

## t19\_index\_1

(TMV6pn1XAnedTkyM7oXT3Bo6xMphxods1AL)

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Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v2\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v4\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v5\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v6\_cat\_1 : \iota \Rightarrow o$  be given. Let  $l1\_cat\_1 : \iota \Rightarrow o$  be given. Let  $v3\_cat\_5 : \iota \Rightarrow o$  be given. Let  $m2\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k13\_index\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k7\_cat\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $l1\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l5\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_graph\_1 : \iota \Rightarrow o$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k12\_mcart\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
 & \forall X0.((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
 & X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
 & X0) \wedge (l1\_cat\_1 X0))))))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge ((\neg \\
 & v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
 & X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge ((v3\_cat\_5 X1) \wedge (l1\_cat\_1 \\
 & X1)))))))))) \Rightarrow (\forall X2.((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 \\
 & X2) \wedge ((v2\_cat\_1 X2) \wedge ((v3\_cat\_1 X2) \wedge ((v4\_cat\_1 X2) \wedge ((v5\_cat\_1 \\
 & X2) \wedge ((v6\_cat\_1 X2) \wedge ((v3\_cat\_5 X2) \wedge (l1\_cat\_1 X2)))))))))) \Rightarrow (\forall X3. \\
 & (m2\_cat\_1 X3 X0 X1) \Rightarrow (\forall X4.(m2\_cat\_1 X4 X0 X2) \Rightarrow ((r1\_funct\_2 \\
 & (u4\_struct\_0 X0) (u4\_struct\_0 X1) (u4\_struct\_0 X0) (u4\_struct\_0 \\
 & X2) X3 X4) \Rightarrow (r1\_funct\_2 (u1\_struct\_0 X0) (u1\_struct\_0 X1) (u1\_struct\_0 \\
 & X0) (u1\_struct\_0 X2) (k7\_cat\_1 X0 X1 X3) (k7\_cat\_1 X0 X2 X4))))))
 \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. \forall X3. \forall X4. \forall X5. \\
& ((\neg v1\_xboole\_0 X1) \wedge (\neg v1\_xboole\_0 X3) \wedge ((v1\_funct\_1 X4) \wedge (v1\_funct\_2 X4 X0 X1) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X0 X1)))))) \wedge ((v1\_funct\_1 X5) \wedge ((v1\_funct\_2 X5 X2 X3) \wedge (m1\_subset\_1 X5 (k1\_zfmisc\_1 (k2\_zfmisc\_1 X2 X3)))))) \Rightarrow ((r1\_funct\_2 X0 X1 X2 X3 X4 X5) \Leftrightarrow (X4 = X5))
\end{aligned} \tag{2}$$

Assume the following.

$$\forall X0. ((\neg v2\_struct\_0 X0) \wedge (l1\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 (u1\_struct\_0 X0)) \tag{3}$$

Assume the following.

$$\forall X0. ((\neg v11\_struct\_0 X0) \wedge (l5\_struct\_0 X0)) \Rightarrow (\neg v1\_xboole\_0 (u4\_struct\_0 X0)) \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. (((\neg v2\_struct\_0 X0) \wedge (\neg v11\_struct\_0 X0) \wedge \\
& ((v2\_cat\_1 X0) \wedge (v3\_cat\_1 X0) \wedge (v4\_cat\_1 X0) \wedge (v5\_cat\_1 X0) \wedge \\
& ((v6\_cat\_1 X0) \wedge (l1\_cat\_1 X0)))))) \wedge ((\neg v2\_struct\_0 X1) \wedge (\neg \\
& v11\_struct\_0 X1) \wedge (v2\_cat\_1 X1) \wedge (v3\_cat\_1 X1) \wedge (v4\_cat\_1 X1) \wedge \\
& ((v5\_cat\_1 X1) \wedge (v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))) \Rightarrow (\forall X2. \\
& (m2\_cat\_1 X2 X0 X1) \Rightarrow ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (u4\_struct\_0 X0) (u4\_struct\_0 X1)) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u4\_struct\_0 X0) (u4\_struct\_0 X1)))))))
\end{aligned} \tag{5}$$

