

t18_anproj_2
(TML7neJuwvUjHfXgn6JyVav6wFuPbogSjY6)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_numbers : \iota$ be given. Let $k9_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_funcsdom : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_funcsdom : \iota \Rightarrow \iota$ be given. Let $k2_funcsdom : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k7_funcsdom : \iota \Rightarrow \iota$ be given. Let $k1_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8_funcsdom : \iota \Rightarrow \iota$ be given. Let $k6_numbers : \iota$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given.

Let $np_{-1} : \iota$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned}
& \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (m2_funct_2 X1 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X2. (m2_funct_2 X2 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X3. (m2_funct_2 X3 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X4. (m2_funct_2 X4 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X5. (m1_subset_1 X5 X0) \Rightarrow \\
& (\forall X6. (m1_subset_1 X6 X0) \Rightarrow (\forall X7. (m1_subset_1 X7 X0) \Rightarrow \\
& (\forall X8. (m1_subset_1 X8 X0) \Rightarrow (((k3_funct_2 X0 k1_numbers X1 \\
& X5 = np_{-1}) \wedge ((\forall X9. (X9 \in X0) \Rightarrow ((X9 = X5) \vee (k1_funct_1 X1 X9 = \\
& k6_numbers))) \wedge ((k3_funct_2 X0 k1_numbers X2 X6 = np_{-1}) \wedge ((\forall X9. \\
& (X9 \in X0) \Rightarrow ((X9 = X6) \vee (k1_funct_1 X2 X9 = k6_numbers))) \wedge ((k3_funct_2 \\
& X0 k1_numbers X3 X7 = np_{-1}) \wedge ((\forall X9. (X9 \in X0) \Rightarrow ((X9 = X7) \vee (k1_funct_1 \\
& X3 X9 = k6_numbers))) \wedge ((k3_funct_2 X0 k1_numbers X4 X8 = np_{-1}) \wedge \\
& (\forall X9. (X9 \in X0) \Rightarrow ((X9 = X8) \vee (k1_funct_1 X4 X9 = k6_numbers))))))))) \Rightarrow \\
& ((X5 = X6) \vee ((X5 = X7) \vee ((X5 = X8) \vee ((X6 = X7) \vee ((X6 = X8) \vee ((X7 = X8) \vee (\\
& \forall X9. (m1_subset_1 X9 k1_numbers) \Rightarrow (\forall X10. (m1_subset_1 \\
& X10 k1_numbers) \Rightarrow (\forall X11. (m1_subset_1 X11 k1_numbers) \Rightarrow (\\
& \forall X12. (m1_subset_1 X12 k1_numbers) \Rightarrow ((r2_funct_2 X0 k1_numbers \\
& (k1_funcsdom X0 k1_numbers (k5_funcsdom X0) (k1_funcsdom X0 k1_numbers \\
& (k5_funcsdom X0) (k1_funcsdom X0 k1_numbers (k5_funcsdom X0) (\\
& k2_funcsdom X0 k1_numbers k1_numbers (k9_funct_2 X0 k1_numbers) \\
& (k7_funcsdom X0) (k1_domain_1 k1_numbers (k9_funct_2 X0 k1_numbers) \\
& X9 X1)) (k2_funcsdom X0 k1_numbers k1_numbers (k9_funct_2 X0 k1_numbers) \\
& (k7_funcsdom X0) (k1_domain_1 k1_numbers (k9_funct_2 X0 k1_numbers) \\
& X10 X2))) (k2_funcsdom X0 k1_numbers k1_numbers (k9_funct_2 X0 \\
& k1_numbers) (k7_funcsdom X0) (k1_domain_1 k1_numbers (k9_funct_2 \\
& X0 k1_numbers) X11 X3))) (k2_funcsdom X0 k1_numbers k1_numbers \\
& (k9_funct_2 X0 k1_numbers) (k7_funcsdom X0) (k1_domain_1 k1_numbers \\
& (k9_funct_2 X0 k1_numbers) X12 X4))) (k8_funcsdom X0) \Rightarrow ((X9 = k6_numbers) \wedge \\
& ((X10 = k6_numbers) \wedge ((X11 = k6_numbers) \wedge (X12 = k6_numbers))))))))) \\
& \hspace{15em} (1)
\end{aligned}$$

