

# t20\_midsp\_2 (TMMedgBGca- muTQWiy11C6WpfBxBu89AfZs2)

October 27, 2020

Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v13\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $v2\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v3\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v4\_rlvect\_1 : \iota \Rightarrow o$  be given. Let  $v2\_midsp\_2 : \iota \Rightarrow o$  be given. Let  $l2\_algstr\_0 : \iota \Rightarrow o$  be given. Let  $l1\_midsp\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_zfmisc\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $u1\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_zfmisc\_1 : \iota \Rightarrow \iota$  be given. Let  $r1\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_midsp\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v2\_midsp\_1 : \iota \Rightarrow o$  be given. Let  $k1\_midsp\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_midsp\_1 X0)) \Rightarrow (\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X3.((\neg v2\_struct\_0 X3) \wedge ((v13\_algstr\_0 \\
& X3) \wedge ((v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 X3) \wedge (l2\_algstr\_0 X3)))))) \Rightarrow \\
& (\forall X4.((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (k2\_zfmisc\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0)) (u1\_struct\_0 X3)) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& (u1\_struct\_0 X3)))))) \Rightarrow (\neg(r1\_midsp\_2 (u1\_struct\_0 X0) X3 X4) \wedge \\
& ((v1\_midsp\_2 X4 X0 X3) \wedge (\forall X5.(m1\_subset\_1 X5 (u1\_struct\_0 \\
& X0)) \Rightarrow (k1\_midsp\_1 X0 X5 X1 \neq X2)))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_midsp\_1 X0)) \Rightarrow (\forall X1. \\
& (m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2.(m1\_subset\_1 X2 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X3.((\neg v2\_struct\_0 X3) \wedge ((v13\_algstr\_0 \\
& X3) \wedge ((v3\_rlvect\_1 X3) \wedge ((v4\_rlvect\_1 X3) \wedge (l2\_algstr\_0 X3)))))) \Rightarrow \\
& (\forall X4.((v1\_funct\_1 X4) \wedge ((v1\_funct\_2 X4 (k2\_zfmisc\_1 (u1\_struct\_0 \\
& X0) (u1\_struct\_0 X0)) (u1\_struct\_0 X3)) \wedge (m1\_subset\_1 X4 (k1\_zfmisc\_1 \\
& (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X0) (u1\_struct\_0 X0)) \\
& (u1\_struct\_0 X3)))))) \Rightarrow (((r1\_midsp\_2 (u1\_struct\_0 X0) X3 X4) \wedge \\
& (v1\_midsp\_2 X4 X0 X3)) \Rightarrow (k1\_midsp\_1 X0 X1 X2 = k1\_midsp\_1 X0 X2 X1))))))
\end{aligned} \tag{2}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l2\_algstr\_0 X0)) \Rightarrow (\forall X1. \\
& ((\neg v2\_struct\_0 X1) \wedge (l1\_midsp\_1 X1)) \Rightarrow (\forall X2.(m1\_subset\_1 \\
& X2 (u1\_struct\_0 X1)) \Rightarrow (\forall X3.((v1\_funct\_1 X3) \wedge ((v1\_funct\_2 \\
& X3 (k2\_zfmisc\_1 (u1\_struct\_0 X1) (u1\_struct\_0 X1)) (u1\_struct\_0 \\
& X0)) \wedge (m1\_subset\_1 X3 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X1) (u1\_struct\_0 X1)) (u1\_struct\_0 X0)))))) \Rightarrow ((v1\_midsp\_2 \\
& X3 X1 X0) \Rightarrow (k1\_midsp\_1 X1 X2 X2 = X2))))))
\end{aligned} \tag{3}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v2\_midsp\_2 X0) \wedge ( \\
& l2\_algstr\_0 X0)))))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge (l1\_midsp\_1 \\
& X1)) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X1) (u1\_struct\_0 X1)) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X1) (u1\_struct\_0 \\
& X1)) (u1\_struct\_0 X0)))))) \Rightarrow (((r1\_midsp\_2 (u1\_struct\_0 X1) X0 \\
& X2) \wedge (v1\_midsp\_2 X2 X1 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u1\_struct\_0 \\
& X1)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X1)) \Rightarrow (\forall X5. \\
& (m1\_subset\_1 X5 (u1\_struct\_0 X1)) \Rightarrow (\forall X6.(m1\_subset\_1 X6 \\
& (u1\_struct\_0 X1)) \Rightarrow (k1\_midsp\_1 X1 (k1\_midsp\_1 X1 X3 X4) (k1\_midsp\_1 \\
& X1 X5 X6) = k1\_midsp\_1 X1 (k1\_midsp\_1 X1 X3 X5) (k1\_midsp\_1 X1 X4 X6))))))))))
\end{aligned} \tag{4}$$

Assume the following.

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge (l1\_midsp\_1 X0)) \Rightarrow ((v2\_midsp\_1 \\
& X0) \Leftrightarrow (\forall X1.(m1\_subset\_1 X1 (u1\_struct\_0 X0)) \Rightarrow (\forall X2. \\
& (m1\_subset\_1 X2 (u1\_struct\_0 X0)) \Rightarrow (\forall X3.(m1\_subset\_1 X3 \\
& (u1\_struct\_0 X0)) \Rightarrow (\forall X4.(m1\_subset\_1 X4 (u1\_struct\_0 X0)) \Rightarrow \\
& ((k1\_midsp\_1 X0 X1 X1 = X1) \wedge ((k1\_midsp\_1 X0 X1 X2 = k1\_midsp\_1 X0 X2 \\
& X1) \wedge ((k1\_midsp\_1 X0 (k1\_midsp\_1 X0 X1 X2) (k1\_midsp\_1 X0 X3 X4) = \\
& k1\_midsp\_1 X0 (k1\_midsp\_1 X0 X1 X3) (k1\_midsp\_1 X0 X2 X4)) \wedge (\exists X5. \\
& (m1\_subset\_1 X5 (u1\_struct\_0 X0)) \wedge (k1\_midsp\_1 X0 X5 X1 = X2))))))))))
\end{aligned} \tag{5}$$

**Theorem 1**

$$\begin{aligned}
& \forall X0.((\neg v2\_struct\_0 X0) \wedge ((v13\_algstr\_0 X0) \wedge ((v2\_rlvect\_1 \\
& X0) \wedge ((v3\_rlvect\_1 X0) \wedge ((v4\_rlvect\_1 X0) \wedge ((v2\_midsp\_2 X0) \wedge ( \\
& l2\_algstr\_0 X0)))))) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge (l1\_midsp\_1 \\
& X1)) \Rightarrow (\forall X2.((v1\_funct\_1 X2) \wedge ((v1\_funct\_2 X2 (k2\_zfmisc\_1 \\
& (u1\_struct\_0 X1) (u1\_struct\_0 X1)) (u1\_struct\_0 X0)) \wedge (m1\_subset\_1 \\
& X2 (k1\_zfmisc\_1 (k2\_zfmisc\_1 (k2\_zfmisc\_1 (u1\_struct\_0 X1) (u1\_struct\_0 \\
& X1)) (u1\_struct\_0 X0)))))) \Rightarrow (((r1\_midsp\_2 (u1\_struct\_0 X1) X0 \\
& X2) \wedge (v1\_midsp\_2 X2 X1 X0)) \Rightarrow ((\neg v2\_struct\_0 X1) \wedge ((v2\_midsp\_1 X1) \wedge \\
& (l1\_midsp\_1 X1))))))
\end{aligned}$$