

# t16\_ring\_1 (TMEgvLbB- muoB3aMo59dexRLa7gAoYREHTYB)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v3\_group\_1 : \iota \Rightarrow o$  be given. Let  $v4\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v5\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $l6\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v3\_ideal\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v6\_struct\_0 : \iota \Rightarrow o$  be given. Let  $k2\_ring\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_ring\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v3\_vectsp\_1 : \iota \Rightarrow o$  be given. Let  $k5\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l4\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l4\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l3\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l3\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v36\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k8\_eqrel\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_binop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_rlvect\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u2\_algstr\_0 : \iota \Rightarrow \iota$  be given. Let  $k6\_algstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v6\_vectsp\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v3\_group\_1 \\
& X0) \wedge ((v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge \\
& ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow \\
& (\forall X1. ((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge ((v2\_ideal\_1 \\
& X1 X0) \wedge ((v3\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\
& X0)))))))))) \Rightarrow (\forall X2. (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3. \\
& (m1\_subset\_1 X3 (u1\_struct\_0 X0)) \Rightarrow ((k6\_eqrel\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X2 = k6\_eqrel\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X3) \Leftrightarrow (k5\_algstr\_0 X0 X2 X3 \in \\
& X1))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v3\_vectsp\_1 X0) \wedge (l6\_algstr\_0 \\ X0))) \Rightarrow (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v2\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 \\ X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))) \Rightarrow ((v1\_subset\_1 X1 (u1\_struct\_0 \\ X0)) \Leftrightarrow (\neg k5\_struct\_0 X0 \in X1))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v3\_rlvect\_1 \\ X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l2\_algstr\_0 X0)))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ X1 (u1\_struct\_0 X0)) \Rightarrow (k5\_algstr\_0 X0 X1 (k4\_struct\_0 X0) = X1)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.(l6\_algstr\_0 X0) \Rightarrow ((l2\_algstr\_0 X0) \wedge (l5\_algstr\_0 X0)) \quad (4)$$

Assume the following.

$$\forall X0.(l5\_algstr\_0 X0) \Rightarrow ((l4\_algstr\_0 X0) \wedge (l4\_struct\_0 X0)) \quad (5)$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0) \Rightarrow ((l3\_struct\_0 X0) \wedge (l3\_algstr\_0 X0)) \quad (6)$$

Assume the following.

$$\forall X0.(l2\_algstr\_0 X0) \Rightarrow ((l2\_struct\_0 X0) \wedge (l1\_algstr\_0 X0)) \quad (7)$$

Assume the following.

$$\forall X0.(l3\_struct\_0 X0) \Rightarrow (m1\_subset\_1 (k5\_struct\_0 X0) (u1\_struct\_0 \\ X0)) \quad (8)$$

Assume the following.

$$\forall X0.(l2\_struct\_0 X0) \Rightarrow (m1\_subset\_1 (k4\_struct\_0 X0) (u1\_struct\_0 \\ X0)) \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge \\ ((v3\_group\_1 X0) \wedge ((v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 \\ X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \wedge \\ ((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge ((v2\_ideal\_1 X1 X0) \wedge ( \\ (v3\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 \\ X0)))))))))) \Rightarrow ((v36\_algstr\_0 (k2\_ring\_1 X0 X1)) \wedge (l6\_algstr\_0 ( \\ k2\_ring\_1 X0 X1))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.(l4\_struct\_0 X0) \Rightarrow ((v6\_struct\_0 X0) \Leftrightarrow (k4\_struct\_0 X0 = k5\_struct\_0 X0)) \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow \\ & (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge ((v2\_ideal\_1 X1 X0) \wedge ((v3\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))))))) \Rightarrow (\forall X2.((v36\_algstr\_0 X2) \wedge (l6\_algstr\_0 X2)) \Rightarrow \\ & ((X2 = k2\_ring\_1 X0 X1) \Leftrightarrow ((u1\_struct\_0 X2 = k8\_eqrel\_1 (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1)) \wedge ((k5\_struct\_0 X2 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) (k5\_struct\_0 X0)) \wedge ((k4\_struct\_0 X2 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) (k4\_struct\_0 X0)) \wedge ((\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X2)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X2)) \Rightarrow (\exists X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \wedge (\exists X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \wedge ((X3 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X5) \wedge ((X4 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X6) \wedge (k5\_binop\_1 (u1\_struct\_0 X2) (u1\_algstr\_0 X2) X3 X4 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) (k3\_rlvect\_1 X0 X5 X6)))))))))) \wedge (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 X2)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X2)) \Rightarrow (\exists X5.(m1\_subset\_1 X5 (u1\_struct\_0 X0)) \wedge (\exists X6.(m1\_subset\_1 X6 (u1\_struct\_0 X0)) \wedge ((X3 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X5) \wedge ((X4 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) X6) \wedge (k5\_binop\_1 (u1\_struct\_0 X2) (u2\_algstr\_0 X2) X3 X4 = k6\_eqrel\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0) (k1\_ring\_1 X0 X1) (k6\_algstr\_0 X0 X5 X6)))))))))))))) \quad (12) \end{aligned}$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0) \Rightarrow (((\neg v2\_struct\_0 X0) \wedge (v4\_vectsp\_1 X0)) \Rightarrow ((\neg v2\_struct\_0 X0) \wedge ((v3\_vectsp\_1 X0) \wedge (v6\_vectsp\_1 X0)))) \quad (13)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v3\_group\_1 X0) \wedge ((v4\_vectsp\_1 X0) \wedge ((v5\_vectsp\_1 X0) \wedge ((v2\_rlvect\_1 X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge (l6\_algstr\_0 X0)))))))))) \Rightarrow \\ & (\forall X1.((\neg v1\_xboole\_0 X1) \wedge ((v1\_ideal\_1 X1 X0) \wedge ((v2\_ideal\_1 X1 X0) \wedge ((v3\_ideal\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (u1\_struct\_0 X0)))))))))) \Rightarrow ((v1\_subset\_1 X1 (u1\_struct\_0 X0)) \Leftrightarrow (\neg v6\_struct\_0 (k2\_ring\_1 X0 X1))) \end{aligned}$$