

t17\_afinsq\_1  
 (TMcj6e8Zq154azajhZ9VZ1u9y3QTsUUA1cK)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k1\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_ordinal4 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_nat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k2\_afinsq\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_afinsq\_1 X0 = k1\_card\_1 X0) \quad (1)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (k1\_card\_1 X0 = k9\_xtuple\_0 X0) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. (((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 X0) \wedge (v1\_finset\_1 X0)))) \wedge ((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finset\_1 X1))))) \Rightarrow ((v1\_relat\_1 (k1\_ordinal4 X0 X1)) \wedge ((v5\_ordinal1 (k1\_ordinal4 X0 X1)) \wedge ((v1\_funct\_1 (k1\_ordinal4 X0 X1)) \wedge (v1\_finset\_1 (k1\_ordinal4 X0 X1))))) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. (((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge (v1\_funct\_1 X0))) \wedge ((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 X1) \wedge (v1\_funct\_1 X1)))) \Rightarrow ((v1\_relat\_1 (k1\_ordinal4 X0 X1)) \wedge ((v5\_ordinal1 (k1\_ordinal4 X0 X1)) \wedge (v1\_funct\_1 (k1\_ordinal4 X0 X1)))) \quad (4)$$

Assume the following.

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 \\
& X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 \\
& X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finset\_1 X1)))) \Rightarrow (\forall X2.((v1\_relat\_1 \\
& X2) \wedge ((v5\_ordinal1 X2) \wedge (v1\_funct\_1 X2)))) \Rightarrow ((X2 = k1\_ordinal4 X0 \\
& X1) \Leftrightarrow ((k9\_xtuple\_0 X2 = k2\_nat\_1 (k1\_afinsq\_1 X0) (k1\_afinsq\_1 \\
& X1)) \wedge ((\forall X3.(v7\_ordinal1 X3) \Rightarrow ((X3 \in k2\_afinsq\_1 X0) \Rightarrow (k1\_funct\_1 \\
& X2 X3 = k1\_funct\_1 X0 X3))) \wedge (\forall X3.(v7\_ordinal1 X3) \Rightarrow ((X3 \in \\
& k2\_afinsq\_1 X1) \Rightarrow (k1\_funct\_1 X2 (k2\_nat\_1 (k1\_afinsq\_1 X0) X3) = \\
& k1\_funct\_1 X1 X3)))))))))
\end{aligned} \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((v1\_relat\_1 X0) \wedge ((v5\_ordinal1 X0) \wedge ((v1\_funct\_1 \\
& X0) \wedge (v1\_finset\_1 X0)))) \Rightarrow (\forall X1.((v1\_relat\_1 X1) \wedge ((v5\_ordinal1 \\
& X1) \wedge ((v1\_funct\_1 X1) \wedge (v1\_finset\_1 X1)))) \Rightarrow (k1\_afinsq\_1 (k1\_ordinal4 \\
& X0 X1) = k2\_nat\_1 (k1\_afinsq\_1 X0) (k1\_afinsq\_1 X1)))
\end{aligned}$$