

## t17\_scmfsa\_2

(TMFcLFb7CvkUGmaZCrf7i3KY4bbqxskzHNz)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_compos\_1 : \iota \Rightarrow \iota$  be given. Let  $k1\_ami\_3 : \iota$  be given. Let  $k1\_scmfsa\_2 : \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_compos\_0 : \iota \Rightarrow o$  be given. Let  $v2\_compos\_0 : \iota \Rightarrow o$  be given. Let  $v3\_compos\_0 : \iota \Rightarrow o$  be given. Let  $v5\_compos\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_card\_3 : \iota \Rightarrow \iota$  be given. Let  $k3\_relat\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $g1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_scm\_inst : \iota$  be given. Let  $k2\_scmfsa\_i : \iota$  be given. Let  $k9\_ami\_2 : \iota$  be given. Let  $k3\_ami\_2 : \iota$  be given. Let  $k4\_ami\_2 : \iota$  be given. Let  $k5\_scmfsa\_1 : \iota$  be given. Let  $np\_3 : \iota$  be given. Let  $k4\_scmfsa\_1 : \iota$  be given. Let  $k1\_scmfsa\_1 : \iota$  be given. Let  $np\_2 : \iota$  be given. Let  $k1\_ami\_2 : \iota$  be given. Let  $v1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funct\_7 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_scmfsa\_1 : \iota$  be given. Let  $k2\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $k7\_card\_1 : \iota \Rightarrow \iota$  be given. Let  $np\_13 : \iota$  be given. Let  $k2\_scm\_inst : \iota$  be given. Let  $k1\_scmfsa\_i : \iota$  be given. Let  $k3\_xtuple\_0 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $k11\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_9 : \iota$  be given. Let  $np\_10 : \iota$  be given. Let  $k10\_finseq\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_11 : \iota$  be given. Let  $np\_12 : \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u2\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $u1\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u2\_memstr\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_extpro\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (2)$$

Assume the following.

$$\begin{aligned}
& \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.\forall X5. \\
& \forall X6.((m1\_subset\_1 X2 X1)\wedge(((v1\_compos\_0 X3)\wedge((v2\_compos\_0 \\
& X3)\wedge((v3\_compos\_0 X3)\wedge(v5\_compos\_0 X3))))\wedge(((v1\_funct\_1 X4)\wedge \\
& ((v1\_funct\_2 X4 X1 X0)\wedge(m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\
& X1 X0))))\wedge(((v1\_relat\_1 X5)\wedge((v4\_relat\_1 X5 X0)\wedge((v1\_funct\_1 \\
& X5)\wedge(v1\_partfun1 X5 X0))))\wedge((v1\_funct\_1 X6)\wedge((v1\_funct\_2 X6 \\
& X3 (k1\_funct\_2 (k4\_card\_3 (k3\_relat\_1 X4 X5)) (k4\_card\_3 (k3\_relat\_1 \\
& X4 X5))))\wedge(m1\_subset\_1 X6 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X3 (k1\_funct\_2 \\
& (k4\_card\_3 (k3\_relat\_1 X4 X5)) (k4\_card\_3 (k3\_relat\_1 X4 X5))))))))))\Rightarrow \\
& (\forall X7.\forall X8.\forall X9.\forall X10.\forall X11.\forall X12. \\
& \forall X13.(g1\_extpro\_1 X0 X1 X2 X3 X4 X5 X6 = g1\_extpro\_1 X7 X8 X9 \\
& X10 X11 X12 X13)\Rightarrow((X0 = X7)\wedge((X1 = X8)\wedge((X2 = X9)\wedge((X3 = X10)\wedge((X4 = \\
& X11)\wedge((X5 = X12)\wedge(X6 = X13))))))))))
\end{aligned} \tag{3}$$

Assume the following.

$$(\neg v1\_xboole\_0 k3\_scm\_inst)\wedge(v5\_compos\_0 k3\_scm\_inst) \tag{4}$$

Assume the following.

$$(\neg v1\_xboole\_0 k2\_scmfsa\_i)\wedge(v5\_compos\_0 k2\_scmfsa\_i) \tag{5}$$

Assume the following.

