

# t21\_cfuncdom

(TMWdLSd3cMdwP4ZkXdd3veWA4hSnyHKYSuk)

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Let  $v1\_xboole\_0 : \iota \Rightarrow o$  be given. Let  $k2\_tarski : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k2\_numbers : \iota$  be given. Let  $k9\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $r2\_funct\_2 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_funcsdom : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_cfuncdom : \iota \Rightarrow \iota$  be given. Let  $k2\_funcsdom : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k3\_cfuncdom : \iota \Rightarrow \iota$  be given. Let  $k1\_domain\_1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k1\_funct\_1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_complex1 : \iota$  be given. Let  $k6\_numbers : \iota$  be given. Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. \forall X2. (\neg v1\_xboole\_0 X2) \Rightarrow (\forall X3. \\
& (m2\_funct\_2 X3 X2 k2\_numbers (k9\_funct\_2 X2 k2\_numbers)) \Rightarrow (\forall X4. \\
& (m2\_funct\_2 X4 X2 k2\_numbers (k9\_funct\_2 X2 k2\_numbers)) \Rightarrow (((X2 = \\
& k2\_tarski X0 X1) \wedge ((\forall X5. (X5 \in X2) \Rightarrow (((X5 = X0) \Rightarrow (k1\_funct\_1 \\
& X3 X5 = k6\_complex1)) \wedge ((X5 \neq X0) \Rightarrow (k1\_funct\_1 X3 X5 = k6\_numbers)))))) \wedge \\
& (\forall X5. (X5 \in X2) \Rightarrow (((X5 = X0) \Rightarrow (k1\_funct\_1 X4 X5 = k6\_numbers)) \wedge \\
& ((X5 \neq X0) \Rightarrow (k1\_funct\_1 X4 X5 = k6\_complex1)))))) \Rightarrow ((X0 = X1) \vee (\forall X5. \\
& (m2\_funct\_2 X5 X2 k2\_numbers (k9\_funct\_2 X2 k2\_numbers)) \Rightarrow (\exists X6. \\
& (m1\_subset\_1 X6 k2\_numbers) \wedge (\exists X7. (m1\_subset\_1 X7 k2\_numbers) \wedge \\
& (r2\_funct\_2 X2 k2\_numbers X5 (k1\_funcsdom X2 k2\_numbers (k1\_cfuncdom \\
& X2) (k2\_funcsdom X2 k2\_numbers k2\_numbers (k9\_funct\_2 X2 k2\_numbers) \\
& (k3\_cfuncdom X2) (k1\_domain\_1 k2\_numbers (k9\_funct\_2 X2 k2\_numbers) \\
& X6 X3)) (k2\_funcsdom X2 k2\_numbers k2\_numbers (k9\_funct\_2 X2 k2\_numbers) \\
& (k3\_cfuncdom X2) (k1\_domain\_1 k2\_numbers (k9\_funct\_2 X2 k2\_numbers) \\
& X7 X4))))))))))
\end{aligned} \tag{1}$$

Assume the following.

$$\begin{aligned}
& \forall X0. \forall X1. (\neg v1\_xboole\_0 X1) \Rightarrow (\exists X2. (m2\_funct\_2 \\
& X2 X1 k2\_numbers (k9\_funct\_2 X1 k2\_numbers)) \wedge (\exists X3. (m2\_funct\_2 \\
& X3 X1 k2\_numbers (k9\_funct\_2 X1 k2\_numbers)) \wedge ((\forall X4. (X4 \in \\
& X1) \Rightarrow (((X4 = X0) \Rightarrow (k1\_funct\_1 X2 X4 = k6\_complex1)) \wedge ((X4 \neq X0) \Rightarrow (k1\_funct\_1 \\
& X2 X4 = k6\_numbers)))))) \wedge (\forall X4. (X4 \in X1) \Rightarrow (((X4 = X0) \Rightarrow (k1\_funct\_1 \\
& X3 X4 = k6\_numbers)) \wedge ((X4 \neq X0) \Rightarrow (k1\_funct\_1 X3 X4 = k6\_complex1))))))
\end{aligned} \tag{2}$$

**Theorem 1**

$$\begin{aligned} & \forall X0.\forall X1.\forall X2.(\neg v1\_xboole\_0 X2)\Rightarrow(\neg(X2 = k2\_tarski \\ & X0 X1)\wedge((X0\neq X1)\wedge(\forall X3.(m2\_funct\_2 X3 X2 k2\_numbers (k9\_funct\_2 \\ & X2 k2\_numbers))\Rightarrow(\forall X4.(m2\_funct\_2 X4 X2 k2\_numbers (k9\_funct\_2 \\ & X2 k2\_numbers))\Rightarrow(\exists X5.(m2\_funct\_2 X5 X2 k2\_numbers (k9\_funct\_2 \\ & X2 k2\_numbers))\wedge(\forall X6.(m1\_subset\_1 X6 k2\_numbers)\Rightarrow(\forall X7. \\ & (m1\_subset\_1 X7 k2\_numbers)\Rightarrow(\neg r2\_funct\_2 X2 k2\_numbers X5 (k1\_funcsdom \\ & X2 k2\_numbers (k1\_cfuncsdom X2) (k2\_funcsdom X2 k2\_numbers k2\_numbers \\ & (k9\_funct\_2 X2 k2\_numbers) (k3\_cfuncsdom X2) (k1\_domain\_1 k2\_numbers \\ & (k9\_funct\_2 X2 k2\_numbers) X6 X3)) (k2\_funcsdom X2 k2\_numbers k2\_numbers \\ & (k9\_funct\_2 X2 k2\_numbers) (k3\_cfuncsdom X2) (k1\_domain\_1 k2\_numbers \\ & (k9\_funct\_2 X2 k2\_numbers) X7 X4)))))))))) \end{aligned}$$