

t1_projpl_1 (TMWBWjFdb- dzjfQMvWp2Cieq4oRwMdpfX3YK)

October 27, 2020

Let $l1_incsp_1 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_incsp_1 : \iota \Rightarrow \iota$ be given. Let $u2_incsp_1 : \iota \Rightarrow \iota$ be given. Let $r4_incsp_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k7_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k8_domain_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $r2_projpl_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r3_projpl_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_incsp_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0.(l1_incsp_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u2_incsp_1 \\ & X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u1_incsp_1 X0)) \Rightarrow (\forall X3. \\ & (m1_subset_1 X3 (u1_incsp_1 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 \\ & (u1_incsp_1 X0)) \Rightarrow ((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 X0) \\ & X2 X3 X4) X1) \Leftrightarrow ((r1_incsp_1 X0 X2 X1) \wedge ((r1_incsp_1 X0 X3 X1) \wedge (r1_incsp_1 \\ & X0 X4 X1)))))))))) \end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned} & \forall X0.(l1_incsp_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u2_incsp_1 \\ & X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u1_incsp_1 X0)) \Rightarrow (\forall X3. \\ & (m1_subset_1 X3 (u1_incsp_1 X0)) \Rightarrow ((r4_incsp_1 X0 (k7_domain_1 \\ & (u1_incsp_1 X0) X2 X3) X1) \Leftrightarrow ((r1_incsp_1 X0 X2 X1) \wedge (r1_incsp_1 X0 \\ & X3 X1)))))) \end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned} & \forall X0.(l1_incsp_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_incsp_1 \\ & X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u2_incsp_1 X0)) \Rightarrow (\forall X3. \\ & (m1_subset_1 X3 (u2_incsp_1 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 \\ & (u2_incsp_1 X0)) \Rightarrow ((r3_projpl_1 X0 X1 X2 X3 X4) \Leftrightarrow ((r1_incsp_1 X0 \\ & X1 X2) \wedge ((r1_incsp_1 X0 X1 X3) \wedge (r1_incsp_1 X0 X1 X4)))))) \end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.(l1_incsp_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_incsp_1 \\
& \quad X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u2_incsp_1 X0)) \Rightarrow (\forall X3. \\
& (m1_subset_1 X3 (u2_incsp_1 X0)) \Rightarrow ((r2_projpl_1 X0 X1 X2 X3) \Leftrightarrow ((\\
& \quad r1_incsp_1 X0 X1 X2) \wedge (r1_incsp_1 X0 X1 X3))))))
\end{aligned} \tag{4}$$

Theorem 1

$$\begin{aligned}
& \forall X0.(l1_incsp_1 X0) \Rightarrow (\forall X1.(m1_subset_1 X1 (u1_incsp_1 \\
& \quad X0)) \Rightarrow (\forall X2.(m1_subset_1 X2 (u1_incsp_1 X0)) \Rightarrow (\forall X3. \\
& (m1_subset_1 X3 (u1_incsp_1 X0)) \Rightarrow (\forall X4.(m1_subset_1 X4 \\
& (u2_incsp_1 X0)) \Rightarrow (\forall X5.(m1_subset_1 X5 (u2_incsp_1 X0)) \Rightarrow \\
& (\forall X6.(m1_subset_1 X6 (u2_incsp_1 X0)) \Rightarrow (((r4_incsp_1 X0 \\
& (k7_domain_1 (u1_incsp_1 X0) X1 X2) X4) \Rightarrow (r4_incsp_1 X0 (k7_domain_1 \\
& (u1_incsp_1 X0) X2 X1) X4)) \wedge (((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 \\
& X0) X1 X2 X3) X4) \Rightarrow ((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 X0) X1 \\
& X3 X2) X4) \wedge ((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 X0) X2 X1 X3) \\
& X4) \wedge ((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 X0) X2 X3 X1) X4) \wedge \\
& ((r4_incsp_1 X0 (k8_domain_1 (u1_incsp_1 X0) X3 X1 X2) X4) \wedge (r4_incsp_1 \\
& X0 (k8_domain_1 (u1_incsp_1 X0) X3 X2 X1) X4)))))) \wedge (((r2_projpl_1 \\
& X0 X1 X4 X5) \Rightarrow (r2_projpl_1 X0 X1 X5 X4)) \wedge ((r3_projpl_1 X0 X1 X4 X5 X6) \Rightarrow \\
& ((r3_projpl_1 X0 X1 X4 X6 X5) \wedge ((r3_projpl_1 X0 X1 X5 X4 X6) \wedge ((r3_projpl_1 \\
& X0 X1 X5 X6 X4) \wedge ((r3_projpl_1 X0 X1 X6 X4 X5) \wedge (r3_projpl_1 X0 X1 X6 \\
& \quad X5 X4))))))))))
\end{aligned}$$