

# t20\_pralg\_3 (TMSmcMthc- SZH4aMnNvmonTEK1DkrqB9oowT)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $v2\_struct\_0 : \iota \Rightarrow o$  be given. Let  $v11\_struct\_0 : \iota \Rightarrow o$  be given. Let  $l1\_msualg\_1 : \iota \Rightarrow o$  be given. Let  $m1\_pralg\_2 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $u4\_struct\_0 : \iota \Rightarrow \iota$  be given. Let  $k1\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_xboole\_0 : \iota$  be given. Let  $v4\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $l3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k3\_msualg\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k14\_pralg\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k10\_funct\_6 : \iota \Rightarrow \iota$  be given. Let  $k5\_pralg\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v1\_relat\_1 : \iota \Rightarrow o$  be given. Let  $v1\_funct\_1 : \iota \Rightarrow o$  be given. Let  $k4\_card\_3 : \iota \Rightarrow \iota$  be given. Let  $k9\_xtuple\_0 : \iota \Rightarrow \iota$  be given. Let  $k2\_funct\_6 : \iota \Rightarrow \iota$  be given. Let  $k12\_pralg\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $v4\_funct\_1 : \iota \Rightarrow o$  be given. Let  $v4\_relat\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_partfun1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $v1\_funcop\_1 : \iota \Rightarrow o$  be given. Assume the following.

$$\begin{aligned} & \forall X0.((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow (\forall X1.(( \\ & v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \Rightarrow ((X0 \in k4\_card\_3 X1) \Leftrightarrow ((k9\_xtuple\_0 \\ & X0 = k9\_xtuple\_0 X1) \wedge (\forall X2.(X2 \in k9\_xtuple\_0 X1) \Rightarrow (k1\_funct\_1 \\ & X0 X2 \in k1\_funct\_1 X1 X2)))))) \end{aligned} \tag{1}$$

Assume the following.

$$\forall X0. \forall X1. (m1\_subset\_1 X0 X1) \Rightarrow ((v1\_xboole\_0 X1) \vee (X0 \in X1)) \tag{2}$$

Assume the following.

$$\forall X0. \forall X1. (X0 \in X1) \Rightarrow (m1\_subset\_1 X0 X1) \tag{3}$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge (l1\_msualg\_1 X1))) \Rightarrow (\forall X2.(m1\_pralg\_2 \\ & X2 X0 X1) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u4\_struct\_0 X1)) \Rightarrow (\forall X4. \\ & (m1\_subset\_1 X4 (k3\_msualg\_1 X1 X3 (k14\_pralg\_2 X0 X1 X2))) \Rightarrow ((k1\_msualg\_1 \\ & X1 X3 \neq k1\_xboole\_0) \Rightarrow (k10\_funct\_6 X4 \in k4\_card\_3 (k2\_funct\_6 (k12\_pralg\_2 \\ & X0 X1 X2 X3)))))))))) \end{aligned} \quad (4)$$

Assume the following.

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge (l1\_msualg\_1 X1))) \Rightarrow (\forall X2.(m1\_pralg\_2 \\ & X2 X0 X1) \Rightarrow (\forall X3.(m1\_subset\_1 X3 (u4\_struct\_0 X1)) \Rightarrow ((k9\_xtuple\_0 \\ & (k2\_funct\_6 (k12\_pralg\_2 X0 X1 X2 X3)) = X0) \wedge (\forall X4.(m1\_subset\_1 \\ & X4 X0) \Rightarrow (k1\_funct\_1 (k2\_funct\_6 (k12\_pralg\_2 X0 X1 X2 X3)) X4 = k3\_msualg\_1 \\ & X1 X3 (k5\_pralg\_2 X0 X1 X2 X4)))))) \end{aligned} \quad (5)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X1) \wedge ((\neg v11\_struct\_0 \\ & X1) \wedge (l1\_msualg\_1 X1))) \wedge (m1\_pralg\_2 X2 X0 X1)) \Rightarrow (v4\_msualg\_1 ( \quad (6) \\ & k14\_pralg\_2 X0 X1 X2) X1) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X0) \wedge ((\neg v11\_struct\_0 \\ & X0) \wedge (l1\_msualg\_1 X0))) \wedge ((v4\_msualg\_1 X1 X0) \wedge (l3\_msualg\_1 X1 \\ & X0)) \wedge (m1\_subset\_1 X2 (u4\_struct\_0 X0))) \Rightarrow (v4\_funct\_1 (k3\_msualg\_1 \\ & X0 X2 X1)) \end{aligned} \quad (7)$$

