

# t18\_polynom7 (TMLFrEc- vAtjH6Ur5fZWohjGiE5WWQjTbVV7)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k3\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_polynom7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k16\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v4\_valued\_0 : \iota \Rightarrow o$  be given. Let  $v2\_pre\_poly : \iota \Rightarrow o$  be given. Let  $k4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_funct\_7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k10\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_tarski : \iota \Rightarrow \iota$  be given. Let  $k8\_funcop\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k15\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k14\_pre\_poly : \iota \Rightarrow \iota$  be given. Let  $k15\_funct\_7 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m2\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l4\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l4\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l3\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l3\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $k7\_polynom1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. \forall X2. (X1 \in X0) \Rightarrow (k1\_funct\_1 (k2\_funcop\_1 X0 X2) X1 = X2) \quad (1)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1. \forall X2. \forall X3. (X2 \neq X3) \Rightarrow (k1\_funct\_1 (k2\_funct\_7 X0 X2 X1) X3 = k1\_funct\_1 X0 X3)) \quad (2)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1. \forall X2. (X2 \in k9\_xtuple\_0 X0) \Rightarrow (k1\_funct\_1 (k2\_funct\_7 X0 X2 X1) X2 = X1)) \quad (3)$$

Assume the following.

$$\forall X0.\forall X1.(m1\_subset\_1 X0 X1)\Rightarrow((v1\_xboole\_0 X1)\vee (X0 \in X1)) \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(k9\_xtuple\_0 (k2\_funcop\_1 X0 X1) = X0)\wedge(r1\_tarski (k10\_xtuple\_0 (k2\_funcop\_1 X0 X1)) (k1\_tarski X1)) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.\forall X2.((\neg v1\_xboole\_0 X0)\wedge(m1\_subset\_1 X2 X0))\Rightarrow(k8\_funcop\_1 X0 X1 X2 = k2\_funcop\_1 X1 X2) \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v2\_struct\_0 \\ & X1)\wedge(l1\_struct\_0 X1))\wedge(((v1\_funct\_1 X2)\wedge((v1\_funct\_2 X2 (k15\_pre\_poly \\ & X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & (k15\_pre\_poly X0) (u1\_struct\_0 X1))))))\wedge((v1\_relat\_1 X3)\wedge(( \\ & v4\_relat\_1 X3 X0)\wedge((v1\_funct\_1 X3)\wedge((v1\_partfun1 X3 X0)\wedge((v4\_valued\_0 \\ & X3)\wedge(v2\_pre\_poly X3))))))))))\Rightarrow(k3\_polynom1 X0 X1 X2 X3 = k1\_funct\_1 \\ & X2 X3) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0.k15\_pre\_poly X0 = k14\_pre\_poly X0 \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.\forall X4.(((v1\_funct\_1 \\ & X2)\wedge((v1\_funct\_2 X2 X0 X1)\wedge(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 \\ & X0 X1))))))\wedge(m1\_subset\_1 X4 X1))\Rightarrow(k15\_funct\_7 X0 X1 X2 X3 X4 = k2\_funct\_7 \\ & X2 X3 X4) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge(l2\_struct\_0 X1))\Rightarrow \\ & (\exists X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly \\ & X0) (u1\_struct\_0 X1))))\wedge((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 (k15\_pre\_poly \\ & X0))\wedge((v5\_relat\_1 X2 (u1\_struct\_0 X1))\wedge((v1\_funct\_1 X2)\wedge((\neg \\ & v1\_xboole\_0 X2)\wedge((v1\_partfun1 X2 (k15\_pre\_poly X0))\wedge((v1\_funct\_2 \\ & X2 (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge(v1\_polynom1 X2 (k15\_pre\_poly \\ & X0) X1)))))))))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.\neg v1\_xboole\_0 (k14\_pre\_poly X0) \quad (11)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v1\_xboole\_0 X0)\wedge((\neg v1\_xboole\_0 X1)\wedge \\ (m1\_subset\_1 X1 (k1\_zfmisc\_1 X0))))\Rightarrow(\forall X2.(m2\_subset\_1 \\ X2 X0 X1)\Rightarrow(m1\_subset\_1 X2 X0)) \end{aligned} \quad (12)$$

Assume the following.

$$\forall X0.(l5\_algstr\_0 X0)\Rightarrow((l4\_algstr\_0 X0)\wedge(l4\_struct\_0 X0)) \quad (13)$$

Assume the following.

$$\forall X0.(l4\_struct\_0 X0)\Rightarrow((l2\_struct\_0 X0)\wedge(l3\_struct\_0 X0)) \quad (14)$$

Assume the following.

$$\forall X0.(l4\_algstr\_0 X0)\Rightarrow((l3\_struct\_0 X0)\wedge(l3\_algstr\_0 X0)) \quad (15)$$

