

t20\_exchsort  
(TMS8c8SaYERTY8SrD19ArhyvHgftG2B8poj)

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Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k1\_exchsort : \iota \Rightarrow \iota$  be given. Let  $k2\_ordinal2 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v2\_exchsort : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v5\_ordinal1 : \iota \Rightarrow o$  be given. Let  $v1\_finset\_1 : \iota \Rightarrow o$  be given. Let  $k2\_ordinal1 : \iota \Rightarrow \iota$  be given. Let  $v3\_ordinal1 : \iota \Rightarrow o$  be given. Let  $k1\_setfam\_1 : \iota \Rightarrow \iota$  be given. Assume the following.

$$\forall X0. \forall X1. \neg (X0 \in X1) \wedge (v1\_xboole\_0 X1) \quad (1)$$

Assume the following.

$$\forall X0. (v1\_xboole\_0 X0) \Rightarrow (X0 = k1\_xboole\_0) \quad (2)$$

Assume the following.

$$\forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (v2\_exchsort X0 (k2\_ordinal2 (k9\_xtuple\_0 X0))) \quad (3)$$

Assume the following.

$$\forall X0. \exists X1. (v1\_relat\_1 X1) \wedge ((v5\_relat\_1 X1 X0) \wedge ((v5\_ordinal1 X1) \wedge ((v1\_funct\_1 X1) \wedge ((v1\_xboole\_0 X1) \wedge (v1\_finset\_1 X1))))) \quad (4)$$

Assume the following.

$$\forall X0. (v1\_xboole\_0 X0) \Rightarrow (v1\_xboole\_0 (k2\_ordinal1 X0)) \quad (5)$$

Assume the following.

$$\forall X0. v3\_ordinal1 (k2\_ordinal2 X0) \quad (6)$$

Assume the following.

$$\forall X0. \forall X1. (X1 = k2\_ordinal1 X0) \Leftrightarrow (\forall X2. (X2 \in X1) \Leftrightarrow ((X2 \in X0) \wedge (v3\_ordinal1 X2))) \quad (7)$$

Assume the following.

$$\begin{aligned} \forall X0.((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1.(v3\_ordinal1 \\ X1) \Rightarrow (((\exists X2.(v3\_ordinal1 X2) \wedge (X2 \in k9\_xtuple\_0 X0)) \Rightarrow (( \\ X1 = k1\_exhsort X0) \Leftrightarrow (v2\_exhsort X0 X1))) \wedge ((\forall X2.(v3\_ordinal1 \\ X2) \Rightarrow (\neg X2 \in k9\_xtuple\_0 X0)) \Rightarrow ((X1 = k1\_exhsort X0) \Leftrightarrow (X1 = k1\_xboole\_0)))))) \end{aligned} \quad (8)$$

Assume the following.

$$\forall X0.k2\_ordinal2 X0 = k1\_setfam\_1 (k2\_ordinal1 X0) \quad (9)$$

Assume the following.

$$\begin{aligned} \forall X0.\forall X1.((X0 \neq k1\_xboole\_0) \Rightarrow ((X1 = k1\_setfam\_1 X0) \Leftrightarrow \\ (\forall X2.(X2 \in X1) \Leftrightarrow (\forall X3.(X3 \in X0) \Rightarrow (X2 \in X3)))))) \wedge ((X0 = \\ k1\_xboole\_0) \Rightarrow ((X1 = k1\_setfam\_1 X0) \Leftrightarrow (X1 = k1\_xboole\_0))) \end{aligned} \quad (10)$$

**Theorem 1**

$$\forall X0.((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (k1\_exhsort X0 = k2\_ordinal2 (k9\_xtuple\_0 X0))$$