

t1\_ltlaxio1  
(TMdgifoqoScZnDKcimw9qguTNYsZRrWscZ79)

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Let  $v1\_xboolean : \iota \Rightarrow o$  be given. Let  $k6\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k4\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $np\_1 : \iota$  be given. Let  $k5\_xboolean : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k2\_xboolean : \iota$  be given. Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (k5\_xboolean X0 (k4\_xboolean X0 X1) = X0)) \quad (1)$$

Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (k6\_xboolean X0 (k6\_xboolean X0 X1) = k6\_xboolean X0 X1)) \quad (2)$$

Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (k6\_xboolean X0 (k5\_xboolean X0 X1) = k2\_xboolean)) \quad (3)$$

Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (\forall X1.(v1\_xboolean X1) \Rightarrow (\forall X2.(v1\_xboolean X2) \Rightarrow ((k6\_xboolean X0 (k6\_xboolean X1 X2) = k2\_xboolean) \Rightarrow (k6\_xboolean (k6\_xboolean X0 X1) (k6\_xboolean X0 X2) = k2\_xboolean)))) \quad (4)$$

Assume the following.

$$\forall X0.(v1\_xboolean X0) \Rightarrow (k6\_xboolean X0 X0 = k2\_xboolean) \quad (5)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xboolean X0) \wedge (v1\_xboolean X1)) \Rightarrow (v1\_xboolean (k4\_xboolean X0 X1)) \quad (6)$$

Assume the following.

$$k2\_xboolean = np\_1 \quad (7)$$

Assume the following.

$$\forall X0.\forall X1.((v1\_xboolean X0) \wedge (v1\_xboolean X1)) \Rightarrow (k5\_xboolean X0 X1 = k5\_xboolean X1 X0) \quad (8)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(v1\_xboolean\ X0) \Rightarrow (\forall X1.(v1\_xboolean\ X1) \Rightarrow (\forall X2. \\ & (v1\_xboolean\ X2) \Rightarrow (k6\_xboolean\ (k6\_xboolean\ X0\ (k4\_xboolean\ X1 \\ & \quad X2))\ (k6\_xboolean\ X0\ X1) = np\_1))) \end{aligned}$$