# t179_member_1 <br> (TMXjJ9m5rARJtKwtDYPsCVig4miMJpKtnqU) 

October 27, 2020

Let $v 1 \_$membered : $\iota \Rightarrow 0$ be given. Let $v 1 \_x c m p l x \_0: ~ \iota \Rightarrow O$ be given. Let r1_tarski : $\iota \Rightarrow \iota \Rightarrow 0$ be given. Let k21_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k19_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let k5_member_1 : $\iota \Rightarrow \iota$ be given. Let $k 9 \_$member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1_{\_}$tarski $: \iota \Rightarrow \iota$ be given. Let $v 1 \_x b o o l e \_0$ : $\iota \Rightarrow o$ be given. Let $k$ 11_member_1: $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(\left(r 1 \_t a r s k i X 0 X 1\right) \Leftrightarrow\left(r 1 \_t a r s k i \quad\left(k 19 \_m e m b e r \_1\right.\right.\right.$
X0 X2) (k19_member_1 X1 X2)))))
Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(( \right. \\
\left.r 1 \_t a r s k i X 0 X 1\right) \Leftrightarrow\left(r 1 \_t a r s k i\right.  \tag{2}\\
\left.\left.\left.\left(k 5 \_m e m b e r \_1 X 0\right)\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right)\right)
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1\right.$. $\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 5 \_m e m b e r \_1\right.$ $\left(k 9 \_m e m b e r \_1 X 0 X 1\right)=k 9 \_m e m b e r \_1$ ( $\left.k 5 \_m e m b e r \_1 X 0\right) ~\left(k 5 \_m e m b e r \_1\right.$ X1)))

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(k 5 \_m e m b e r \_1\left(k 5 \_m e m b e r \_1 X 0\right)=X 0\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d \quad X 0\right) \wedge\left(v 1 \_x c m p l x \_0 X 1\right)\right) \Rightarrow( \\
\left.v 1 \_m e m b e r e d\left(k 21 \_m e m b e r \_1 X 0 X 1\right)\right) \tag{5}
\end{gather*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{6}
\end{equation*}
$$

Assume the following.
$\forall X 0 .\left(\left(\neg v 1 \_x b o o l e \_0 X 0\right) \wedge\left(v 1 \_m e m b e r e d \quad X 0\right)\right) \Rightarrow\left(\left(\neg v 1 \_x b o o l e \_0\right.\right.$
$\left.\left.\left.\left(k 5 \_m e m b e r \_1 X 0\right)\right) \wedge\left(v 1 \_m e m b e r e d\right)\left(k 5 \_m e m b e r \_1 X 0\right)\right)\right)$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \neg v 1 \_x b o o l e \_0\left(k 1 \_t a r s k i \quad X 0\right) \tag{8}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 11 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 9 \_m e m b e r \_1 X 0\left(k 5 \_m e m b e r \_1 X 1\right)\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 21 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 11 \_m e m b e r \_1 X 0\left(k 1 \_t a r s k i X 1\right)\right)\right) \tag{10}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 19 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 11 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{11}
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d ~ X 0\right) \wedge\left(v 1 \_m e m b e r e d ~ X 1\right)\right) \Rightarrow( \\
\left.k 9 \_m e m b e r \_1 X 0 X 1=k 9 \_m e m b e r \_1 X 1 X 0\right) \tag{12}
\end{gather*}
$$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(\left(r 1 \_t a r s k i \quad X 0 X 1\right) \Leftrightarrow\left(r 1 \_t a r s k i\left(k 21 \_m e m b e r \_1\right.\right.\right.$
X0 X2) (k21_member_1 X1 X2)))))

