Rightarrow(\forall X1.(v3\_ordinal1\ X1)\Rightarrow(\forall X2.(v3\_ordinal1 \\ &\quad X2)\Rightarrow(\forall X3.(m1\_subset\_1\ X3\ (k1\_zfmisc\_1\ X0))\Rightarrow((r1\_tarski \\ &\quad (k8\_subset\_1\ X0\ X3\ X1)\ X2)\Rightarrow(r1\_tarski\ (k9\_subset\_1\ X0\ X1\ (k2\_card\_lar \\ &\quad X0\ X3))\ (k1\_ordinal1\ X2)))))) \end{aligned}$$