

# t172\_zf\_lang1

(TMdLnv8isw6utzQzQJWEQxhZZeK8kd5hHej)

October 27, 2020

Let  $v1\_zf\_lang : \iota \Rightarrow o$  be given. Let  $m2\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zf\_lang : \iota$  be given. Let  $v5\_zf\_lang : \iota \Rightarrow o$  be given. Let  $k21\_zf\_lang : \iota \Rightarrow \iota$  be given. Let  $k6\_zf\_lang1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k22\_zf\_lang : \iota \Rightarrow \iota$  be given. Let  $k7\_zf\_lang : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $m1\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow ((v5\_zf\_lang X0) \Rightarrow (X0 = k7\_zf\_lang (k21\_zf\_lang X0) (k22\_zf\_lang X0))) \quad (1)$$

Assume the following.

$$\forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (\forall X1. (m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X2. (m2\_subset\_1 X2 k5\_numbers k1\_zf\_lang) \Rightarrow ((v5\_zf\_lang X0) \Leftrightarrow (v5\_zf\_lang (k6\_zf\_lang1 X0 X1 X2)))))) \quad (2)$$

Assume the following.

$$\forall X0.((v1\_zf\_lang X0) \wedge (m2\_finseq\_1 X0 k5\_numbers)) \Rightarrow (\forall X1. ((v1\_zf\_lang X1) \wedge (m2\_finseq\_1 X1 k5\_numbers)) \Rightarrow (\forall X2. ((v1\_zf\_lang X2) \wedge (m2\_finseq\_1 X2 k5\_numbers)) \Rightarrow (\forall X3. ((v1\_zf\_lang X3) \wedge (m2\_finseq\_1 X3 k5\_numbers)) \Rightarrow (\forall X4. (m2\_subset\_1 X4 k5\_numbers k1\_zf\_lang) \Rightarrow (\forall X5. (m2\_subset\_1 X5 k5\_numbers k1\_zf\_lang) \Rightarrow ((k7\_zf\_lang X0 X1 = k6\_zf\_lang1 (k7\_zf\_lang X2 X3) X4 X5) \Leftrightarrow ((X0 = k6\_zf\_lang1 X2 X4 X5) \wedge (X1 = k6\_zf\_lang1 X3 X4 X5)))))))))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. ((\neg v1\_xboole\_0 X0) \wedge ((\neg v1\_xboole\_0 X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0)))) \Rightarrow (\forall X2. (m2\_subset\_1 X2 X0 X1) \Leftrightarrow (m1\_subset\_1 X2 X1)) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(m2\_finseq\_1 X1 X0)\Leftrightarrow(m1\_finseq\_1 X1 X0) \quad (5)$$

Assume the following.

$$\neg v1\_xboole\_0 k1\_zf\_lang \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(((v1\_zf\_lang X0)\wedge(m1\_finseq\_1 \\ X0 k5\_numbers))\wedge((m1\_subset\_1 X1 k1\_zf\_lang)\wedge(m1\_subset\_1 X2 \\ k1\_zf\_lang)))\Rightarrow((v1\_zf\_lang (k6\_zf\_lang1 X0 X1 X2))\wedge(m2\_finseq\_1 \\ (k6\_zf\_lang1 X0 X1 X2) k5\_numbers)) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.((v1\_zf\_lang X0)\wedge(m1\_finseq\_1 X0 k5\_numbers))\Rightarrow((v1\_zf\_lang (k22\_zf\_lang X0))\wedge(m2\_finseq\_1 (k22\_zf\_lang X0) k5\_numbers)) \quad (8)$$

Assume the following.

$$\forall X0.((v1\_zf\_lang X0)\wedge(m1\_finseq\_1 X0 k5\_numbers))\Rightarrow((v1\_zf\_lang (k21\_zf\_lang X0))\wedge(m2\_finseq\_1 (k21\_zf\_lang X0) k5\_numbers)) \quad (9)$$

Assume the following.

$$m1\_subset\_1 k1\_zf\_lang (k1\_zfmisc\_1 k5\_numbers) \quad (10)$$

Assume the following.

$$\forall X0.(v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))\Rightarrow(v1\_xboole\_0 X1)) \quad (11)$$

**Theorem 1**

$$\begin{aligned} \forall X0.((v1\_zf\_lang X0)\wedge(m2\_finseq\_1 X0 k5\_numbers))\Rightarrow(\forall X1. \\ (m2\_subset\_1 X1 k5\_numbers k1\_zf\_lang)\Rightarrow(\forall X2.(m2\_subset\_1 \\ X2 k5\_numbers k1\_zf\_lang)\Rightarrow((v5\_zf\_lang X0)\Rightarrow((k21\_zf\_lang (k6\_zf\_lang1 \\ X0 X1 X2) = k6\_zf\_lang1 (k21\_zf\_lang X0) X1 X2)\wedge(k22\_zf\_lang (k6\_zf\_lang1 \\ X0 X1 X2) = k6\_zf\_lang1 (k22\_zf\_lang X0) X1 X2)))))) \end{aligned}$$