

t189\_xxreal\_1 (TM-  
SiG9B1MM9Z2TukT7oFs8T9T4A8yZUi6fM)

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Let  $v1\_xxreal\_0 : \iota \Rightarrow o$  be given. Let  $r1\_xxreal\_0 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xxreal\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xxreal\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xboole\_0 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v2\_membered : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k7\_numbers : \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow ((X0 \in k4\_xxreal\_1 X1 X2) \Leftrightarrow ((\neg r1\_xxreal\_0 X0 X1) \wedge \\ & (\neg r1\_xxreal\_0 X2 X0)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow ((X0 \in k2\_xxreal\_1 X1 X2) \Leftrightarrow ((r1\_xxreal\_0 X1 X0) \wedge \\ & (\neg r1\_xxreal\_0 X2 X0)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xxreal\_0 X0) \Rightarrow (\forall X1.(v1\_xxreal\_0 X1) \Rightarrow (\forall X2. \\ & (v1\_xxreal\_0 X2) \Rightarrow (((r1\_xxreal\_0 X0 X1) \wedge (r1\_xxreal\_0 X1 X2)) \Rightarrow \\ & (r1\_xxreal\_0 X0 X2)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\forall X0.\forall X1.k6\_subset\_1 X0 X1 = k4\_xboole\_0 X0 X1 \tag{4}$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0 X0) \wedge (v1\_xxreal\_0 X1)) \Rightarrow (v2\_membered (k4\_xxreal\_1 X0 X1)) \tag{5}$$

Assume the following.

$$\forall X0.\forall X1.(v2\_membered X0) \Rightarrow (v2\_membered (k4\_xboole\_0 X0 X1)) \tag{6}$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xxreal\_0 X0)\wedge(v1\_xxreal\_0 X1))\Rightarrow(v2\_membered (k2\_xxreal\_1 X0 X1)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.(X2 = k4\_xboole\_0 X0 X1)\Leftrightarrow(\forall X3.(X3 \in X2)\Leftrightarrow((X3 \in X0)\wedge(\neg X3 \in X1))) \quad (8)$$

Assume the following.

$$\begin{aligned} \forall X0.(v1\_xxreal\_0 X0)\Rightarrow(\forall X1.(v1\_xxreal\_0 X1)\Rightarrow(k4\_xxreal\_1 \\ X0 X1 = ReplSep (toset (\lambda X2 : \iota.m1\_subset\_1 X2 k7\_numbers)) \\ (\lambda X2 : \iota.(\neg r1\_xxreal\_0 X2 X0)\wedge(\neg r1\_xxreal\_0 X1 X2)) (\lambda X2 : \\ \iota.X2)))) \quad (9) \end{aligned}$$

Assume the following.

$$\forall X0.(v2\_membered X0)\Rightarrow(\forall X1.(v2\_membered X1)\Rightarrow((X0 = X1)\Leftrightarrow(\forall X2.(v1\_xxreal\_0 X2)\Rightarrow((X2 \in X0)\Leftrightarrow(X2 \in X1)))))) \quad (10)$$

**Theorem 1**

$$\begin{aligned} \forall X0.(v1\_xxreal\_0 X0)\Rightarrow(\forall X1.(v1\_xxreal\_0 X1)\Rightarrow(\forall X2. \\ (v1\_xxreal\_0 X2)\Rightarrow((\neg r1\_xxreal\_0 X1 X0)\Rightarrow(k6\_subset\_1 (k4\_xxreal\_1 \\ X0 X2) (k4\_xxreal\_1 X0 X1) = k2\_xxreal\_1 X1 X2)))))) \end{aligned}$$