Assume the following.

$$\forall X0. (l5\_struct\_0 X0) \Rightarrow (l1\_struct\_0 X0) \tag{6}$$

Assume the following.

$$\forall X0. (l1\_graph\_1 X0) \Rightarrow (l5\_struct\_0 X0) \tag{7}$$

Assume the following.

$$\forall X0. (l1\_cat\_1 X0) \Rightarrow (l1\_graph\_1 X0) \tag{8}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 \\
& X0) \wedge ((v2\_cat\_1 X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 \\
& X0) \wedge ((v6\_cat\_1 X0) \wedge (l1\_cat\_1 X0)))))) \wedge (((\neg v2\_struct\_0 X1) \wedge \\
& ((\neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
& X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge (l1\_cat\_1 X1)))))) \wedge ((v1\_funct\_1 \\
& X2) \wedge ((v1\_funct\_2 X2 (u4\_struct\_0 X0) (u4\_struct\_0 X1)) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u4\_struct\_0 X0) (u4\_struct\_0 X1)))))) \Rightarrow \\
& ((v1\_funct\_1 (k7\_cat\_1 X0 X1 X2)) \wedge ((v1\_funct\_2 (k7\_cat\_1 X0 X1 \\
& X2) (u1\_struct\_0 X0) (u1\_struct\_0 X1)) \wedge (m1\_subset\_1 (k7\_cat\_1 \\
& X0 X1 X2) (k1\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 \\
& X1))))))
\end{aligned} \tag{9}$$

Assume the following.

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
& X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
& X0) \wedge (l1\_cat\_1 X0)))))) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge (( \\
& \neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
& X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge ((v3\_cat\_5 X1) \wedge (l1\_cat\_1 \\
& X1)))))) \Rightarrow (\forall X2. (m2\_cat\_1 X2 X0 X1) \Rightarrow (k13\_index\_1 X0 X1 \\
& X2 = k4\_tarski (k7\_cat\_1 X0 X1 X2) (k12\_mcart\_1 X2))))
\end{aligned} \tag{10}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0. ((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 X0) \wedge ((v2\_cat\_1 \\
& X0) \wedge ((v3\_cat\_1 X0) \wedge ((v4\_cat\_1 X0) \wedge ((v5\_cat\_1 X0) \wedge ((v6\_cat\_1 \\
& X0) \wedge (l1\_cat\_1 X0)))))) \Rightarrow (\forall X1. ((\neg v2\_struct\_0 X1) \wedge (( \\
& \neg v11\_struct\_0 X1) \wedge ((v2\_cat\_1 X1) \wedge ((v3\_cat\_1 X1) \wedge ((v4\_cat\_1 \\
& X1) \wedge ((v5\_cat\_1 X1) \wedge ((v6\_cat\_1 X1) \wedge ((v3\_cat\_5 X1) \wedge (l1\_cat\_1 \\
& X1)))))) \Rightarrow (\forall X2. ((\neg v2\_struct\_0 X2) \wedge ((\neg v11\_struct\_0 \\
& X2) \wedge ((v2\_cat\_1 X2) \wedge ((v3\_cat\_1 X2) \wedge ((v4\_cat\_1 X2) \wedge ((v5\_cat\_1 \\
& X2) \wedge ((v6\_cat\_1 X2) \wedge ((v3\_cat\_5 X2) \wedge (l1\_cat\_1 X2)))))) \Rightarrow (\forall X3. \\
& (m2\_cat\_1 X3 X0 X1) \Rightarrow (\forall X4. (m2\_cat\_1 X4 X0 X2) \Rightarrow ((r1\_funct\_2 \\
& (u4\_struct\_0 X0) (u4\_struct\_0 X1) (u4\_struct\_0 X0) (u4\_struct\_0 \\
& X2) X3 X4) \Rightarrow (k13\_index\_1 X0 X1 X3 = k13\_index\_1 X0 X2 X4))))))
\end{aligned}$$