

# t17\_topreal9

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October 27, 2020

Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $v1\_xreal\_0 : \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k15\_euclid : \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_topreal9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_topreal9 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v7\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k14\_euclid : \iota \Rightarrow \iota$  be given. Let  $k11\_metric\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_metric\_1 : \iota \Rightarrow o$  be given. Let  $k10\_metric\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ordinal1 : \iota$  be given. Let  $v6\_membered : \iota \Rightarrow o$  be given. Let  $v1\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v6\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v7\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v8\_metric\_1 : \iota \Rightarrow o$  be given. Let  $v9\_metric\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0.(v7\_ordinal1 X0) \Rightarrow (u1\_struct\_0 (k15\_euclid X0) = u1\_struct\_0 (k14\_euclid X0)) \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k5\_numbers) \Rightarrow (\forall X1.(v1\_xreal\_0 \\ X1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 (k15\_euclid X0))) \Rightarrow \\ (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 (k14\_euclid X0))) \Rightarrow ( \\ (X2 = X3) \Rightarrow (k11\_metric\_1 (k14\_euclid X0) X3 X1 = k3\_topreal9 X0 X2 \\ X1)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\forall X0.(v1\_xreal\_0 X0) \Rightarrow (\forall X1.(l1\_metric\_1 X1) \Rightarrow (\forall X2. \\ (m1\_subset\_1 X2 (u1\_struct\_0 X1)) \Rightarrow (r1\_tarski (k11\_metric\_1 X1 \\ X2 X0) (k10\_metric\_1 X1 X2 X0)))) \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.(m1\_subset\_1 X0 k5\_numbers) \Rightarrow (\forall X1.(v1\_xreal\_0 \\ X1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 (k15\_euclid X0))) \Rightarrow \\ (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 (k14\_euclid X0))) \Rightarrow ( \\ (X2 = X3) \Rightarrow (k10\_metric\_1 (k14\_euclid X0) X3 X1 = k2\_topreal9 X0 X2 \\ X1)))))) \end{aligned} \quad (4)$$

Assume the following.

$$k5\_numbers = k4\_ordinal1 \quad (5)$$

Assume the following.

$$v6\_membered\ k4\_ordinal1 \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0.(v7\_ordinal1\ X0) \Rightarrow & ((v1\_metric\_1\ (k14\_euclid\ X0)) \wedge \\ & ((v6\_metric\_1\ (k14\_euclid\ X0)) \wedge (v7\_metric\_1\ (k14\_euclid\ X0)) \wedge \\ & ((v8\_metric\_1\ (k14\_euclid\ X0)) \wedge (v9\_metric\_1\ (k14\_euclid\ X0)) \wedge \\ & (l1\_metric\_1\ (k14\_euclid\ X0)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.(v6\_membered\ X0) \Rightarrow (\forall X1.(m1\_subset\_1\ X1\ X0) \Rightarrow (v7\_ordinal1\ X1)) \quad (8)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(m1\_subset\_1\ X0\ k5\_numbers) \Rightarrow & (\forall X1.(v1\_xreal\_0 \\ & X1) \Rightarrow (\forall X2.(m1\_subset\_1\ X2\ (u1\_struct\_0\ (k15\_euclid\ X0))) \Rightarrow \\ & (r1\_tarski\ (k3\_topreal9\ X0\ X2\ X1)\ (k2\_topreal9\ X0\ X2\ X1)))) \end{aligned}$$