## t184_member_1 <br> (TMGDgiWQL5txoP8Sevhkdx3ZoHkUHxJ7m9t)

October 27, 2020

Let $v 1 \_$membered $: \iota \Rightarrow o$ be given. Let $v 1 \_x c m p l x \_0: \iota \Rightarrow O$ be given. Let $k 21 \_m e m b e r \_1: ~ \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6_{-}$subset_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 5 \_m e m b e r \_1: ~ \iota \Rightarrow \iota$ be given. Let k19_member_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_x b o o l e \_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_ \text {membered } X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 21 \_m e m b e r \_1\right.\right.  \tag{1}\\
\left.\left.X 0 X 1=k 5 \_m e m b e r \_1\left(k 19 \_m e m b e r \_1 X 0 X 1\right)\right)\right)
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 5 \_m e m b e r \_1\right.\right.$
$\left(k 6 \_s u b s e t \_1 X 0 X 1\right)=k 6 \_s u b s e t \_1\left(k 5 \_m e m b e r \_1 X 0\right)\left(k 5 \_m e m b e r \_1\right.$
$X 1)))$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 19 \_m e m b e r \_1\left(k 6 \_s u b s e t \_1 X 0 X 1\right) X 2=k 6 \_s u b s e t \_1\right.$
$\left.\left.\left.\left(k 19 \_m e m b e r \_1 X 0 X 2\right)\left(k 19 \_m e m b e r \_1 X 1 X 2\right)\right)\right)\right)$

Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 6 \_ \text {subset_1 } X 0 X 1=k 4 \_x b o o l e \_0 X 0 X 1 \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(\left(v 1 \_m e m b e r e d ~ X 0\right) \wedge\left(v 1 \_x c m p l x \_0 X 1\right)\right) \Rightarrow( \\
\left.v 1 \_ \text {membered }\left(k 19 \_m e m b e r \_1 X 0 X 1\right)\right) \tag{5}
\end{gather*}
$$

Assume the following.
$\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d ~\left(k 4 \_x b o o l e \_0\right.\right.$
$X 0 X 1))$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d \quad X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(k 21 \_m e m b e r \_1\right.$ ( $k 6 \_$subset_1 X0 X1) X2 $=k 6 \_s u b s e t \_1$ (k21_member_1 X0 X2) (k21_member_1 X1 X2))))

