# t219_member_1 <br> (TMYiPuVryveDitMjxnFFQMciwfTwLxvQm46) 

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Let $v 1_{\_}$membered $: \iota \Rightarrow 0$ be given. Let $v 1 \_x c m p l x_{-} 0: \iota \Rightarrow o$ be given. Let $k 6 \_n u m b e r s: \iota$ be given. Let $k 25 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 6 \_$_subset_1 : $\iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 7$ _member_ $1: \iota \Rightarrow \iota$ be given. Let $k 23 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 4 \_x b o o l e \_0: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 1 \_$tarski $: \iota \Rightarrow \iota$ be given. Let $v 1 \_x b o o l e \_0: \iota \Rightarrow o$ be given. Let $k 15 \_$member_1 $: ~ \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $k 13 \_m e m b e r \_1: \iota \Rightarrow \iota \Rightarrow \iota$ be given. Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d \quad X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d \quad X 1\right) \Rightarrow\left(k 7 \_m e m b e r \_1\right.\right.$
( $k 6$ _subset_1 X0 X1) $=k$ _s_subset_1 ( $k 7_{-}$member_1 X0) (k7_member_1 X1))

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(\left(X 2 \neq k 6 \_n u m b e r s\right) \Rightarrow\left(k 23 \_m e m b e r \_1\right.\right.$ ( $k 6 \_$subset_1
X0 X1) X2 = k6_subset_1 (k23_member_1 X0 X2) (k23_member_1 X1 X2)))))
Assume the following.

$$
\begin{equation*}
\forall X 0 . \forall X 1 . k 6 \_ \text {subset_1 } X 0 X 1=k 4 \_x b o o l e \_0 X 0 X 1 \tag{3}
\end{equation*}
$$

Assume the following.

$$
\begin{equation*}
\forall X 0 .\left(v 1 \_x c m p l x \_0 X 0\right) \Rightarrow\left(v 1 \_m e m b e r e d\left(k 1 \_t a r s k i X 0\right)\right) \tag{4}
\end{equation*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 . \forall X 1 .\left(v 1 \_m e m b e r e d X 0\right) \Rightarrow\left(v 1 \_ m e m b e r e d ~ \left(k 4 \_x b o o l e \_0\right.\right.  \tag{5}\\
X 0 X 1))
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(\left(\neg v 1 \_x b o o l e \_0 X 0\right) \wedge\left(v 1 \_m e m b e r e d X 0\right)\right) \Rightarrow\left(\left(\neg v 1 \_x b o o l e \_0\right.\right.$
$\left.\left.\left(k 7 \_m e m b e r \_1 X 0\right)\right) \wedge\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right)\right)$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_x b o o l e \_0 X 0\right) \Rightarrow\left(\left(v 1 \_x b o o l e \_0\left(k 7 \_m e m b e r \_1 X 0\right)\right) \wedge\right.  \tag{7}\\
\left.\left(v 1 \_m e m b e r e d\left(k 7 \_m e m b e r \_1 X 0\right)\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 25 \_m e m b e r \_1\right.\right.  \tag{8}\\
\left.\left.X 0 X 1=k 15 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right)
\end{gather*}
$$

Assume the following.

$$
\begin{gather*}
\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_x c m p l x \_0 X 1\right) \Rightarrow\left(k 23 \_m e m b e r \_1\right.\right. \\
\left.\left.X 0 X 1=k 13 \_m e m b e r \_1\left(k 1 \_t a r s k i X 1\right) X 0\right)\right) \tag{9}
\end{gather*}
$$

Assume the following.
$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow\left(k 15 \_m e m b e r \_1\right.\right.$
$\left.\left.X 0 X 1=k 13 \_m e m b e r \_1 X 0\left(k 7 \_m e m b e r \_1 X 1\right)\right)\right)$

## Theorem 1

$\forall X 0 .\left(v 1 \_m e m b e r e d ~ X 0\right) \Rightarrow\left(\forall X 1 .\left(v 1 \_m e m b e r e d ~ X 1\right) \Rightarrow(\forall X 2\right.$.
$\left(v 1 \_x c m p l x \_0 X 2\right) \Rightarrow\left(\left(X 2 \neq k 6 \_n u m b e r s\right) \Rightarrow\left(k 25 \_m e m b e r \_1\right.\right.$ ( $k 6 \_$_subset_1
X0 X1) X2 = k6_subset_1 (k25_member_1 X0 X2) (k25_member_1 X1 X2)) ))

