

t18\_stacks\_1  
(TMLhwjMfneoAtJDthsjsdeNZhbh6CLDQnQ)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $v3\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $v4\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $v5\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $v6\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $l1\_stacks\_1 : \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $r2\_stacks\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_stacks\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k6\_stacks\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k9\_stacks\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_stacks\_1 \\ & X0) \wedge ((v3\_stacks\_1 X0) \wedge ((v4\_stacks\_1 X0) \wedge ((v5\_stacks\_1 X0) \wedge \\ & ((v6\_stacks\_1 X0) \wedge (l1\_stacks\_1 X0)))))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u4\_struct\_0 X0) \Rightarrow ((\neg r1\_stacks\_1 X0 X1) \Rightarrow (k6\_stacks\_1 X0 X1 = \\ & k1\_funct\_1 (k9\_stacks\_1 X0 X1) np\_1))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_stacks\_1 \\ & X0) \wedge ((v3\_stacks\_1 X0) \wedge ((v4\_stacks\_1 X0) \wedge ((v5\_stacks\_1 X0) \wedge \\ & ((v6\_stacks\_1 X0) \wedge (l1\_stacks\_1 X0)))))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u4\_struct\_0 X0) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u4\_struct\_0 \\ & X0) \Rightarrow (((r2\_stacks\_1 X0 X1 X2) \wedge (r1\_stacks\_1 X0 X1) \Rightarrow (r1\_stacks\_1 \\ & X0 X2)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_stacks\_1 \\ & X0) \wedge ((v3\_stacks\_1 X0) \wedge ((v4\_stacks\_1 X0) \wedge ((v5\_stacks\_1 X0) \wedge \\ & ((v6\_stacks\_1 X0) \wedge (l1\_stacks\_1 X0)))))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u4\_struct\_0 X0) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u4\_struct\_0 \\ & X0) \Rightarrow ((r2\_stacks\_1 X0 X1 X2) \Leftrightarrow (k9\_stacks\_1 X0 X1 = k9\_stacks\_1 X0 \\ & X2)))))) \end{aligned} \tag{3}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_stacks\_1 \\ & X0) \wedge ((v3\_stacks\_1 X0) \wedge ((v4\_stacks\_1 X0) \wedge ((v5\_stacks\_1 X0) \wedge \\ & ((v6\_stacks\_1 X0) \wedge (l1\_stacks\_1 X0))))))) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 (u4\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 (u4\_struct\_0 \\ & X0)) \Rightarrow ((r2\_stacks\_1 X0 X1 X2) \Rightarrow ((r1\_stacks\_1 X0 X1) \vee (k6\_stacks\_1 \\ & X0 X1 = k6\_stacks\_1 X0 X2)))))) \end{aligned}$$