

# t19\_ratfunc1 (TMGSfwxpUBRdcnGaYUoy- hzVd7oAob8bGHoP)

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Let  $v7\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l5\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $m1\_ratfunc1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_ratfunc1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_ratfunc1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k5\_ratfunc1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k4\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_numbers : \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_algseq\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_ratfunc1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Assume the following.

$$\forall X0. \forall X1. (k1\_xtuple\_0 (k4\_tarski X0 X1) = X0) \wedge (k2\_xtuple\_0 (k4\_tarski X0 X1) = X1) \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. (((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge (m1\_ratfunc1 X1 X0)) \Rightarrow (k5\_ratfunc1 X0 X1 = k2\_xtuple\_0 X1) \quad (2)$$

Assume the following.

$$\forall X0. \forall X1. (((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge (m1\_ratfunc1 X1 X0)) \Rightarrow (k4\_ratfunc1 X0 X1 = k1\_xtuple\_0 X1) \quad (3)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. (((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_funct\_2 X1 k5\_numbers (u1\_struct\_0 X0)) \wedge ((v1\_algseq\_1 X1 X0) \wedge (m1\_subset\_1 X1 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 X0)))))))) \wedge ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 k5\_numbers (u1\_struct\_0 X0)) \wedge ((v1\_algseq\_1 X2 X0) \wedge ((\neg v1\_ratfunc1 X2 X0) \wedge (m1\_subset\_1 X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 X0)))))))))) \Rightarrow (k3\_ratfunc1 X0 X1 X2 = k4\_tarski X1 X2) \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge \\ & (m1\_ratfunc1 X1 X0)) \Rightarrow ((v1\_funct\_1 (k5\_ratfunc1 X0 X1)) \wedge ((v1\_funct\_2 \\ & (k5\_ratfunc1 X0 X1) k5\_numbers (u1\_struct\_0 X0)) \wedge ((v1\_algseq\_1 \\ & (k5\_ratfunc1 X0 X1) X0) \wedge ((\neg v1\_ratfunc1 (k5\_ratfunc1 X0 X1) X0) \wedge \\ & (m1\_subset\_1 (k5\_ratfunc1 X0 X1) (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers \\ & (u1\_struct\_0 X0)))))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. (((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \wedge \\ & (m1\_ratfunc1 X1 X0)) \Rightarrow ((v1\_funct\_1 (k4\_ratfunc1 X0 X1)) \wedge ((v1\_funct\_2 \\ & (k4\_ratfunc1 X0 X1) k5\_numbers (u1\_struct\_0 X0)) \wedge ((v1\_algseq\_1 \\ & (k4\_ratfunc1 X0 X1) X0) \wedge (m1\_subset\_1 (k4\_ratfunc1 X0 X1) (k1\_zfmisc\_1 \\ & (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 X0)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m1\_ratfunc1 X1 X0) \Leftrightarrow (\exists X2. ((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 \\ & X2 k5\_numbers (u1\_struct\_0 X0)) \wedge ((v1\_algseq\_1 X2 X0) \wedge (m1\_subset\_1 \\ & X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 X0)))))) \wedge \\ & (\exists X3. ((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 X3 k5\_numbers (u1\_struct\_0 \\ & X0)) \wedge ((v1\_algseq\_1 X3 X0) \wedge ((\neg v1\_ratfunc1 X3 X0) \wedge (m1\_subset\_1 \\ & X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 k5\_numbers (u1\_struct\_0 X0)))))) \wedge \\ & (X1 = k4\_tarski X2 X3)))) \end{aligned} \quad (7)$$

**Theorem 1**

$$\begin{aligned} & \forall X0. ((\neg v7\_struct\_0 X0) \wedge (l5\_algstr\_0 X0)) \Rightarrow (\forall X1. \\ & (m1\_ratfunc1 X1 X0) \Rightarrow (X1 = k3\_ratfunc1 X0 (k4\_ratfunc1 X0 X1) (k5\_ratfunc1 \\ & X0 X1))) \end{aligned}$$