$$(\neg v1\_xboole\_0 k3\_scm\_inst)\wedge(v3\_compos\_0 k3\_scm\_inst) \tag{6}$$

Assume the following.

$$(\neg v1\_xboole\_0 k2\_scmfsa\_i)\wedge(v3\_compos\_0 k2\_scmfsa\_i) \tag{7}$$

Assume the following.

$$(\neg v1\_xboole\_0 k3\_scm\_inst)\wedge(v2\_compos\_0 k3\_scm\_inst) \tag{8}$$

Assume the following.

$$(\neg v1\_xboole\_0 k2\_scmfsa\_i)\wedge(v2\_compos\_0 k2\_scmfsa\_i) \tag{9}$$

Assume the following.

$$(\neg v1\_xboole\_0 k3\_scm\_inst)\wedge(v1\_compos\_0 k3\_scm\_inst) \tag{10}$$

Assume the following.

$$(\neg v1\_xboole\_0 k2\_scmfsa\_i)\wedge(v1\_compos\_0 k2\_scmfsa\_i) \tag{11}$$

Assume the following.

$$(v1\_funct\_1 k9\_ami\_2) \wedge ((v1\_funct\_2 k9\_ami\_2 k3\_scm\_inst (k1\_funct\_2 (k4\_card\_3 (k3\_relat\_1 k3\_ami\_2 k4\_ami\_2)) (k4\_card\_3 (k3\_relat\_1 k3\_ami\_2 k4\_ami\_2)))) \wedge (m1\_subset\_1 k9\_ami\_2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k3\_scm\_inst (k1\_funct\_2 (k4\_card\_3 (k3\_relat\_1 k3\_ami\_2 k4\_ami\_2)) (k4\_card\_3 (k3\_relat\_1 k3\_ami\_2 k4\_ami\_2))))))) \quad (12)$$

Assume the following.

$$(v1\_relat\_1 k5\_scmfsa\_1) \wedge ((v4\_relat\_1 k5\_scmfsa\_1 np\_3) \wedge (v1\_funct\_1 k5\_scmfsa\_1) \wedge (v1\_partfun1 k5\_scmfsa\_1 np\_3)) \quad (13)$$

Assume the following.

$$(v1\_funct\_1 k4\_scmfsa\_1) \wedge ((v1\_funct\_2 k4\_scmfsa\_1 k1\_scmfsa\_1 np\_3) \wedge (m1\_subset\_1 k4\_scmfsa\_1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k1\_scmfsa\_1 np\_3)))) \quad (14)$$

Assume the following.

$$(v1\_relat\_1 k4\_ami\_2) \wedge ((v4\_relat\_1 k4\_ami\_2 np\_2) \wedge ((v1\_funct\_1 k4\_ami\_2) \wedge (v1\_partfun1 k4\_ami\_2 np\_2))) \quad (15)$$

Assume the following.

$$(v1\_funct\_1 k3\_ami\_2) \wedge ((v1\_funct\_2 k3\_ami\_2 k1\_ami\_2 np\_2) \wedge (m1\_subset\_1 k3\_ami\_2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k1\_ami\_2 np\_2)))) \quad (16)$$

Assume the following.

$$(v1\_extpro\_1 k1\_scmfsa\_2 np\_3) \wedge (l1\_extpro\_1 k1\_scmfsa\_2 np\_3) \quad (17)$$

Assume the following.

$$\forall X0. \forall X1. m1\_subset\_1 (k1\_funct\_7 X0 X1) X1 \quad (18)$$

Assume the following.

$$(v1\_extpro\_1 k1\_ami\_3 np\_2) \wedge (l1\_extpro\_1 k1\_ami\_3 np\_2) \quad (19)$$

Assume the following.