Assume the following.

$$\begin{aligned}
& \forall X0. (\neg v1_xboole_0 X0) \Rightarrow (\forall X1. (m1_subset_1 X1 X0) \Rightarrow \\
& (\exists X2. (m2_funct_2 X2 X0 k1_numbers (k9_funct_2 X0 k1_numbers)) \wedge \\
& ((k3_funct_2 X0 k1_numbers X2 X1 = np_{-1}) \wedge (\forall X3. (X3 \in X0) \Rightarrow \\
& ((X3 = X1) \vee (k1_funct_1 X2 X3 = k6_numbers)))))) \\
& \hspace{15em} (2)
\end{aligned}$$

Theorem 1

$$\begin{aligned}
& \forall X0.(\neg v1_xboole_0 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 X0) \Rightarrow \\
& (\forall X2.(m1_subset_1 X2 X0) \Rightarrow (\forall X3.(m1_subset_1 X3 X0) \Rightarrow \\
& (\forall X4.(m1_subset_1 X4 X0) \Rightarrow (\neg(X1 \neq X2) \wedge ((X1 \neq X3) \wedge ((X1 \neq X4) \wedge \\
& ((X2 \neq X3) \wedge ((X2 \neq X4) \wedge ((X3 \neq X4) \wedge (\forall X5.(m2_funct_2 X5 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X6.(m2_funct_2 X6 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X7.(m2_funct_2 X7 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\forall X8.(m2_funct_2 X8 X0 k1_numbers \\
& (k9_funct_2 X0 k1_numbers)) \Rightarrow (\exists X9.(m1_subset_1 X9 k1_numbers) \wedge \\
& (\exists X10.(m1_subset_1 X10 k1_numbers) \wedge (\exists X11.(m1_subset_1 \\
& X11 k1_numbers) \wedge (\exists X12.(m1_subset_1 X12 k1_numbers) \wedge (\\
& (r2_funct_2 X0 k1_numbers (k1_funcsdom X0 k1_numbers (k5_funcsdom \\
& X0) (k1_funcsdom X0 k1_numbers (k5_funcsdom X0) (k1_funcsdom X0 \\
& k1_numbers (k5_funcsdom X0) (k2_funcsdom X0 k1_numbers k1_numbers \\
& (k9_funct_2 X0 k1_numbers) (k7_funcsdom X0) (k1_domain_1 k1_numbers \\
& (k9_funct_2 X0 k1_numbers) X9 X5)) (k2_funcsdom X0 k1_numbers k1_numbers \\
& (k9_funct_2 X0 k1_numbers) (k7_funcsdom X0) (k1_domain_1 k1_numbers \\
& (k9_funct_2 X0 k1_numbers) X10 X6))) (k2_funcsdom X0 k1_numbers \\
& k1_numbers (k9_funct_2 X0 k1_numbers) (k7_funcsdom X0) (k1_domain_1 \\
& k1_numbers (k9_funct_2 X0 k1_numbers) X11 X7))) (k2_funcsdom X0 \\
& k1_numbers k1_numbers (k9_funct_2 X0 k1_numbers) (k7_funcsdom \\
& X0) (k1_domain_1 k1_numbers (k9_funct_2 X0 k1_numbers) X12 X8))) \\
& (k8_funcsdom X0)) \wedge (\neg(X9 = k6_numbers) \wedge ((X10 = k6_numbers) \wedge ((\\
& X11 = k6_numbers) \wedge (X12 = k6_numbers))))))))))))))))))
\end{aligned}$$