

t21_polyalg1 (TM-
box58DKJJXXhSwwtqLmXvEDqpk27bCQ8m)

October 27, 2020

Let $v2_struct_0 : \iota \Rightarrow o$ be given. Let $l3_algstr_0 : \iota \Rightarrow o$ be given. Let $l1_polyalg1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $v1_xboole_0 : \iota \Rightarrow o$ be given. Let $m1_subset_1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k1_zfmisc_1 : \iota \Rightarrow \iota$ be given. Let $u1_struct_0 : \iota \Rightarrow \iota$ be given. Let $v3_polyalg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $k2_polyalg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow \iota$ be given. Let $v1_polyalg1 : \iota \Rightarrow \iota \Rightarrow o$ be given. Let $m1_polyalg1 : \iota \Rightarrow \iota \Rightarrow \iota \Rightarrow o$ be given. Let $r1_tarski : \iota \Rightarrow \iota \Rightarrow o$ be given. Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge (l3_algstr_0 X0)) \Rightarrow (\forall X1. \\ & ((\neg v2_struct_0 X1) \wedge (l1_polyalg1 X1 X0)) \Rightarrow (\forall X2.(m1_subset_1 \\ & X2 (k1_zfmisc_1 (u1_struct_0 X1))) \Rightarrow (\neg (v3_polyalg1 X2 X0 X1) \wedge (\\ & \forall X3.((v1_polyalg1 X3 X0) \wedge (m1_polyalg1 X3 X0 X1)) \Rightarrow (u1_struct_0 \\ & X3 \neq X2)))))) \end{aligned} \quad (1)$$

Assume the following.

$$\forall X0. \forall X1. r1_tarski X0 X0 \quad (2)$$

Assume the following.

$$\begin{aligned} & \forall X0. \forall X1. \forall X2. (((\neg v2_struct_0 X0) \wedge (l3_algstr_0 \\ & X0)) \wedge (((\neg v2_struct_0 X1) \wedge (l1_polyalg1 X1 X0)) \wedge ((\neg v1_xboole_0 \\ & X2) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (u1_struct_0 X1)))))) \Rightarrow ((\neg v2_struct_0 \\ & (k2_polyalg1 X0 X1 X2)) \wedge ((v1_polyalg1 (k2_polyalg1 X0 X1 X2) X0) \wedge \\ & (m1_polyalg1 (k2_polyalg1 X0 X1 X2) X0 X1))) \end{aligned} \quad (3)$$

Assume the following.

$$\begin{aligned} & \forall X0.((\neg v2_struct_0 X0) \wedge (l3_algstr_0 X0)) \Rightarrow (\forall X1. \\ & ((\neg v2_struct_0 X1) \wedge (l1_polyalg1 X1 X0)) \Rightarrow (\forall X2.((\neg v1_xboole_0 \\ & X2) \wedge (m1_subset_1 X2 (k1_zfmisc_1 (u1_struct_0 X1)))) \Rightarrow (\forall X3. \\ & ((\neg v2_struct_0 X3) \wedge ((v1_polyalg1 X3 X0) \wedge (m1_polyalg1 X3 X0 X1))) \Rightarrow \\ & ((X3 = k2_polyalg1 X0 X1 X2) \Leftrightarrow ((r1_tarski X2 (u1_struct_0 X3)) \wedge (\\ & \forall X4.(m1_polyalg1 X4 X0 X1) \Rightarrow ((r1_tarski X2 (u1_struct_0 \\ & X4)) \Rightarrow (r1_tarski (u1_struct_0 X3) (u1_struct_0 X4)))))))))) \end{aligned} \quad (4)$$

Assume the following.

$$\forall X0.\forall X1.(X0 = X1) \Leftrightarrow ((r1_tarski\ X0\ X1) \wedge (r1_tarski\ X1\ X0)) \quad (5)$$

Theorem 1

$$\begin{aligned} & \forall X0.((\neg v2_struct_0\ X0) \wedge (l3_algstr_0\ X0)) \Rightarrow (\forall X1. \\ & ((\neg v2_struct_0\ X1) \wedge (l1_polyalg1\ X1\ X0)) \Rightarrow (\forall X2.((\neg v1_xboole_0 \\ & X2) \wedge (m1_subset_1\ X2\ (k1_zfmisc_1\ (u1_struct_0\ X1)))) \Rightarrow ((v3_polyalg1 \\ & X2\ X0\ X1) \Rightarrow (u1_struct_0\ (k2_polyalg1\ X0\ X1\ X2) = X2)))) \end{aligned}$$