$$(v1\_funct\_1 k12\_scmfsa\_1) \wedge ((v1\_funct\_2 k12\_scmfsa\_1 k2\_scmfsa\_i (k1\_funct\_2 (k4\_card\_3 (k3\_relat\_1 k4\_scmfsa\_1 k5\_scmfsa\_1)) (k4\_card\_3 (k3\_relat\_1 k4\_scmfsa\_1 k5\_scmfsa\_1)))) \wedge (m1\_subset\_1 k12\_scmfsa\_1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k2\_scmfsa\_i (k1\_funct\_2 (k4\_card\_3 (k3\_relat\_1 k4\_scmfsa\_1 k5\_scmfsa\_1)) (k4\_card\_3 (k3\_relat\_1 k4\_scmfsa\_1 k5\_scmfsa\_1))))))) \quad (20)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(X2 = k2\_xboole\_0 X0 X1) \Leftrightarrow (\forall X3. \\ (X3 \in X2) \Leftrightarrow ((X3 \in X0) \vee (X3 \in X1))) \end{aligned} \quad (21)$$

Assume the following.

$$\begin{aligned} k2\_scmf\_sa\_i = k2\_xboole\_0 (k2\_xboole\_0 k3\_scm\_inst (ReplSep4 \\ (toset (\lambda X0 : \iota.m2\_subset\_1 X0 k4\_ordinal1 (k7\_card\_1 np\_13))) \\ (\lambda X0 : \iota.toset (\lambda X1 : \iota.m1\_subset\_1 X1 k2\_scm\_inst)) \\ (\lambda X0 : \iota.\lambda X1 : \iota.toset (\lambda X2 : \iota.m1\_subset\_1 X2 k2\_scm\_inst)) \\ (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \iota.toset (\lambda X3 : \iota.m1\_subset\_1 \\ X3 k1\_scmf\_sa\_i)) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \iota.\lambda X3 : \\ \iota.X0 \in k2\_tarski np\_9 np\_10) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \\ \iota.\lambda X3 : \iota.k3\_xtuple\_0 X0 k1\_xboole\_0 (k11\_finseq\_1 X1 X3 \\ X2)))) (ReplSep3 (toset (\lambda X0 : \iota.m2\_subset\_1 X0 k4\_ordinal1 \\ (k7\_card\_1 np\_13))) (\lambda X0 : \iota.toset (\lambda X1 : \iota.m1\_subset\_1 \\ X1 k2\_scm\_inst)) (\lambda X0 : \iota.\lambda X1 : \iota.toset (\lambda X2 : \iota. \\ m1\_subset\_1 X2 k1\_scmf\_sa\_i)) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \iota. \\ \iota.X0 \in k2\_tarski np\_11 np\_12) (\lambda X0 : \iota.\lambda X1 : \iota.\lambda X2 : \\ \iota.k3\_xtuple\_0 X0 k1\_xboole\_0 (k10\_finseq\_1 X1 X2)))) \end{aligned} \quad (22)$$

Assume the following.

$$\begin{aligned} k1\_scmf\_sa\_2 = g1\_extpro\_1 np\_3 k1\_scmf\_sa\_1 (k1\_funct\_7 k5\_numbers \\ k1\_scmf\_sa\_1) k2\_scmf\_sa\_i k4\_scmf\_sa\_1 k5\_scmf\_sa\_1 k12\_scmf\_sa\_1 \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} k1\_ami\_3 = g1\_extpro\_1 np\_2 k1\_ami\_2 (k1\_funct\_7 k5\_numbers k1\_ami\_2) \\ k3\_scm\_inst k3\_ami\_2 k4\_ami\_2 k9\_ami\_2 \end{aligned} \quad (24)$$

Assume the following.

$$\forall X0.\forall X1.k2\_xboole\_0 X0 X1 = k2\_xboole\_0 X1 X0 \quad (25)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.(l1\_extpro\_1 X1 X0) \Rightarrow ((v1\_extpro\_1 X1 X0) \Rightarrow \\ (X1 = g1\_extpro\_1 X0 (u1\_struct\_0 X1) (u2\_struct\_0 X1) (u1\_compos\_1 \\ X1) (u1\_memstr\_0 X0 X1) (u2\_memstr\_0 X0 X1) (u1\_extpro\_1 X0 X1))) \end{aligned} \quad (26)$$

### Theorem 1

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 (u1\_compos\_1 k1\_ami\_3)) \Rightarrow (m1\_subset\_1 \\ X0 (u1\_compos\_1 k1\_scmf\_sa\_2)) \end{aligned}$$