

# t1\_exchsort (TMRpEEeDu- aWxu6QCpKbCFCwExVDkEW3TURZ)

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Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k6\_subset\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_ordinal2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $r1\_tarski : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r1\_ordinal1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k5\_ordinal3 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v1\_ordinal6 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} \forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (\forall X2. \\ (X2 \in k6\_subset\_1 X0 X1) \Leftrightarrow ((r1\_tarski X1 X2) \wedge (X2 \in X0)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} \forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (\forall X2. \\ (v3\_ordinal1 X2) \Rightarrow ((X0 \in X1) \Rightarrow (k10\_ordinal2 X2 X0 \in k10\_ordinal2 \\ X2 X1)))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} \forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (( \\ r1\_ordinal1 X0 (k10\_ordinal2 X0 X1)) \wedge (r1\_ordinal1 X1 (k10\_ordinal2 \\ X0 X1)))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} \forall X0.(v3\_ordinal1 X0) \Rightarrow (\forall X1.(v3\_ordinal1 X1) \Rightarrow (\forall X2. \\ (v3\_ordinal1 X2) \Rightarrow ((k10\_ordinal2 X0 X1 \in k10\_ordinal2 X0 X2) \Rightarrow (X1 \in \\ X2)))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((v3\_ordinal1 X0) \wedge (v3\_ordinal1 X1)) \Rightarrow ( \\ (r1\_ordinal1 X0 X1) \Leftrightarrow (r1\_tarski X0 X1)) \end{aligned} \quad (6)$$

Assume the following.

$$\forall X0.\forall X1.((v3\_ordinal1\ X0)\wedge(v3\_ordinal1\ X1))\Rightarrow(v3\_ordinal1\ (k5\_ordinal3\ X0\ X1)) \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.((v3\_ordinal1\ X0)\wedge(v3\_ordinal1\ X1))\Rightarrow(v3\_ordinal1\ (k10\_ordinal2\ X0\ X1)) \quad (8)$$

Assume the following.

$$\begin{aligned} &\forall X0.(v3\_ordinal1\ X0)\Rightarrow(\forall X1.(v3\_ordinal1\ X1)\Rightarrow(\forall X2. \\ &(v3\_ordinal1\ X2)\Rightarrow(((r1\_ordinal1\ X1\ X0)\Rightarrow((X2 = k5\_ordinal3\ X0\ X1)\Leftrightarrow \\ &(X0 = k10\_ordinal2\ X1\ X2))))\wedge((\neg r1\_ordinal1\ X1\ X0)\Rightarrow((X2 = k5\_ordinal3 \\ &X0\ X1)\Leftrightarrow(X2 = k1\_xboole\_0)))))) \end{aligned} \quad (9)$$

Assume the following.

$$\forall X0.(v1\_ordinal6\ X0)\Rightarrow(\forall X1.(m1\_subset\_1\ X1\ X0)\Rightarrow(v3\_ordinal1\ X1)) \quad (10)$$

Assume the following.

$$\forall X0.(v3\_ordinal1\ X0)\Rightarrow(v1\_ordinal6\ X0) \quad (11)$$

**Theorem 1**

$$\begin{aligned} &\forall X0.(v3\_ordinal1\ X0)\Rightarrow(\forall X1.(v3\_ordinal1\ X1)\Rightarrow(\forall X2. \\ &(X2 \in k6\_subset\_1\ (k10\_ordinal2\ X0\ X1)\ X0)\Leftrightarrow(\exists X3.(v3\_ordinal1 \\ &X3)\wedge((X2 = k10\_ordinal2\ X0\ X3)\wedge(X3 \in X1)))))) \end{aligned}$$