

t20_equation (TM-
FvVc3Vh9DoGsgbKcu9Fb854X3FRR77xGg)

October 27, 2020

Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $v11_struct_0 : \iota \Rightarrow o$ be given. Let $l1_msualg_1 : \iota \Rightarrow o$ be given. Let $m1_pralg_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_msualg_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k14_pralg_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u4_struct_0 : \iota \Rightarrow \iota$ be given. Let $k3_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_relat_1 : \iota \Rightarrow o$ be given. Let $k1_funct_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k5_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_funct_1 : \iota \Rightarrow o$ be given. Let $k3_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k4_card_3 : \iota \Rightarrow \iota$ be given. Let $k9_pralg_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k2_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $l3_msualg_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $v1_funct_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $k2_zfmisc_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k10_pralg_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v2_relat_1 : \iota \Rightarrow o$ be given. Let $v4_relat_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v1_partfun1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v4_msualg_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k10_xtuple_0 : \iota \Rightarrow \iota$ be given. Let $k6_finseq_2 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $u3_msualg_1 : \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1_subset_1 X0 X1) \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2_struct_0 X1) \wedge ((\neg v11_struct_0 X1) \wedge \\ & (l1_msualg_1 X1))) \Rightarrow (\forall X2. (m1_pralg_2 X2 X0 X1) \Rightarrow (\forall X3. \\ & (m1_subset_1 X3 (u4_struct_0 X1)) \Rightarrow (\forall X4. (m1_subset_1 X4 \\ & (k3_msualg_1 X1 X3 (k14_pralg_2 X0 X1 X2))) \Rightarrow (k3_funct_2 (k3_msualg_1 \\ & X1 X3 (k14_pralg_2 X0 X1 X2)) (k4_msualg_1 X1 X3 (k14_pralg_2 X0 X1 \\ & X2)) (k5_msualg_1 X1 X3 (k14_pralg_2 X0 X1 X2)) X4 \in k4_card_3 (k9_pralg_2 \\ & X0 X1 (k2_msualg_1 X1 X3) X2)))))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 \\ & X0))) \Rightarrow (\forall X1.(l3_msualg_1 X1 X0) \Rightarrow (\forall X2.(m1_msualg_2 \\ & X2 X0 X1) \Rightarrow (\forall X3.(m1_subset_1 X3 (u4_struct_0 X0)) \Rightarrow (\forall X4. \\ & (X4 \in k3_msualg_1 X0 X3 X2) \Rightarrow (k1_funct_1 (k5_msualg_1 X0 X3 X2) X4 = \\ & k1_funct_1 (k5_msualg_1 X0 X3 X1) X4)))))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 X0) \wedge (l1_msualg_1 \\ & X0))) \Rightarrow (\forall X1.(l3_msualg_1 X1 X0) \Rightarrow (\forall X2.(m1_msualg_2 \\ & X2 X0 X1) \Rightarrow (\forall X3.(m1_subset_1 X3 (u4_struct_0 X0)) \Rightarrow (\forall X4. \\ & (X4 \in k3_msualg_1 X0 X3 X2) \Rightarrow (X4 \in k3_msualg_1 X0 X3 X1)))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.((\neg v1_xboole_0 X0) \wedge \\ & (((v1_funct_1 X2) \wedge ((v1_funct_2 X2 X0 X1) \wedge (m1_subset_1 X2 (k1_zfmisc_1 \\ & (k2_zfmisc_1 X0 X1)))))) \wedge (m1_subset_1 X3 X0))) \Rightarrow (k3_funct_2 X0 \\ & X1 X2 X3 = k1_funct_1 X2 X3) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X1) \wedge (l1_msualg_1 \\ & X1)) \wedge (m1_pralg_2 X2 X0 X1)) \Rightarrow ((v1_relat_1 (k10_pralg_2 X0 X1 X2)) \wedge \\ & ((v2_relat_1 (k10_pralg_2 X0 X1 X2)) \wedge ((v4_relat_1 (k10_pralg_2 \\ & X0 X1 X2) (u1_struct_0 X1)) \wedge ((v1_funct_1 (k10_pralg_2 X0 X1 X2)) \wedge \\ & (v1_partfun1 (k10_pralg_2 X0 X1 X2) (u1_struct_0 X1)))))) \end{aligned} \quad (6)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X1) \wedge ((\neg v11_struct_0 \\ & X1) \wedge (l1_msualg_1 X1))) \wedge (m1_pralg_2 X2 X0 X1)) \Rightarrow (v4_msualg_1 (\\ & k14_pralg_2 X0 X1 X2) X1) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X0) \wedge ((\neg v11_struct_0 \\ & X0) \wedge (l1_msualg_1 X0))) \wedge ((m1_subset_1 X1 (u4_struct_0 X0)) \wedge (\\ & l3_msualg_1 X2 X0))) \Rightarrow ((v1_funct_1 (k5_msualg_1 X0 X1 X2)) \wedge ((v1_funct_2 \\ & (k5_msualg_1 X0 X1 X2) (k3_msualg_1 X0 X1 X2) (k4_msualg_1 X0 X1 X2)) \wedge \\ & (m1_subset_1 (k5_msualg_1 X0 X1 X2) (k1_zfmisc_1 (k2_zfmisc_1 \\ & (k3_msualg_1 X0 X1 X2) (k4_msualg_1 X0 X1 X2)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X0)\wedge(\neg v11_struct_0 \\ & X0)\wedge(l1_msualg_1 X0)))\wedge((m1_subset_1 X1 (u4_struct_0 X0))\wedge(\\ & l3_msualg_1 X2 X0))\Rightarrow(m1_subset_1 (k3_msualg_1 X0 X1 X2) (k10_xtuple_0 \\ & (k6_finseq_2 (u1_struct_0 X0) (u3_msualg_1 X0 X2)))) \end{aligned} \quad (9)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0 X0)\wedge(\neg v11_struct_0 X0)\wedge \\ & (l1_msualg_1 X0)))\wedge(m1_subset_1 X1 (u4_struct_0 X0))\Rightarrow(m1_subset_1 \\ & (k2_msualg_1 X0 X1) (u1_struct_0 X0)) \end{aligned} \quad (10)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X1)\wedge(\neg v11_struct_0 \\ & X1)\wedge(l1_msualg_1 X1)))\wedge(m1_pralg_2 X2 X0 X1)\Rightarrow(l3_msualg_1 (\\ & k14_pralg_2 X0 X1 X2) X1) \end{aligned} \quad (11)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(((\neg v2_struct_0 X1)\wedge(l1_msualg_1 \\ & X1))\wedge(m1_pralg_2 X2 X0 X1))\Rightarrow((v1_relat_1 (k10_pralg_2 X0 X1 X2))\wedge \\ & ((v4_relat_1 (k10_pralg_2 X0 X1 X2) (u1_struct_0 X1))\wedge((v1_funct_1 \\ & (k10_pralg_2 X0 X1 X2))\wedge(v1_partfun1 (k10_pralg_2 X0 X1 X2) (u1_struct_0 \\ & X1)))))) \end{aligned} \quad (12)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0 X1)\wedge(l1_msualg_1 X1))\Rightarrow \\ & (\forall X2.(m1_pralg_2 X2 X0 X1)\Rightarrow(\forall X3.((v1_relat_1 X3)\wedge \\ & ((v4_relat_1 X3 (u1_struct_0 X1))\wedge((v1_funct_1 X3)\wedge(v1_partfun1 \\ & X3 (u1_struct_0 X1))))))\Rightarrow((X3 = k10_pralg_2 X0 X1 X2)\Leftrightarrow(\forall X4. \\ & (m1_subset_1 X4 (u1_struct_0 X1))\Rightarrow(k1_funct_1 X3 X4 = k4_card_3 \\ & (k9_pralg_2 X0 X1 X4 X2)))))) \end{aligned} \quad (13)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.\forall X3.(((\neg v2_struct_0 \\ & X0)\wedge(\neg v11_struct_0 X0)\wedge(l1_msualg_1 X0))\wedge((m1_subset_1 X2 \\ & (u1_struct_0 X0))\wedge(m1_pralg_2 X3 X1 X0)))\Rightarrow(\forall X4.(m1_subset_1 \\ & X4 (k1_funct_1 (k10_pralg_2 X1 X0 X3) X2))\Rightarrow((v1_relat_1 X4)\wedge(v1_funct_1 \\ & X4))) \end{aligned} \quad (14)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.(((\neg v2_struct_0 X0)\wedge(l1_msualg_1 X0))\wedge \\ & ((v4_msualg_1 X1 X0)\wedge(l3_msualg_1 X1 X0)))\Rightarrow(\forall X2.(m1_subset_1 \\ & X2 (k10_xtuple_0 (k6_finseq_2 (u1_struct_0 X0) (u3_msualg_1 X0 \\ & X1))))\Rightarrow(\neg v1_xboole_0 X2)) \end{aligned} \quad (15)$$

Theorem 1

$$\begin{aligned} & \forall X0. \forall X1. ((\neg v2_struct_0 X1) \wedge (\neg v11_struct_0 X1) \wedge \\ & (l1_msualg_1 X1)) \Rightarrow (\forall X2. (m1_pralg_2 X2 X0 X1) \Rightarrow (\forall X3. \\ & (m1_msualg_2 X3 X1 (k14_pralg_2 X0 X1 X2)) \Rightarrow (\forall X4. (m1_subset_1 \\ & X4 (u4_struct_0 X1)) \Rightarrow (\forall X5. (X5 \in k3_msualg_1 X1 X4 X3) \Rightarrow ((\\ & (v1_relat_1 (k1_funct_1 (k5_msualg_1 X1 X4 X3) X5)) \wedge (v1_funct_1 \\ & (k1_funct_1 (k5_msualg_1 X1 X4 X3) X5))) \wedge ((v1_relat_1 (k1_funct_1 \\ & (k5_msualg_1 X1 X4 (k14_pralg_2 X0 X1 X2)) X5)) \wedge (v1_funct_1 (k1_funct_1 \\ & (k5_msualg_1 X1 X4 (k14_pralg_2 X0 X1 X2)) X5)))))))))) \end{aligned}$$