Assume the following.

$$\begin{aligned} & \forall X0. ((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow ((v1\_relat\_1 ( \quad (8) \\ & k2\_funct\_6 X0)) \wedge (v1\_funct\_1 (k2\_funct\_6 X0))) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2\_struct\_0 X1) \wedge ((\neg v11\_struct\_0 \\ & X1) \wedge (l1\_msualg\_1 X1))) \wedge (m1\_pralg\_2 X2 X0 X1)) \Rightarrow (l3\_msualg\_1 ( \quad (9) \\ & k14\_pralg\_2 X0 X1 X2) X1) \end{aligned}$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. \forall X3. (((\neg v2\_struct\_0 \\ & X1) \wedge ((\neg v11\_struct\_0 X1) \wedge (l1\_msualg\_1 X1))) \wedge ((m1\_pralg\_2 X2 \\ & X0 X1) \wedge (m1\_subset\_1 X3 (u4\_struct\_0 X1))) \Rightarrow ((v1\_relat\_1 (k12\_pralg\_2 \\ & X0 X1 X2 X3)) \wedge ((v4\_relat\_1 (k12\_pralg\_2 X0 X1 X2 X3) X0) \wedge ((v1\_funct\_1 \\ & (k12\_pralg\_2 X0 X1 X2 X3)) \wedge ((v1\_partfun1 (k12\_pralg\_2 X0 X1 X2 X3) \\ & X0) \wedge (v1\_funcop\_1 (k12\_pralg\_2 X0 X1 X2 X3)))))) \end{aligned} \quad (10)$$

Assume the following.

$$\forall X0.((v1\_relat\_1 X0) \wedge (v1\_funct\_1 X0)) \Rightarrow ((v1\_relat\_1 (k10\_funct\_6 X0)) \wedge ((v1\_funct\_1 (k10\_funct\_6 X0)) \wedge (v1\_funct\_1 (k10\_funct\_6 X0)))) \quad (11)$$

Assume the following.

$$\forall X0.(v4\_funct\_1 X0) \Rightarrow (\forall X1.(m1\_subset\_1 X1 X0) \Rightarrow (v1\_relat\_1 X1) \wedge (v1\_funct\_1 X1)) \quad (12)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(\neg v1\_xboole\_0 X0) \Rightarrow (\forall X1.((\neg v2\_struct\_0 X1) \wedge \\ & ((\neg v11\_struct\_0 X1) \wedge (l1\_msualg\_1 X1))) \Rightarrow (\forall X2.(m1\_pralg\_2 \\ & X2 X0 X1) \Rightarrow (\forall X3.(m1\_subset\_1 X3 X0) \Rightarrow (\forall X4.(m1\_subset\_1 \\ & X4 (u4\_struct\_0 X1)) \Rightarrow ((k1\_msualg\_1 X1 X4 \neq k1\_xboole\_0) \Rightarrow (\forall X5. \\ & ((v4\_msualg\_1 X5 X1) \wedge (l3\_msualg\_1 X5 X1)) \Rightarrow (\forall X6.(m1\_subset\_1 \\ & X6 (k3\_msualg\_1 X1 X4 (k14\_pralg\_2 X0 X1 X2))) \Rightarrow (m1\_subset\_1 (k1\_funct\_1 \\ & (k10\_funct\_6 X6) X3) (k3\_msualg\_1 X1 X4 (k5\_pralg\_2 X0 X1 X2 X3)))))))))) \end{aligned}$$