

## t16\_ens\_1

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_ens\_1 : \iota \Rightarrow \iota$  be given. Let  $k7\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ens\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xtuple\_0 : \iota \Rightarrow o$  be given. Let  $k1\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v4\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k1\_ens\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned} \forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1. (m1\_subset\_1 X1 (k2\_ens\_1 \\ X0)) \Rightarrow (X1 = k4\_tarski (k1\_domain\_1 X0 X0 (k3\_ens\_1 X0 X1) (k4\_ens\_1 \\ X0 X1)) (k2\_xtuple\_0 X1))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1\_xboole\_0 X0) \wedge \\ ((\neg v1\_xboole\_0 X1) \wedge ((m1\_subset\_1 X2 X0) \wedge (m1\_subset\_1 X3 X1)))) \Rightarrow \\ (k1\_domain\_1 X0 X1 X2 X3 = k4\_tarski X2 X3) \end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. (v1\_xtuple\_0 X0) \Rightarrow (k4\_tarski (k1\_xtuple\_0 X0) (k2\_xtuple\_0 X0) = X0) \tag{3}$$

Assume the following.

$$\forall X0. \forall X1. k1\_xtuple\_0 (k4\_tarski X0 X1) = X0 \tag{4}$$

Assume the following.

$$\forall X0. \forall X1. v1\_xtuple\_0 (k4\_tarski X0 X1) \tag{5}$$

Assume the following.

$$\forall X0. (\neg v1\_xboole\_0 X0) \Rightarrow ((v4\_funct\_1 (k1\_ens\_1 X0)) \wedge (\neg v1\_xboole\_0 (k1\_ens\_1 X0))) \tag{6}$$

Assume the following.

$$\forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge(\neg v1\_xboole\_0 X1))\Rightarrow (\neg v1\_xboole\_0 (k2\_zfmisc\_1 X0 X1)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.\forall X3.((\neg v1\_xboole\_0 X0)\wedge ((\neg v1\_xboole\_0 X1)\wedge((m1\_subset\_1 X2 X0)\wedge(m1\_subset\_1 X3 X1))))\Rightarrow (m1\_subset\_1 (k1\_domain\_1 X0 X1 X2 X3) (k2\_zfmisc\_1 X0 X1)) \quad (8)$$

Assume the following.

$$\begin{aligned} &\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow \\ &(\forall X2.(m1\_subset\_1 X2 X0)\Rightarrow(k7\_ens\_1 X0 X1 X2 = ReplSep (toset \\ &(\lambda X3 : \iota.m1\_subset\_1 X3 (k1\_ens\_1 X0))) (\lambda X3 : \iota.k1\_domain\_1 \\ &(k2\_zfmisc\_1 X0 X0) (k1\_ens\_1 X0) (k1\_domain\_1 X0 X0 X1 X2) X3 \in k2\_ens\_1 \\ &X0) (\lambda X3 : \iota.k1\_domain\_1 (k2\_zfmisc\_1 X0 X0) (k1\_ens\_1 X0) \\ &(k1\_domain\_1 X0 X0 X1 X2) X3)))) \end{aligned} \quad (9)$$

**Theorem 1**

$$\begin{aligned} &\forall X0.(\neg v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 X0)\Rightarrow \\ &(\forall X2.(m1\_subset\_1 X2 X0)\Rightarrow(\forall X3.(m1\_subset\_1 X3 ( \\ &k2\_ens\_1 X0))\Rightarrow((X3 \in k7\_ens\_1 X0 X1 X2)\Rightarrow(X3 = k4\_tarSKI (k1\_domain\_1 \\ &X0 X0 X1 X2) (k2\_xtuple\_0 X3)))))) \end{aligned}$$