# t175_member_1 <br> (TMcBem6oDfcALVERiqcBF3eVQiSgpXeq9RH) 

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Let $v 2 \_$membered : $\iota \Rightarrow o$ be given. Let $v 1 \_x r e a l \_0: ~ \iota \Rightarrow o$ be given. Let $k 20 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5 \_$xboole_ $0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_m e m b e r \_1: \iota \Rightarrow \iota$ be given. Let $v 1 \_x x r e a l \_0: \iota \Rightarrow o$ be given. Let $k 18 \_m e m b e r \_1$ : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_ \text {_membered } X 1\right) \Rightarrow\left(k 4 \_m e m b e r \_1\right.\right. \\
\left(k 5 \_x b o o l e \_0 X 0 X 1\right)=k 5 \_x b o o l e \_0\left(k 4 \_m e m b e r \_1 X 0\right)\left(k 4 \_m e m b e r \_1\right. \\
X 1))) \tag{1}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x x r e a l \_0 X 1\right) \Rightarrow\left(k 20 \_m e m b e r \_1\right.\right.  \tag{2}\\
\left.\left.X 0 X 1=k 4 \_m e m b e r \_1\left(k 18 \_m e m b e r \_1 X 0 X 1\right)\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 2 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d X 1\right) \Rightarrow(\forall X 2 .\right. \\
\left(v 1 \_x r e a l \_0 X 2\right) \Rightarrow\left(k 18 \_m e m b e r \_1(k 5 \text { _xboole_0 X0 X1) X2=k5_xboole_0}\right. \\
\left.\left.\left.\left(k 18 \_m e m b e r \_1 X 0 X 2\right)\left(k 18 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right) \tag{3}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_ \text {membered } X 0\right) \wedge\left(v 1 \_x x r e a l \_0 X 1\right)\right) \Rightarrow(  \tag{4}\\
\left.v 2 \_ \text {membered }\left(k 18 \_m e m b e r \_1 X 0 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 2 \_m e m b e r e d X 0\right) \wedge\left(v 2 \_ \text {membered } X 1\right)\right) \Rightarrow(  \tag{5}\\
\left.v 2 \_m e m b e r e d ~\left(k 5 \_x b o o l e \_0 X 0 X 1\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 5 \_x b o o l e \_0 X 0 X 1=k 5 \_x b o o l e \_0 X 1 X 0 \tag{6}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x r e a l \_0 X 0\right) \Rightarrow\left(v 1 \_x x r e a l \_0 X 0\right) \tag{7}
\end{equation*}
$$

## Theorem 1

$\forall X 0 .\left(v 2 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 2 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.

(k20_member_1 X0 X2) (k20_member_1 X1 X2))))

