

## t17\_topalg\_5

(TMYjxmxv6pC2bsmgF2Ha677KvWWxHUQDKAk)

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Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_connsp\_2 : \iota \Rightarrow o$  be given. Let  $k4\_topmetr : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $v1\_cantor\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_tops\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_topmetr : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_numbers : \iota$  be given. Let  $k9\_metric\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_real\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k6\_numbers : \iota$  be given. Let  $k3\_card\_3 : \iota \Rightarrow \iota$  be given. Let  $v2\_connsp\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_topc : \iota \Rightarrow o$  be given. Let  $l1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $m1\_pre\_topc : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_pre\_topc : \iota \Rightarrow o$  be given. Let  $k3\_topmetr : \iota$  be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. ((X0 \in X1) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 X2))) \Rightarrow (m1\_subset\_1 X0 X2) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. (v1\_xreal\_0 X0) \Rightarrow (\forall X1. (v1\_xreal\_0 X1) \Rightarrow (\neg(r1\_xxreal\_0 \\ & X0 X1) \wedge (\forall X2. ((v1\_cantor\_1 X2 (k4\_topmetr X0 X1)) \wedge ((v1\_tops\_2 \\ & X2 (k4\_topmetr X0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k1\_zfmisc\_1 \\ & (u1\_struct\_0 (k4\_topmetr X0 X1)))))))) \Rightarrow (\neg(\exists X3. ((v1\_relat\_1 \\ & X3) \wedge ((v4\_relat\_1 X3 (u1\_struct\_0 (k4\_topmetr X0 X1))) \wedge ((v1\_funct\_1 \\ & X3) \wedge (v1\_partfun1 X3 (u1\_struct\_0 (k4\_topmetr X0 X1)))))) \wedge (\forall X4. \\ & (m1\_subset\_1 X4 (u1\_struct\_0 (k2\_topmetr X0 X1))) \Rightarrow ((k1\_funct\_1 \\ & X3 X4 = ReplSep (toSet (\lambda X5 : \iota. m1\_subset\_1 X5 k5\_numbers)) \\ & (\lambda X5 : \iota. X5 \neq k6\_numbers) (\lambda X5 : \iota. k9\_metric\_1 (k2\_topmetr \\ & X0 X1) X4 (k10\_real\_1 np\_1 X5)))) \wedge (X2 = k3\_card\_3 X3)))) \wedge (\forall X3. \\ & (m1\_subset\_1 X3 (k1\_zfmisc\_1 (u1\_struct\_0 (k4\_topmetr X0 X1)))) \Rightarrow \\ & ((X3 \in X2) \Rightarrow (v2\_connsp\_1 X3 (k4\_topmetr X0 X1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v2\_pre\_topc X0) \wedge (l1\_pre\_topc \\ X0))) \Rightarrow ((\exists X1.((v1\_cantor\_1 X1 X0) \wedge ((v1\_tops\_2 X1 X0) \wedge ( \\ m1\_subset\_1 X1 (k1\_zfmisc\_1 (k1\_zfmisc\_1 (u1\_struct\_0 X0))))))) \wedge \\ (\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (u1\_struct\_0 X0))) \Rightarrow \\ ((X2 \in X1) \Rightarrow (v2\_connsp\_1 X2 X0))) \Rightarrow (v1\_connsp\_2 X0)) \end{aligned} \quad (3)$$

Assume the following.

$$\forall X0.(l1\_pre\_topc X0) \Rightarrow (\forall X1.(m1\_pre\_topc X1 X0) \Rightarrow (l1\_pre\_topc X1)) \quad (4)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v1\_xreal\_0 X0) \wedge (v1\_xreal\_0 X1)) \Rightarrow ((\neg \\ v2\_struct\_0 (k4\_topmetr X0 X1)) \wedge ((v1\_pre\_topc (k4\_topmetr X0 \\ X1)) \wedge (m1\_pre\_topc (k4\_topmetr X0 X1) k3\_topmetr))) \end{aligned} \quad (5)$$

Assume the following.

$$(v2\_pre\_topc k3\_topmetr) \wedge (l1\_pre\_topc k3\_topmetr) \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.((v2\_pre\_topc X0) \wedge (l1\_pre\_topc X0)) \Rightarrow (\forall X1. \\ (m1\_pre\_topc X1 X0) \Rightarrow (v2\_pre\_topc X1)) \end{aligned} \quad (7)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(v1\_xreal\_0 X1) \Rightarrow ((r1\_xxreal\_0 \\ X0 X1) \Rightarrow (v1\_connsp\_2 (k4\_topmetr X0 X1)))) \end{aligned}$$