

t1_msafree
(TMGjs65YdPH5RJyVKdhS8RKBx1QLsuWzZ8)

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Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k3_finseq_2 : \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $v4_relat_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m2_finseq_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k3_relat_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k6_finseq_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_card_3 : \iota \Rightarrow \iota$ be given. Let $k9_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k13_finseq_1 : \iota \Rightarrow \iota$ be given. Let $k1_relset_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((v1_relat_1 X1) \wedge (v1_funct_1 X1)) \Rightarrow (\forall X2. \\ & ((v1_relat_1 X2) \wedge (v1_funct_1 X2)) \Rightarrow ((X0 \in k9_xtuple_0 (k3_relat_1 \\ & X2 X1)) \Rightarrow (k1_funct_1 (k3_relat_1 X2 X1) X0 = k1_funct_1 X1 (k1_funct_1 \\ & X2 X0)))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. k3_finseq_2 X0 = k13_finseq_1 X0 \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. ((v1_relat_1 X1) \wedge (v4_relat_1 X1 X0)) \Rightarrow (k1_relset_1 X0 X1 = k9_xtuple_0 X1) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. ((\neg v1_xboole_0 X1) \wedge \\ & (((v1_funct_1 X2) \wedge ((v1_funct_2 X2 X0 X1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X1)))))) \wedge ((v1_relat_1 X3) \wedge ((v4_relat_1 X3 X1) \wedge \\ & ((v1_funct_1 X3) \wedge (v1_partfun1 X3 X1)))))) \Rightarrow ((v1_relat_1 (k3_relat_1 \\ & X2 X3)) \wedge ((v4_relat_1 (k3_relat_1 X2 X3) X0) \wedge ((v1_funct_1 (k3_relat_1 \\ & X2 X3)) \wedge (v1_partfun1 (k3_relat_1 X2 X3) X0)))) \end{aligned} \tag{4}$$

Assume the following.

$$\forall X0. \neg v1_xboole_0 (k13_finseq_1 X0) \quad (5)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\ (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow ((v1_relat_1 (k6_finseq_2 \\ X0 X1)) \wedge ((v4_relat_1 (k6_finseq_2 X0 X1) (k3_finseq_2 X0)) \wedge ((\\ v1_funct_1 (k6_finseq_2 X0 X1)) \wedge (v1_partfun1 (k6_finseq_2 X0 \\ X1) (k3_finseq_2 X0)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} \forall X0. \forall X1. ((v1_relat_1 X1) \wedge ((v4_relat_1 X1 X0) \wedge \\ (v1_funct_1 X1) \wedge (v1_partfun1 X1 X0))) \Rightarrow (\forall X2. ((v1_relat_1 \\ X2) \wedge ((v4_relat_1 X2 (k3_finseq_2 X0)) \wedge ((v1_funct_1 X2) \wedge (v1_partfun1 \\ X2 (k3_finseq_2 X0)))))) \Rightarrow ((X2 = k6_finseq_2 X0 X1) \Leftrightarrow (\forall X3. \\ (m2_finseq_2 X3 X0 (k3_finseq_2 X0)) \Rightarrow (k1_funct_1 X2 X3 = k4_card_3 \\ (k3_relat_1 X3 X1)))))) \end{aligned} \quad (7)$$

Assume the following.

$$\forall X0. \forall X1. ((v1_relat_1 X1) \wedge (v4_relat_1 X1 X0)) \Rightarrow (\\ (v1_partfun1 X1 X0) \Leftrightarrow (k1_relset_1 X0 X1 = X0)) \quad (8)$$

Assume the following.

$$\forall X0. \forall X1. \forall X2. (m1_subset_1 X2 (k1_zfmisc_1 \\ (k2_zfmisc_1 X0 X1))) \Rightarrow (v1_relat_1 X2) \quad (9)$$

Theorem 1

$$\begin{aligned} \forall X0. \forall X1. (\neg v1_xboole_0 X1) \Rightarrow (\forall X2. ((v1_funct_1 \\ X2) \wedge ((v1_funct_2 X2 X0 (k3_finseq_2 X1)) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ (k2_zfmisc_1 X0 (k3_finseq_2 X1)))))) \Rightarrow (\forall X3. ((v1_relat_1 \\ X3) \wedge ((v4_relat_1 X3 X1) \wedge ((v1_funct_1 X3) \wedge (v1_partfun1 X3 X1)))) \Rightarrow \\ (\forall X4. (m2_finseq_2 X4 X1 (k3_finseq_2 X1)) \Rightarrow (\forall X5. \\ ((X5 \in X0) \wedge (X4 = k1_funct_1 X2 X5)) \Rightarrow (k1_funct_1 (k3_relat_1 X2 (\\ k6_finseq_2 X1 X3)) X5 = k4_card_3 (k3_relat_1 X4 X3)))))) \end{aligned}$$