

t21\_hilbert1 (TMFHwD-  
JxsWVpMY27CD6U4yDoMZzPDBgSWfW)

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Let  $m1\_subset\_1 : \iota \Rightarrow \iota \Rightarrow o$  be given. Let  $k1\_hilbert1 : \iota$  be given. Let  $k3\_hilbert1 : \iota \Rightarrow \iota \Rightarrow \iota$  be given. Let  $k6\_hilbert1 : \iota$  be given. Assume the following.

$$\begin{aligned} & \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k1\_hilbert1) \Rightarrow (( \\ & k3\_hilbert1 X0 (k3\_hilbert1 X1 X2) \in k6\_hilbert1) \Rightarrow (k3\_hilbert1 \\ & X1 (k3\_hilbert1 X0 X2) \in k6\_hilbert1)))) \end{aligned} \quad (1)$$

Assume the following.

$$\begin{aligned} & \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k1\_hilbert1) \Rightarrow (k3\_hilbert1 \\ & (k3\_hilbert1 X0 X1) (k3\_hilbert1 (k3\_hilbert1 X2 X0) (k3\_hilbert1 \\ & X2 X1)) \in k6\_hilbert1))) \end{aligned} \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0.\forall X1.((m1\_subset\_1 X0 k1\_hilbert1) \wedge (m1\_subset\_1 \\ & X1 k1\_hilbert1)) \Rightarrow (m1\_subset\_1 (k3\_hilbert1 X0 X1) k1\_hilbert1) \end{aligned} \quad (3)$$

**Theorem 1**

$$\begin{aligned} & \forall X0.(m1\_subset\_1 X0 k1\_hilbert1) \Rightarrow (\forall X1.(m1\_subset\_1 \\ & X1 k1\_hilbert1) \Rightarrow (\forall X2.(m1\_subset\_1 X2 k1\_hilbert1) \Rightarrow (k3\_hilbert1 \\ & (k3\_hilbert1 X0 X1) (k3\_hilbert1 (k3\_hilbert1 X1 X2) (k3\_hilbert1 \\ & X0 X2)) \in k6\_hilbert1))) \end{aligned}$$