Assume the following.

$$\forall X0.(l3\_struct\_0 X0)\Rightarrow(l1\_struct\_0 X0) \quad (16)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge(l2\_struct\_0 X1))\Rightarrow \\ ((v1\_funct\_1 (k7\_polynom1 X0 X1))\wedge((v1\_funct\_2 (k7\_polynom1 \\ X0 X1) (k15\_pre\_poly X0) (u1\_struct\_0 X1))\wedge(m1\_subset\_1 (k7\_polynom1 \\ X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 \\ X1)))))) \end{aligned} \quad (17)$$

Assume the following.

$$\forall X0.(l2\_struct\_0 X0)\Rightarrow(m1\_subset\_1 (k4\_struct\_0 X0) (u1\_struct\_0 X0)) \quad (18)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.\forall X2.(((\neg v2\_struct\_0 X1)\wedge(l2\_struct\_0 \\ X1))\wedge(m1\_subset\_1 X2 (u1\_struct\_0 X1)))\Rightarrow((v1\_funct\_1 (k4\_polynom7 \\ X0 X1 X2))\wedge((v1\_funct\_2 (k4\_polynom7 X0 X1 X2) (k15\_pre\_poly X0) \\ (u1\_struct\_0 X1))\wedge(m1\_subset\_1 (k4\_polynom7 X0 X1 X2) (k1\_zfmisc\_1 \\ (k2\_zfmisc\_1 (k15\_pre\_poly X0) (u1\_struct\_0 X1)))))) \end{aligned} \quad (19)$$

Assume the following.

$$\forall X0.m2\_subset\_1 (k16\_pre\_poly X0) (k14\_pre\_poly X0) (k15\_pre\_poly X0) \quad (20)$$

Assume the following.

$$\forall X0.m1\_subset\_1 (k15\_pre\_poly X0) (k1\_zfmisc\_1 (k14\_pre\_poly X0)) \quad (21)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge(l2\_struct\_0 X1))\Rightarrow \\ & (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X1))\Rightarrow(k4\_polynom7 X0 \\ & X1 X2 = k15\_funct\_7 (k15\_pre\_poly X0) (u1\_struct\_0 X1) (k7\_polynom1 \\ & X0 X1) (k16\_pre\_poly X0) X2)) \end{aligned} \quad (22)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge(l2\_struct\_0 X1))\Rightarrow \\ & (k7\_polynom1 X0 X1 = k8\_funcop\_1 (u1\_struct\_0 X1) (k15\_pre\_poly \\ & X0) (k4\_struct\_0 X1)) \end{aligned} \quad (23)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(X1 = k14\_pre\_poly X0)\Leftrightarrow(\forall X2.(X2 \in \\ & X1)\Leftrightarrow((v1\_relat\_1 X2)\wedge((v4\_relat\_1 X2 X0)\wedge((v1\_funct\_1 X2)\wedge( \\ & (v1\_partfun1 X2 X0)\wedge((v4\_valued\_0 X2)\wedge(v2\_pre\_poly X2)))))) \end{aligned} \quad (24)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(v1\_xboole\_0 X0)\Rightarrow(\forall X2.(m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X1 X0)))\Rightarrow(v1\_xboole\_0 X2)) \end{aligned} \quad (25)$$

Assume the following.

$$\begin{aligned} & \forall X0.(v1\_xboole\_0 X0)\Rightarrow(\forall X1.(m1\_subset\_1 X1 (k1\_zfmisc\_1 \\ & X0))\Rightarrow(v1\_xboole\_0 X1)) \end{aligned} \quad (26)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(m1\_subset\_1 X2 (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 X0 X1)))\Rightarrow(v1\_relat\_1 X2) \end{aligned} \quad (27)$$

### Theorem 1

$$\begin{aligned} & \forall X0.\forall X1.((\neg v2\_struct\_0 X1)\wedge(l5\_algstr\_0 X1))\Rightarrow \\ & (\forall X2.(m1\_subset\_1 X2 (u1\_struct\_0 X1))\Rightarrow((k3\_polynom1 \\ & X0 X1 (k4\_polynom7 X0 X1 X2) (k16\_pre\_poly X0) = X2)\wedge(\forall X3. \\ & ((v1\_relat\_1 X3)\wedge((v4\_relat\_1 X3 X0)\wedge((v1\_funct\_1 X3)\wedge((v1\_partfun1 \\ & X3 X0)\wedge((v4\_valued\_0 X3)\wedge(v2\_pre\_poly X3))))))\Rightarrow((X3\neq k16\_pre\_poly \\ & X0)\Rightarrow(k3\_polynom1 X0 X1 (k4\_polynom7 X0 X1 X2) X3 = k4\_struct\_0 X1)))) \end{aligned}$$